

Crystal structures and X-ray powder diffraction data for AAIGe2O6 synthetic leucite analogs (A = K, Rb, Cs)

BELL, Anthony https://orcid.org/0000-0001-5038-5621 Available from Sheffield Hallam University Research Archive (SHURA) at: https://shura.shu.ac.uk/33734/

This document is the Published Version [VoR]

Citation:

BELL, Anthony (2024). Crystal structures and X-ray powder diffraction data for AAIGe2O6 synthetic leucite analogs (A = K, Rb, Cs). Powder Diffraction. [Article]

Copyright and re-use policy

See http://shura.shu.ac.uk/information.html

Crystal structures and X-ray powder diffraction data for $AAIGe_2O_6$ synthetic leucite analogs (A = K, Rb, Cs)

Anthony M. T. Bell (Da)

Materials and Engineering Research Institute, Sheffield Hallam University, Sheffield S1 1WB, UK

(Received 19 February 2024; accepted 5 May 2024)

Leucites are tetrahedrally coordinated silicate framework structures with some of the silicon framework cations that are partially replaced by divalent or trivalent cations. These structures have general formulae $A_2BSi_5O_{12}$ and $ACSi_2O_6$, where A is a monovalent alkali metal cation, B is a divalent cation, and C is a trivalent cation. There are also leucite analogs with analogous tetrahedrally coordinated **germanate** framework structures. These have general formulae $A_2BGe_5O_{12}$ and $ACGe_2O_6$. In this paper, the Rietveld refinements of three synthetic Ge-leucite analogs with stoichiometries of $AAlGe_2O_6$ (A = K, Rb, Cs) are discussed. $KAlGe_2O_6$ is $I4_1/a$ tetragonal and is isostructural with $KAlSi_2O_6$. RbAlGe $_2O_6$ and CsAlGe $_2O_6$ are $I\bar{4}3d$ cubic and are isostructural with $KBSi_2O_6$. © The Author(s), 2024. Published by Cambridge University Press on behalf of International Centre for Diffraction Data. This is an Open Access article, distributed under the terms of the Creative Commons Attribution licence (http://creativecommons.org/licenses/by/4.0/), which permits unrestricted re-use, distribution and reproduction, provided the original article is properly cited. [doi:10.1017/S088571562400023X]

Keywords: powder diffraction, Rietveld refinement, leucite minerals, germanate framework structures

I. INTRODUCTION

Synthetic anhydrous analogs of the silicate framework minerals such as leucite (KAlSi₂O₆) and pollucite (CsAlSi₂O₆) can be prepared with the general formulae A_2B Si₅O₁₂ and ACSi₂O₆, where A is a monovalent alkali metal cation, B is a divalent cation, and C is a trivalent cation. These structures have the same topology, with B and C cations partially substituting onto tetrahedrally coordinated sites (T-sites) in the silicate framework, and charge-balancing A cations sitting in extraframework channels. The A cations can be replaced by ion exchange, and Cs-containing silicate framework minerals are of potential technological interest as storage media for radioactive Cs from nuclear waste (Gatta et al., 2008, 2009).

Many ambient temperature leucite analogs are known with different crystal structures and different *A*, *B*, and *C* cations (Bell, 2024). These structures all have the same topology, CsAlSi₂O₆ is *Ia*3*d* cubic (Beger, 1969), KBSi₂O₆ is *I*43*d* cubic (Millini et al., 1993), and KAlSi₂O₆ is *I*41/*a* tetragonal (Mazzi et al., 1976). All these high symmetry structures have *disordered* T-site cations. However, lower symmetry structures are also known with *ordered* T-site cations. Examples of these cation-ordered structures are Eu²⁺-doped CsZnSi₂O₆ (Hariyani et al., 2020, *Pa*3̄ *cubic*), Cs₂CdSi₅O₁₂ (Bell et al., 1994b, *Pbca* orthorhombic), and K₂MgSi₅O₁₂ (Bell et al., 1994a, *P*2₁/*c* monoclinic).

However, it is also possible to synthesize analogs of leucite and pollucite in which silicon is replaced with germanium. These Ge-leucites have **germanate** framework structures with the same topology as the leucite structure. In these cases,

 A_2B Ge₅O₁₂ and ACGe₂O₆ leucite analogs can be synthesized where B and C cations partially substitute onto tetrahedrally coordinated sites (T-sites) in the **germanate** framework, and charge-balancing A cations sit in extraframework channels.

Lattice parameters have been reported for A_2B Ge₅O₁₂ analogs (A = Rb, Cs; B = Be, Mg, Zn, Co, Fe, Ni, Cu, Cd) (Richerson and Hummel, 1972; Torres-Martinez et al., 1984; Torres-Martinez and West, 1989). Lattice parameters have also been reported for analogs ACGe₂O₆ (A = K, Rb, Cs, NH₄; C = B, Al, Ga, Cr, Fe) (Torres-Martinez et al., 1984; Torres-Martinez and West, 1989). Additionally, lattice parameters have been reported for $K_{0.8}$ Rb_{0.2}AlGe₂O₆ (Klaska, 1978).

This paper reports the Rietveld refinements (Rietveld, 1969) of three Ge-leucites with stoichiometries of $AAlGe_2O_6$ (A=K, Rb, Cs). A crystal structure has been reported for $CsAlGe_2O_6$ (Tripathi and Parise, 2002), but no crystal structures have yet been reported for the K and Rb analogs. Powder Diffraction File (Gates-Rector and Blanton, 2019) data have been reported for these three Ge-leucite analogs. The PDF numbers are 00-37-1349 (KAlGe $_2O_6$), 00-37-348 (RbAlGe $_2O_6$), 00-37-347, and 04-012-2039 (CsAlGe $_2O_6$).

II. EXPERIMENTAL

A. Sample synthesis

All three samples were prepared from appropriate stoichiometric mixtures of K_2CO_3 , Rb_2CO_3 , $Cs_2CO_3.3H_2O$, GeO_2 , and Al_2O_3 . These mixtures were loaded into Pt crucibles and heated in air in a furnace. For all three samples, the mixtures were heated for 12 h at 1073 K (to decompose carbonates). For A = K, the crucible was air quenched, but for



Powder Diffraction, 2024 0885-7156/2024/1/8/\$18.00 © 2024 JCPDS-ICDD

^{a)}Author to whom correspondence should be addressed. Electronic mail: anthony.bell@shu.ac.uk

 $A = \mathrm{Rb}$ and Cs the crucibles were quenched by dipping the bottom of the crucible in the bucket of cold water. For $A = \mathrm{K}$, the mixture was then heated for 3 days at 1373 K. The sample was then removed from the furnace, reground, and then reheated for 4 days at 1373 K. For $A = \mathrm{Rb}$, the mixture was then reground before further heating for 4 days at 1373 K. For $A = \mathrm{Cs}$, the mixture was then reground before further heating for 50 h at 1373 K. The sample was then ground again before heating for 1 more day at 1373 K.

B. X-ray powder diffraction data collection

After heating, the samples were removed from the Pt crucibles, ground with a mortar and pestle, and then mounted on low-background silicon wafers with a drop of acetone prior to ambient temperature X-ray powder diffraction.

For A = K, data were collected on a PANalytical X'Pert Pro MPD using Cu $K\alpha$ X-rays, with a nickel β -filter and a 3.3473° 2θ wide 255 channel PIXCEL-1D area detector. Data were collected in two scans using Data Collector 5.5a (PANalytical, 2017), scan 1 lasted 1 h, and scan 2 lasted 7 h and 30 min. These data were collected over the range of 5–100° 2θ with a step width of 0.0131° 2θ and an effective counting times of 118 s per point (scan 1) and 919 s per point (scan 2). For both scans, the beam size was defined with a 20 mm mask, fixed antiscatter ($\frac{1}{4}$ °), and divergence ($\frac{1}{8}$ °) slits. These two scans were summed together after data collection.

For A=Rb, data were also collected on a PANalytical X'Pert Pro MPD using Cu $K\alpha$ X-rays, with a nickel β -filter and a 3.3473° 2θ wide 255 channel PIXCEL-1D area detector. Data were collected in a single scan over 22 h using Data Collector 5.5a (PANalytical, 2017). These data were collected over the range of $10-100^{\circ}$ 2θ with a step width of 0.0131° 2θ and an effective counting time of 2838 s per point. The beam size was defined with a 20 mm mask, fixed antiscatter (1/4°), and divergence (1/8°) slits.

For A = Cs, data were collected on a PANalytical Empyrean diffractometer using Co $K\alpha$ X-rays with an iron β -filter and a 3.3473° 2θ wide 255 channel PIXCEL-3D area detector. Data were collected in a single scan over 19 h using Data Collector 5.1a (PANalytical, 2014). These data were collected over the range of 15–100° 2θ with a step width of 0.0131° 2θ and an effective counting time of 2592 s per point. The beam size was defined with a 20 mm mask, fixed divergence antiscatter ($^{1}\!4^{\circ}$) slit, and automatic divergence slit with a 20 mm long beam footprint. These diffracted intensities were converted from an automatic divergence slit mode to a fixed divergence slit mode in HighScore Plus (PANalytical, 2009) prior to data analysis.

No smoothing or α_2 stripping was done on any of these data. Both diffractometers were calibrated with an external NIST SRM640e silicon standard.

C. X-ray powder diffraction data analysis

All powder diffraction data were analyzed using HighScore Plus and the ICDD Powder Diffraction File. For A = K, analysis of the powder diffraction data showed that this sample was mostly KAlGe₂O₆ (PDF# 00-37-1349) with GeO₂ (PDF# 00-43-1016) and KAlGeO₄ (PDF# 01-78-1173) present as minor phases. For A = Rb, analysis

of the powder diffraction data showed that this sample was mostly RbAlGe₂O₆ (PDF# 00-37-0348) with GeO₂ (PDF# 04-03-0650) and Al₂O₃ (PDF# 01-73-5928) present as minor phases. For A = Cs, analysis of the powder diffraction data showed that this sample was single-phase CsAlGe₂O₆ (PDF# 00-37-0347), apart from an unassigned Bragg reflection at about 17.8° 2θ .

All Rietveld refinements (Rietveld, 1969) for these data were done using GSAS-II (Toby and von Dreele, 2013). Table I shows details of the refinements, including the number of observed and calculated reflections, the number of structural parameters and profile parameters, and the *R* factors.

For A = K, the crystal structure of KAlGe₂O₆ was refined using the I4₁/a tetragonal structure of KAlSi₂O₆ (Mazzi et al., 1976) as a starting model. The lattice parameters from PDF# 00-37-1349 were used and Ge atoms were put on the Si sites. The crystal structures of GeO₂ (Haines et al., 2002) and KAlGeO₄ (Sun et al., 2019) were used for the minor phases. Rietveld refinement showed that for A = K, the sample consisted of 98.1(5) wt% KAlGe₂O₆, 0.32(31) wt% GeO₂, and 1.57(7) wt% KAlGeO₄. In this KAlGe₂O₆ crystal structure, all atoms were located on the I4₁/a 16f Wyckoff general position. There is one 16f position for K, three 16f positions for T-sites (disordered 1/3rd Al and 2/3rd Ge), and six 16f positions for O. The isotropic temperature factors of the T-site atoms Al and Ge were constrained to be the same on each T-site but were allowed to vary between different T-sites. All isotropic temperature factors for the six O sites were constrained to have the same value. The T-O interatomic distances were soft-constrained to be $1.74 \pm 0.02 \,\text{Å}$ (average bond distance for tetrahedral Al-O and Ge-O). This assumption is made due to complete T-site disorder (1/3rd Al and 2/3rd Ge on each T-site) as it was not possible to refine chemically sensible T-site occupancies. This constraint distance was determined from the differences between the ionic radii for Si⁴⁺ and Ge⁴⁺ (Shannon, 1976) and then added the difference to the KAlSi₂O₆ T–O soft constraint distance of 1.68 ± 0.02 Å.

For A = Cs, the crystal structure of $CsAlGe_2O_6$ was refined using the $I\bar{4}3d$ cubic structure of $CsAlGe_2O_6$ (Tripathi and Parise, 2002) as a starting model. Due to the presence of the unassigned Bragg reflection at about 17.8° 2θ , the data from 15 to 18° 2θ were excluded from the Rietveld refinement, which was then done assuming a single phase of $CsAlGe_2O_6$. For A = Rb, the crystal structure of $CsAlGe_2O_6$ was used as a starting model, the lattice parameters from PDF# 00-37-0348 were used, and Rb was replaced Cs in the extraframework cation site. The crystal structures of GeO_2 (Haines et al., 2002) and Al_2O_3 (Finger and Hazen, 1978) were used for the minor phases. Rietveld refinement showed that for A = Rb, the sample consisted of 88.80(24)

TABLE I. Details of Rietveld refinements.

Stoichiometry	$KAlGe_2O_6$	$RbAlGe_2O_6$	CsAlGe ₂ O ₆
Observed reflections	97	81	47
Calculated reflections	1654	181	88
Refined parameters	61	40	35
R_factor	0.03171	0.02881	0.01237
wR_factor	0.04540	0.04605	0.02060
wR_expected	0.01253	0.00565	0.00800
goodness_of_fit	3.62	8.15	2.347

2

TABLE II. Refined lattice parameters compared with those for starting structures.

Stoichiometry	Space group	a (Å)	b (Å)	c (Å)	$V(\mathring{A}^3)$
KAlSi ₂ O ₆ ^a	I4 ₁ /a	13.09(1)	13.09(1)	13.75(1)	2356(4)
KAlGe ₂ O ₆ ^b	I4 ₁ /a	13.3316(5)	13.3316(5)	14.3206(3)	2545.23(19)
CsAlGe ₂ O ₆ ^c	$I\bar{4}3d$	13.945(2)	13.945(2)	13.945(2)	2711.8(5)
CsAlGe ₂ O ₆ ^b	$I\bar{4}3d$	13.8951(6)	13.8951(6)	13.8951(6)	2682.8(3)
RbAlGe ₂ O ₆ ^b	$I\bar{4}3d$	13.7153(5)	13.7153(5)	13.7153(5)	2579.97(26)

^aMazzi et al. (1976)

wt% RbAlGe₂O₆, 0.24(7) wt% GeO₂, and 10.96(23) wt% Al₂O₃. For both A = Cs and A = Rb, the T–O interatomic distances were also soft-constrained to be 1.74 ± 0.02 Å.

VESTA (Momma and Izumi, 2011) was used to plot crystal structures.

III. RESULTS AND DISCUSSION

Crystal structures have been refined for $AAlGe_2O_6$ (A = K, Rb, Cs) synthetic leucite analogs from X-ray powder diffraction data. The crystal structure of $KAlGe_2O_6$ is isostructural with the $I4_1/a$ tetragonal structure of $KAlSi_2O_6$. The crystal structures of $RbAlGe_2O_6$ and $CsAlGe_2O_6$ are both isostructural with the $I\bar{4}3d$ cubic structure of $CsAlGe_2O_6$ (Tripathi and Parise, 2002). All refined structures have disordered T-site cations.

Table II shows the comparison of the refined lattice parameters for AAlGe₂O₆ (*A* = K, Rb, Cs) with the starting structures used for Rietveld refinement. Table III, Table IV, and Table V similarly show refined interatomic distances and angles. Table VI shows the tetrahedral angle variances for the T-sites (Robinson et al., 1971) in these germanate framework structures.

A. KAIGe₂O₆ structure

Figures 1 and 2, respectively, show the Rietveld difference and the VESTA crystal structure plots for the refined crystal structure of KAlGe₂O₆. Table II shows that this crystal

structure has a unit cell volume that is larger than the isostructural KAlSi₂O₆, which was used as a starting model for Rietveld refinement, reflecting the difference between the ionic radii for Si⁴⁺ and Ge⁴⁺ (Shannon, 1976).

B. RbAlGe₂O₆ structure

Figures 3 and 4, respectively, show the Rietveld difference and the VESTA crystal structure plots for the refined crystal structure of RbAlGe₂O₆. Table II shows that the crystal structure of RbGaSi₂O₆ has a smaller unit cell volume than that of CsGaSi₂O₆, which was used as a starting model for Rietveld refinement. This also reflects the difference in the ionic radii for Rb⁺ and Cs⁺ cations (Shannon, 1976).

C. CsAlGe₂O₆ structure

Figures 5 and 6, respectively, show the Rietveld difference and the VESTA crystal structure plots for the refined crystal structure of CsAlGe₂O₆. Table II shows that the crystal structure of CsAlGe₂O₆ has a slightly smaller unit cell volume than that of the CsAlGe₂O₆ structure (Tripathi and Parise, 2002), which was used as a starting model for Rietveld refinement.

D. Comparisons between AAIGe₂O₆ structures

Figures 2, 4, and 6 show plots of the $AAIGe_2O_6$ crystal structures. Figure 2 (A = K) shows that the central channel

TABLE III. Refined interatomic A–O distances (Å) (A = K, Rb, Cs).

K1-O1 ¹	3.088(15)	Rb1-O1 ^{1,2,3}	4.000(10)
K1–O1 ²	3.607(15)	Rb1–O1 ^{16,17,18}	3.392(9)
K1-O2 ¹	4.268(12)	Rb1-O2 ^{4,5,6}	3.084(8)
K1-O2 ¹⁴	2.974(14)	Rb1-O2 ^{16,17,18}	3.467(11)
K1-O3 ⁴	3.855(15)	Mean Rb-O	3.486(10)
$K1-3^8$	3.062(11)	Cs1-O1 ^{1,2,3}	3.435(8)
K1-O4 ⁸	3.065(14)	Cs1-O1 ^{16,17,18}	3.862(12)
K1-O4 ¹⁴	3.784(13)	$Cs1-O2^{4,5,6}$	3.246(11)
K1-O5 ¹	2.822(11)	Cs1-O2 ^{16,17,18}	3.957(11)
K1-O5 ⁴	3.630(17)	Mean Cs–O	3.625(11)
K1-O6 ¹	3.860(14)		
K1-O6 ⁴	3.162(13)		
Mean K-O	3.431(14)		
A = K symmetry operations for	or O atoms in A-O distances:	A = Rb and Cs symmetry operation	ons for O atoms in A-O
$^{1}x,y,z;$ $^{2}3/4 - y,1/4 + x,1/4 + z;$	$4^{4}3/4 + y,3/4 - x,3/4 + z;$	distances: ${}^{1}x,y,z^{2}z,x,y^{3}y,z,x^{4}3/4$	$+y$, $1/4 - x$, $3/4 - z$ $^{5}3/4 - z$,
$81/4 - y, 1/4 + x, 1/4 - z^{14}3/4$	+y,1/4-x,1/4-z	$3/4 + y, 1/4 - x^{6}1/4 - x, 3/4 - z, 3/4$	$/4 + y^{16}3/4 + x, 3/4 + z, 3/4 + y$
•		$^{17}3/4 + y, 3/4 + x, 3/4 + z$ $^{18}3/4 + z, 3/4 + z$	3/4 + y, 3/4 + x

3 Powder Diffr., 2024 Bell 3

bThis work.

^cTripathi and Parise (2002).

A = K		A = Rb	
T1-O1 ¹	1.727(5)	T1-O1 ¹	1.619(5)
T1-O1 ⁸	1.729(6)	T1-O1 ⁴⁵	1.630(5)
T1-O2 ¹	1.726(6)	$T1-O2^1$	1.776(5)
$T1-O4^2$	1.699(6)	$T1-O2^4$	1.725(6)
T2-O2 ¹	1.733(6)	Mean T-O	1.688(5)
T2-O3 ¹	1.707(6)	A = Cs	
T2-O4 ¹	1.675(6)	T1-O1 ¹	1.729(5)
T2-O5 ¹	1.776(6)	T1-O1 ⁴⁵	1.719(5)
T3-O3 ⁴	1.681(6)	$T1-O2^1$	1.716(5)
T3-O5 ¹	1.712(6)	$T1-O2^4$	1.723(5)
T3-O6 ¹	1.702(6)	Mean T-O	1.722(5)
T3-O6 ¹⁴	1.733(6)		
Mean T-O	1.717(6)		
A = K symmetry operations for G	O atoms in T–O distances:	A = Rb and Cs symmetry for O	atom operations for T-O
$^{1}x,y,z;$ $^{2}3/4 - y,1/4 + x,1/4 + z;$ $^{4}3$	3/4 + y, 3/4 - x, 3/4 + z;	distances: ${}^{1}x,y,z$ ${}^{45}3/4+z,1/4-$	$y,3/4 - x^43/4 + y,1/4 - x,$
$x^{8}1/4 - y, 1/4 + x, 1/4 - z^{14}3/4 + y, 1/4 - x, 1/4 - z$		3/4 - z	

for the $I4_1/a$ tetragonal structure shows greater framework collapse (Taylor and Henderson, 1968) compared to the corresponding channels for the $I\overline{4}3d$ cubic structures for A = Rb and Cs, reflecting the differences in the sizes of the extraframework alkali metal cations (Shannon, 1976).

Table III shows that the mean A–O distances are smallest for A = K and largest for A = Cs, also reflecting the differences

TABLE V. Refined interatomic angles (°) (T = Al/Ge).

A = K		A = Rb			
O1-T1-O1 ^{1,8}	116.2(7)	O1-T1-O1 ^{1,45}	103.3(7)		
$O1-T1-O2^{1,1}$	111.8(7)	$O1-T1-O2^{1,1}$	102.6(5)		
$O1-T1-O2^{8,1}$	104.0(6)	O1-T1-O2 ^{45,1}	115.7(4)		
O1-T1-O4 ^{1,2}	107.8(7)	$O1-T1-O2^{1,4}$	114.7(4)		
O1-T1-O4 ^{8,2}	105.7(6)	O1-T1-O2 ^{45,4}	106.7(4)		
O2-T1-O4 ^{1,2}	111.2(6)	$O2-T1-O2^{1,4}$	113.6(7)		
O2-T2-O3 ^{1,1}	96.0(6)	T1-O1-T1 ^{1,14}	148.6(6)		
O2-T2-O4 ^{1,1}	106.6(5)	T1-O2-T1 ^{1,13}	128.6(5)		
O3-T2-O4 ^{1,1}	111.9(5)	Mean O-T1-O	109.4(5)		
O2-T2-O5 ^{1,1}	110.0(5)	Mean T1-O-T1	138.6(5)		
O3-T2-O5 ^{1,1}	112.1(9)	A = Cs			
O4-T2-O5 ^{1,1}	117.9(8)	O1-T1-O1 ^{1,45}	129.2(6)		
O3-T3-O5 ^{4,1}	118.8(7)	$O1-T1-O2^{1,1}$	113.1(6)		
O3-T3-O6 ^{4,1}	113.5(5)	O1-T1-O2 ^{45,1}	109.2(5)		
O5-T3-O6 ^{1,1}	108.0(6)	$O1-T1-O2^{1,4}$	102.2(5)		
O3-T3-O6 ^{4,14}	99.0(6)	$O1-T1-O2^{45,4}$	106.1(6)		
O5-T3-O6 ^{1,14}	117.6(6)	$O2-T1-O2^{1,4}$	88.0(8)		
O6-T3-O6 ^{1,14}	98.0(7)	T1-O1-T1 ^{1,14}	128.1(7)		
T2-O1-T1 ^{1,14}	139.8(6)	T1-O2-T1 ^{1,13}	141.4(7)		
T1-O2-T2 ^{1,1}	150.3(7)	Mean O-T1-O	108.0(6)		
T2-O3-T3 ^{1,2}	132.0(5)	Mean T1-O-T1	134.8(7)		
T2-O4-T2 ^{4,1}	140.3(7)				
T2-O5-T3 ^{1,1}	124.4(4)				
T3-O6-T3 ^{1,8}	131.7(6)				
Mean O-T1-O	109.5(6)				
Mean O-T2-O	109.1(6)				
Mean O-T3-O	109.2(6)				
Mean T-O-T	136.4(6)				
A = K symmetry operations for O		A = Rb and Cs symm	A = Rb and Cs symmetry		
	atoms in O-T-O angles and		operations for O atoms in O-T-		
	for T atoms in T-O-T angles:		O angles and for T atoms in T-		
$^{1}x,y,z;$ $^{2}3/4-y,1/$			O–T angles: $^{1}x, y, z^{45} 3/4 + z, 1/$		
4 3/4 + y,3/4 - x,3		$4 - y, 3/4 - x^4 3/4$			
4 - y, 1/4 + x, 1/4	$-z^{14}3/4+$	$x,3/4-z^{14}3/4-$			
y, $1/4 - x$, $1/4 - z$		$+x^{13} 1/4 - y, 1/4$	+x,3/4-z		

in the sizes of the extraframework alkali metal cations (Shannon, 1976). Table IV shows that there are some significant differences between the mean T–O distances in these crystal structures. All refinements were done assuming stoichiometries of $AAlGe_2O_6$, with Ge and Al in a 2:1 ratio. However, the presence of impurity phases in the A=K and Rb samples could mean that the Ge and Al may not be in an exact 2:1 ratio. This could change the mean size of the T-site cation and consequently change the mean T–O distances.

Table V shows the intratetrahedral (O–T–O) and intertetrahedral (T–O–T) angles for the three crystal structures. The mean O–T–O angles are close to the ideal tetrahedral angle of 109.47° , and the mean T–O–T angles for the three structures are similar. Table VI shows that the greatest tetrahedral distortion is for the A = Cs structure.

E. Future work on the KAIGe₂O₆ structure

The crystal structure of KAlGe₂O₆ is isostructural with the $I4_1/a$ tetragonal structure of KAlSi₂O₆ (Mazzi et al., 1976) and KGaSi₂O₆ (Bell and Henderson, 2020). Both $I4_1/a$ silicate structures undergo high temperature-phase transitions to $Ia\bar{3}d$ cubic structures, which was isostructural with CsAlSi₂O₆ (Beger, 1969). The phase transition temperatures were 943 K (KAlSi₂O₆, Palmer et al., 1997) and 673–970 K (KGaSi₂O₆, Bell and Henderson, 2020). It would be interesting to see if KAlGe₂O₆ would undergo a similar phase transition on heating, would there be a phase transition to an $Ia\bar{3}d$ or $I\bar{4}3d$ cubic structure?

TABLE VI. Tetrahedral angle variance $[\sigma^2, \deg^2]$: $\sigma^2 = \Sigma(\theta - 109.47)^2/5$ (Robinson et al., 1971) where θ is the O–T–O tetrahedral angle.

Stoichiometry	Space group	σ^2 (T1) deg	σ^2 (T2) deg	σ^2 (T3) deg	σ^2 (T) \deg^2
KAlGe ₂ O ₆ RbAlGe ₂ O ₆ CsAlGe ₂ O ₆	I4 ₁ /a I43d I43d	19.76	54.79	82.55	52.36 (31.47) 35.23 185.54

Mean variance and standard deviation are given for the three tetrahedral sites in the $A = K I A_1 / a$ structure. Variance is given for the single tetrahedral site in the A = Rb and Cs $I \bar{4} 3 d$ structures.

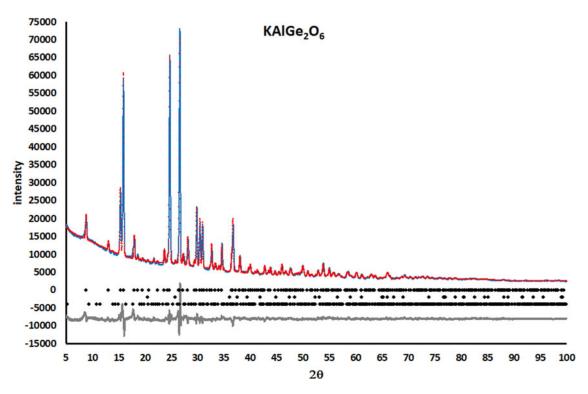


Figure 1. Rietveld difference plot for $KAlGe_2O_6$. Red circles represent observed data points, blue line represents calculated data points, and the green line represents difference curves. The upper line of black crosses represents positions of Bragg reflections for $KAlGe_2O_6$, the middle line of black crosses represents positions of Bragg reflections for GeO_2 , and the lower line of black crosses represents positions of Bragg reflections for $KAlGeO_4$.

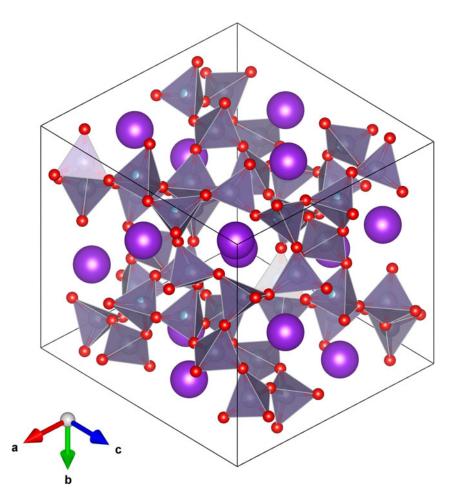


Figure 2. VESTA $I4_1/a$ tetragonal structure plot for KAlGe₂O₆, viewed down [1–11] showing a channel for extraframework purple K⁺ cations. Disordered (Al/Ge)O₄ tetrahedra are shown in light purple, and O²⁻ anions are shown in red.

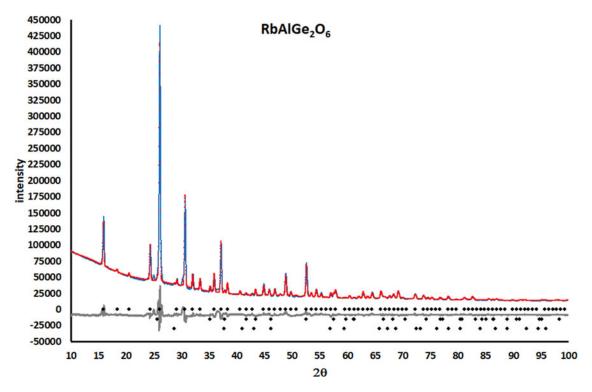


Figure 3. Rietveld difference plot for RbAlGe₂O₆. Red circles represent observed data points, blue line represents calculated data points, and the green line represents difference curves. The upper line of black crosses represents positions of Bragg reflections for RbAlGe₂O₆, the middle line of black crosses represents positions of Bragg reflections for Al_2O_3 , and the lower line of black crosses represents positions of Bragg reflections for Bra

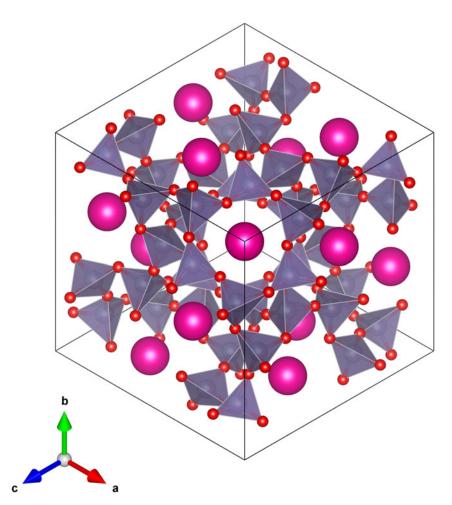


Figure 4. VESTA $I\bar{4}3d$ cubic structure plot for RbAlGe₂O₆, viewed down [111] showing a channel for extraframework pink Rb⁺ cations. Disordered (Al/Ge)O₄ tetrahedra are shown in light purple, and O²⁻ anions are shown in red.

6

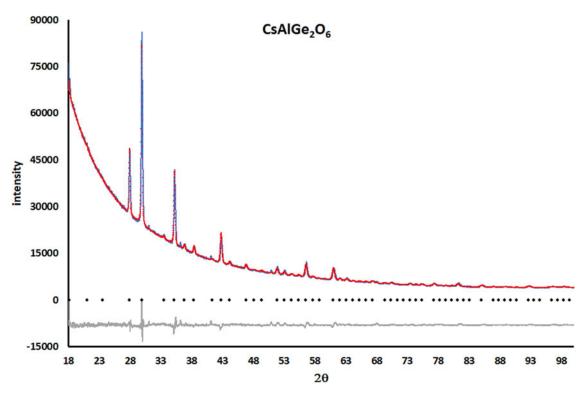


Figure 5. Rietveld difference plot for $CsAlGe_2O_6$. Red circles represent observed data points, blue line represents calculated data points, and the green line represents difference curves. The line of black crosses represents positions of Bragg reflections for $CsAlGe_2O_6$.

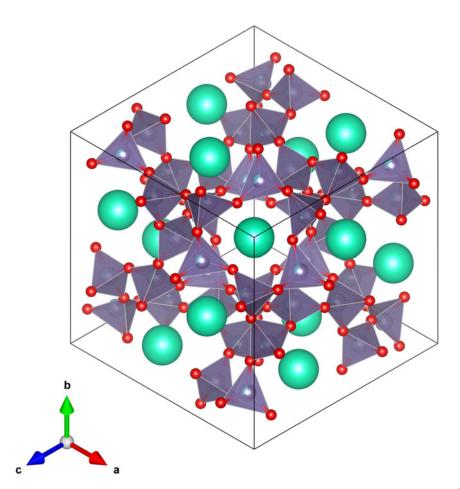


Figure 6. VESTA $I\bar{4}3d$ cubic structure plot for CsAlGe₂O₆, viewed down [111] showing a channel for extraframework light blue Cs⁺ cations. Disordered (Al/ Ge)O₄ tetrahedra are shown in light purple, and O²⁻ anions are shown in red.

IV. CONCLUSIONS

Crystal structures have been refined for $AAlGe_2O_6$ synthetic leucite analogs (A = K, Rb, Cs). All refined structures have disordered T-site cations. KAlGe₂O₆ is isostructural with $I4_1/a$ tetragonal KAlSi₂O₆ leucite. However, CsAlGe₂O₆ has the $I\bar{4}3d$ cubic space group and is isostructural with a previously published structure for CsAlGe₂O₆. RbAlGe₂O₆ also has the $I\bar{4}3d$ cubic space group and is isostructural with CsAlGe₂O₆.

V. DEPOSITED DATA

CIF files with information related to crystal structure, interatomic distances and angles, and powder diffraction data for KAlGe₂O₆, RbAlGe₂O₆, and CsAlGe₂O₆ synthetic leucite analogs were deposited with the ICDD. You may request these data from ICDD at info@icdd.com.

ACKNOWLEDGEMENTS

The author wishes to acknowledge the use of the EPSRC funded National Chemical Database Service hosted by the Royal Society of Chemistry.

REFERENCES

- Beger, R. M. 1969. "The Crystal Structure and Chemical Composition of Pollucite." Zeitschrift für Kristallographie – Crystalline Materials 129: 280–302. doi:10.1524/zkri.1969.129.16.280.
- Bell, A. M. T. 2024. "Crystal Structures of Leucites Past, Present, and Future?" Submitted to Crystallography Reviews.
- Bell, A. M. T., and C. M. B. Henderson. 2020. "Tetragonal-Cubic Phase Transition in KGaSi₂O₆ Synthetic Leucite Analogue and its Probable Mechanism." *Journal of Solid State Chemistry* 284: 121142. doi:10.1016/j.jssc.2019.121142.
- Bell, A. M. T., C. M. B. Henderson, S. A. T. Redfern, R. J. Cernik, P. E. Champness, A. N. Fitch, and S. C. Kohn. 1994a. "Structures of Synthetic K₂MgSi₅O₁₂ Leucites by Integrated X-ray Powder Diffraction, Electron Diffraction and ²⁹Si MAS NMR Methods." Acta Crystallographica B 50: 31–41. doi:10.1107/S0108768193008754.
- Bell, A. M. T., S. A. T. Redfern, C. M. B. Henderson, and S. C. Kohn. 1994b.
 "Structural Relations and Tetrahedral Ordering Pattern of Synthetic Orthorhombic Cs₂CdSi₅O₁₂ Leucite: A Combined Synchrotron X-ray Powder Diffraction and Multinuclear MAS NMR Study." Acta Crystallographica B 50: 560–6. doi:10.1107/S0108768194003393.
- Finger, L. W., and R. M. Hazen. 1978. "Crystal Structure and Compression of Ruby to 46 kbar." *Journal of Applied Physics (Melville, NY, United States)* 49: 5823–6.
- Gates-Rector, S., and T. Blanton. 2019. "The Powder Diffraction File: A Quality Materials Characterization Database." *Powder Diffraction* 34 (4): 352–60. doi:10.1017/S0885715619000812.
- Gatta, G. D., N. Rotiroti, M. Fisch, M. Kadiyski, and T. Armbruster. 2008.
 "Stability at High-Pressure, Elastic Behaviour and Pressure-Induced Structural Evolution of CsAlSi₅O₁₂: A Potential Host for Nuclear Waste." Physics and Chemistry of Minerals 35: 521–33.
- Gatta, G. D., R. Rinaldi, G. J. McIntyre, G. Nénert, and F. Bellatreccia. 2009.
 "On the Crystal Structure and Crystal Chemistry of Pollucite, (Cs, Na)₁₆Al₁₆Si₃₂O₉₆nH₂O: A Natural Microporous Material of Interest in

- Nuclear Technology." *American Mineralogist* 94: 1560–8. doi:10.2138/am.2009.3237.
- Haines, J., O. Cambon, E. Philippot, L. Chapon, and S. Hull. 2002. "A Neutron Diffraction Study of the Thermal Stability of the Alpha-Quartz-Type Structure in Germanium Dioxide." *Journal of Solid State Chemistry* 166: 434–41.
- Hariyani, S., E. Armijo, and J. Brgoch. 2020. "Broad Green Emission in the Leucite-Like Cs₂ZnSi₅O₁₂:Eu²⁺ Phosphor." *ECS Journal of Solid State Science and Technology* 9: 016015. doi:10.1149/2.0222001JSS.
- Klaska, R. 1978. "Ein synthetischer Leucit-typ mit Ordnungstenenz." Naturwissenschaften 65: 592–93.
- Mazzi, F., E. Galli, and G. Gottardi. 1976. "The Crystal Structure of Tetragonal Leucite." American Mineralogist 61: 108–15.
- Millini, R., L. Montanari, and G. Bellussi. 1993. "Synthesis and Characterization of a Potassium Borosilicate with ANA Framework Type Structure." *Microporous Materials* 1: 9–15.
- Momma, K., and F. Izumi. 2011. "VESTA 3 for Three-Dimensional Visualization of Crystal, Volumetric and Morphology Data." *Journal of Applied Crystallography* 44: 1272–6. doi:10.1107/S0021889811038970.
- Palmer, D. C., M. T. Dove, R. M. Ibberson, and B. M. Powell. 1997.
 "Structural Behavior, Crystal Chemistry, and Phase Transitions in Substituted Leucite: High-Resolution Neutron Powder Diffraction Studies." American Mineralogist 82: 16–29.
- PANalytical. 2009. *High Score Plus 2.2e (Computer Software)*. Almelo, The Netherlands, PANalytical.
- PANalytical. 2014. *Data Collector 5.1a (Computer Software)*. Almelo, The Netherlands, PANalytical.
- PANalytical. 2017. Data Collector 5.5a (Computer Software). Almelo, The Netherlands, PANalytical.
- Richerson, D. W., and F. A. Hummel. 1972. "Synthesis and Thermal Expansion of Polycrystalline Cesium Minerals." Journal of the American Ceramic Society 55 (5): 269–73.
- Rietveld, H. M. 1969. "A Profile Refinement Method for Nuclear and Magnetic Structures." *Journal of Applied Crystallography* 2: 65–71. doi:10.1107/S0021889869006558.
- Robinson, K., G. V. Gibbs, and P. H. Ribbe. 1971. "Quadratic Elongation: A Quantitative Measure of Distortion in Coordination Polyhedra." *Science* 172: 567–70.
- Shannon, R. D. 1976. "Revised Effective Ionic Radii and Systematic Studies of Interatomic Distances in Halides and Chalcogenides." Acta Crystallographica Section A 32 (5): 751–67. doi:10.1107/ S0567739476001551.
- Sun, W., H. Li, B. Zheng, R. Pang, L. Jiang, S. Zhang, and C. Li. 2019. "Electronic Structure and Photoluminescence Properties of a Novel Single-Phased Color Tunable Phosphor KAlGeO₄:Bi³⁺,Eu³⁺ for WLEDs." Journal of Alloys and Compounds 774: 477–86.
- Taylor, D., and C. M. B. Henderson. 1968. "The Thermal Expansion of the Leucite Group of Minerals." American Mineralogist 53 (9-10): 1476–89.
- Toby, B. H., and R. B. Von Dreele. 2013. "GSAS-II: The Genesis of a Modern Open-Source All Purpose Crystallography Software Package." *Journal of Applied Crystallography* 46 (2): 544–9. doi:10.1107/ S0021889813003531.
- Torres-Martinez, L. M., and A. R. West. 1989. "Pollucite- and Leucite-Related Phases: A₂BX₅O₁₂ and ACX₂O₆ (A = K, Rb, Cs; B = Be, Mg, Fe, Co, Ni, Cu, Zn, Cd; C = B, Al, Ga, Fe, Cr; X = Si, Ge)." *Zeitschrift für Anorganische und Allgemaine Chemie* 578: 223–30.
- Torres-Martinez, L. M., J. A. Gard, and A. R. West. 1984. "Synthesis and Structure of a New Family of Phases, A₂MGe₅O₁₂: A = Rb, Cs; M = Be, Mg, Co, Zn." *Journal of Solid State Chemistry* 53: 354–9.
- Tripathi, A., and J. B. Parise. 2002. "Hydrothermal Synthesis and Structural Characterization of the Aluminogermanate Analogues of JBW, Montesommaite, Analcime and Paracelsian." Microporous and Mesoporous Materials 52: 65–78.

8