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Effects of Hydroelasticity on Elastic and Rigid Behaviour of Floating Systems



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Abstract

Hydroelasticity of marine structures with and without forward speed is studied directly using time dependent Boundary Integral Equation Method with Neumann-Kelvin linearisation where the potential is considered as the impulsive velocity potential. The exciting and radiation hydrodynamic parameters are predicted in time with transient wave green function whilst the structural analysis is solved with Euler-Bernoulli beam method at which modeshapes are defined analytically. The modal analysis is used to approximate the hydroelastic behaviour of the floating systems through fully coupling of the structural and hydrodynamic analyses. As it is expected, it is found with numerical experience that the effects of the rigid body modes are greater than elastic modes in the case of stiff structures. The predicted numerical results of the present in-house computational tool ITU-WAVE are compared with experimental results for validation purposes and show the acceptable agreements.

Keywords: Hydroelasticity; Boundary integral equation method; Transient wave green function; Time domain; Neumann-Kelvin linearisation; Euler-Bernoulli beam.

Introduction

The fluid-structure interactions of the floating system result in rigid or elastic motions which depend on the disturbance of pressure field around marine structures. If the effects of the rigid body modes are greater than elastic modes, the contribution of elastic modes to the disturbance of the pressure field is not important which implicitly means that the floating system is a stiff structure, and the structural and hydrodynamic analyses are weakly coupled, and two analyses can be done separately [1-3]. If the radiation field is affected significantly with the structural deformation, the hydroelastic analysis, which considers the fully coupling of the structural and hydrodynamic analysis, needs to be taken into account for the prediction of the motion of the floating systems [4,5]. Hydroelasticity plays significant role especially for the high-speed crafts and larger marine vehicles. In the case of larger floating systems, the incident wave frequencies and natural frequency are closer to each other whilst the frequency range that results in the hull-girder vibrations approaches the encounter frequency of the high-speed crafts.

The elastic deflection of the structures in air can be predicted accurately with mode shapes, however, in the case of floating systems, due to the effects of the radiation pressure field the mode

shapes need to be determined at current time and the elastic deformation of the floating structures may be predicted with the mode shape superpositions. The dry mode shapes in air can be used to predict the elastic deformation of the floating systems [1], alternatively, elastic deflection in fluid may be represented with orthogonal polynomials [4] or orthogonal beam of a uniform beam [6]. The rigid body modes are considered as the part of the elastic modes under the same boundary conditions in the hydroelastic analysis. It is expected that the effects of higher modes on elastic motions would not be significant as the interactions between the natural frequencies of the higher modes and incident wave frequencies would be weaker compared to those of lower modes.

The frequency domain [1] or time domain [2,3,5] methods may be used to predict the hydroelastic behaviour and analysis of the floating systems. Two-dimensional strip theory methods [7,8] are one of the options that may be used for the approximations of the hydrodynamic and hydroelastic parameters. However, the strip theory method has shortcomings at bow and stern regions of floating systems, global loads approximations, complex geometries, high forward speed, and low frequency ranges. These shortcomings of the strip theory methods could be overcome

with the use of three-dimensional methods both in frequency and time domains which include the interactions amongst panels automatically.

The hydrodynamic parameters can be predicted with two popular numerical methods both in frequency and time domains including wave green function [2,9,10] and Rankine panel methods [11,12]. The wave green function methods satisfy the condition at infinity and free surface boundary condition automatically which results in only discretisation of the body surface under mean water level to satisfy the body boundary condition. In the case of Rankine panel method, both some part of the free surface and body surface under mean position need to be discretised to satisfy the condition at infinity and body boundary condition respectively. in the context of linear analysis, the frequency and time domain results depend on each other via Fourier transform. The time domain methods are better suited to predict the nonlinear cable forces, unsteady manoeuvring, motions with large amplitudes, and nonconstant forward speed compared to frequency domain methods.

The finite element method with three-dimensional shell elements [12], two-dimensional plate elements using Kirchoff or Mindlin plates [2,3] or one-dimensional beam elements using Vlasov, Timoshenko and Euler-Bernoulli beams [1,5,13] are used to predict the hydroelastic behaviour of the floating systems including eigenvectors and eigenvalues. The body boundary conditions for elastic floating bodies, which include rigid body boundary conditions, are obtained [1,4,5] through the extension of unified theory [1,4].

The fluid forces and velocities are predicted with potential three-dimensional formulation and transient wave green function whilst the structural parameters are obtained with one-dimensional Euler-Bernoulli beam approximation in the present paper. The free stream is selected as a basis flow which results in the linearisation of the initial boundary value problem. The time dependent boundary integral equation is obtained using the three-dimensional transient wave green function and green theorem [2,3,5,15-29]. The present in-house ITU-WAVE computational numerical results are validated against the experimental results [30,31] which shows acceptable agreements.

Equation of Motion of Elastic Floating Systems

The body-fixed Cartesian coordinate system $\vec{x}=(x,y,z)$ in (Figure 1) is used to represent the fluid behaviour around the elastic floating systems. The positive directions of x, y and z directions are defined with the positive direction of a right-hand coordinate system. The free surface is coincident with z=0 plane. The elastic floating body moves forward in positive x direction

with forward speed U_0 , the fluid domain in Figure 1 is identified with boundary at infinity S_∞ , boundary on free surface $S_f(t)$ boundary of body surface $S_b(t)$ and interaction between free surface and body $\Gamma(t)$ [2, 15].

It is assumed that the fluid is inviscid, incompressible and the flow of the fluid is irrotational. These assumptions result in the fluid velocities to be represented as the gradient of the velocity

potential $\vec{v}(\vec{x},t)=\nabla\Phi(\vec{x},t)$ and Laplace equation governs the fluid

domain $\nabla^2\Phi(\vec{x},t)=0$. The time dependent equation of motions includes the inertia term, elastic hydrostatic and hydrodynamic restoring coefficients which is represented with convolution integral and excitation force due to incident wave which is also represented with convolution integral [32].

$$\sum_{k=1}^K (M_{jk} + a_{jk}) \ddot{x}_k(t) + b_{jk} \dot{x}_k(t) + (k_{jk} + c_{jk} + \int_0^t d\tau K_{jk}(t-\tau)) x_k(t) = \int_{-\infty}^{\infty} d\tau K_{jD}(t-\tau) \zeta(\tau) \quad (1)$$

where $j=1,2, 3\dots, K$ and the coefficients in Eq. (1) are given as

$$M_{jk} = \int_{-L/2}^{L/2} m \omega_j(x) \omega_k(x) dx \quad (2)$$

$$k_{jk} = \int_{L/2}^{L/2} EI \omega_j''(x) \omega_k''(x) dx \quad (3)$$

$$C_{jk} = \rho g \iint_{S_o} ds_Q \left(\omega_j + z \nabla \cdot \vec{u}_j \right) n_k \quad (4)$$

The displacement, velocity and acceleration of elastic floating system are given in Eq. (1) with $x_k(t)$, $\dot{x}_k(t)$ and $\ddot{x}_k(t)$ respectively.

The structural mass matrix Eq. (2) where ω_j is the part of the

mode shapes $\vec{u}_j=(0,0,\omega_j)$ structural stiffness matrix Eq. (3), and hydrostatic restoring force coefficients Eq. (4) are represented

with M_{jk} , k_{jk} , and C_{jk} respectively. The nondimensional stiffness

parameter $S = EI / \rho g L^3$, which is the function of the hydrostatic restoring force and structural stiffness, is developed assuming the mass m per unit length and structural stiffness EI are uniformly distributed along longitudinal direction [33]. The nondimensional

parameter $S = 0$ is used for fully elastic structure whilst $S = \infty$ is for fully rigid structures. The generalised modes with separation

of variables are used to represent the total displacements of the elastic floating structures.

$$\vec{u}(x, y, z, t) = \sum_{k=1}^k \vec{u}_k(x, y, z) x_k(t) \quad (5)$$

where time dependent principal coordinates $x_k(t)$ and mode shapes depending on spatial variables (x, y, z) are given with

$x_k(t)$ and $\vec{u}_k(x, y, z)$ respectively. The elastic modeshapes $\vec{u}_k(x, y, z)$ include the rigid body modes such that $\vec{u}_3(0, 0, 1)$

is used for heave mode whilst $\vec{u}_5(0, 1, 0) \times \vec{x}$ is used for pitch mode.

$$a_{jk} = \rho \iint_{s_o} dS_Q \psi_{1k} n_j \quad (6)$$

$$b_{jk} = \rho \iint_{s_o} dS_Q (\psi_{1k} m_j - \psi_{2k} n_j) \quad (7)$$

$$c_{jk} = -\rho \iint_{s_o} dS_Q \psi_{2k} m_j \quad (8)$$

$$K_{jk}(t) = \rho \iint_{s_o} dS_Q \left\{ \frac{\partial}{\partial t} x_k(t) n_j - x_k(t) m_j \right\} \quad (9)$$

The convolution integral at the left-hand side of Eq. (1) is the function of the radiation Impulse Response Functions (IRFs)

$K_{jk}(t)$ and the velocity $\dot{x}_k(t)$ of the elastic floating systems. This convolution integral represents the wave damping or hydrodynamic restoring force coefficients. The time dependent

IRFs $K_{jk}(t)$ represent the memory or free surface effect. The frequency and time independent infinite added mass, damping

and restoring force related coefficients are given with a_{jk} , b_{jk}

, and c_{jk} respectively. The time independent instantaneous fluid response and the steady displacement of the elastic structure due

to forward speed effect are given with $\psi_{1k}(P)$ and $\psi_{2k}(P)$ respectively. The transient behaviour of elastic floating system due to free surface effect is considered with the time dependent

potential $x_k(t)$ [34].

$$F_{jD}(t) = \int_{-\infty}^{\infty} d\tau K_{jD}(t-\tau) \zeta(\tau) = \int_{-\infty}^{\infty} d\tau \{K_{js}(t-\tau) + K_{jl}(t-\tau)\} \zeta(\tau) \quad (10)$$

$$K_{jI}(t) = \iint_{s_o} dS_Q \hat{p}(t) n_j \quad (11)$$

$$K_{js}(t) = \rho \iint_{s_o} dS_Q \left\{ -\frac{\partial}{\partial t} \hat{\phi}_s(t) n_j + \hat{\phi}_s(t) m_j \right\} \quad (12)$$

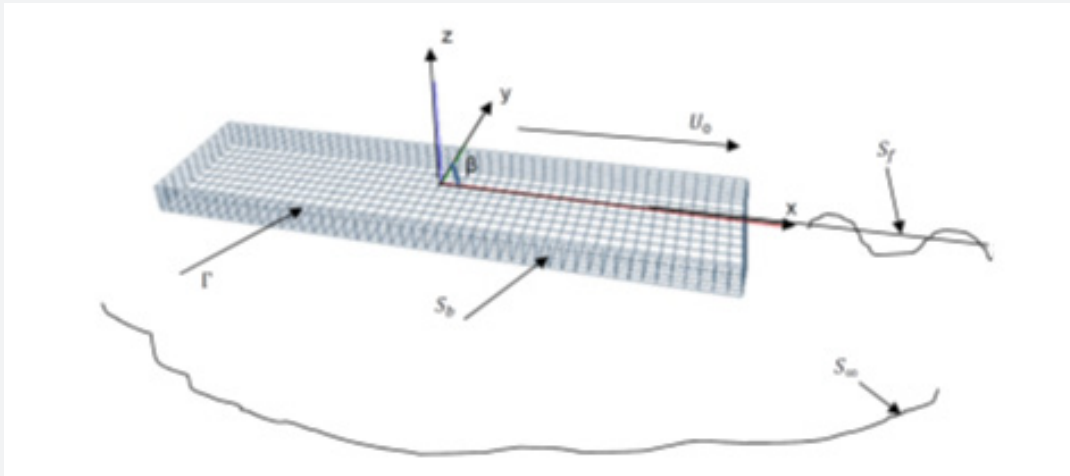


Figure 1: Fluid boundaries and Coordinate system.

The convolution integral in the right-hand side of Eq. (1) is the function of the exciting IRFs $K_{jD}(t)$ and incident wave elevation $\zeta(t)$ which is impulsive and defined at the centre of the fixed coordinate system with heading angle β in (Figure 1). The exciting IRFs $K_{jD}(t)$ have two components; one of them is due to incident waves $K_{jI}(t)$ in Eq. (11) whilst the second one is due to the effects of the scattering waves $K_{jS}(t)$ in Eq. (12) respectively. The time dependent impulsive pressure is given with

$\hat{p}(t)$ whilst the scattering wave potential which results from the interactions of the incident waves with floating systems is given with $\hat{\phi}_s(t)$ [10].

Deflection of Elastic Floating Bodies

The bending moments and shear forces of elastic floating systems with three-dimensional finite element methods [2, 3, 35] can be predicted with the free vibration of the marine structures defining the deformations with mode shapes. Free-free beam [6], Chebyshev and Legendre polynomials or Fourier series [4] could be also used to determine the deformation of the elastic marine structures. Euler-Bernoulli beam theory with free-free beam modes and nondimensional coordinates $q = 2x / L$, which

satisfy the boundary conditions of zero shear forces and bending moments at the end points, is used in the present paper [6].

$$(13)$$

$$u_{2j}(q) = \frac{1}{2} \left(\frac{\cos(k_{2j}q)}{\cos(k_{2j})} + \frac{\cosh(k_{2j}q)}{\cosh(k_{2j})} \right)$$

$$u_{2j+1}(q) = \frac{1}{2} \left(\frac{\sin(k_{2j+1}q)}{\sin(k_{2j+1})} + \frac{\sinh(k_{2j+1}q)}{\sinh(k_{2j+1})} \right) \tag{14}$$

where nondimensional normalized coordinate $q \in [-1,1]$ and mode index $j = 1,2,3,\dots$. As the rigid body modes are the part of the elastic modes, the first elastic mode is the heave rigid body

mode $u_0(q) = 1$ whilst the second elastic mode is the pitch rigid

body mode $u_1(q) = -qL/2$. The $\vec{u}_2 = (0,0,u_k(q))$ vector represents the mode shapes in Eq. (13) and Eq. (14) in which the

k_j parameters are determined with Eq. (15).

$$(-1)^j k_j \tan k_j + \tan k_j = 0 \tag{15}$$

The free-free beam modeshapes of the elastic modes, which include the rigid modes of heave and pitch, are presented in (Figure 2).

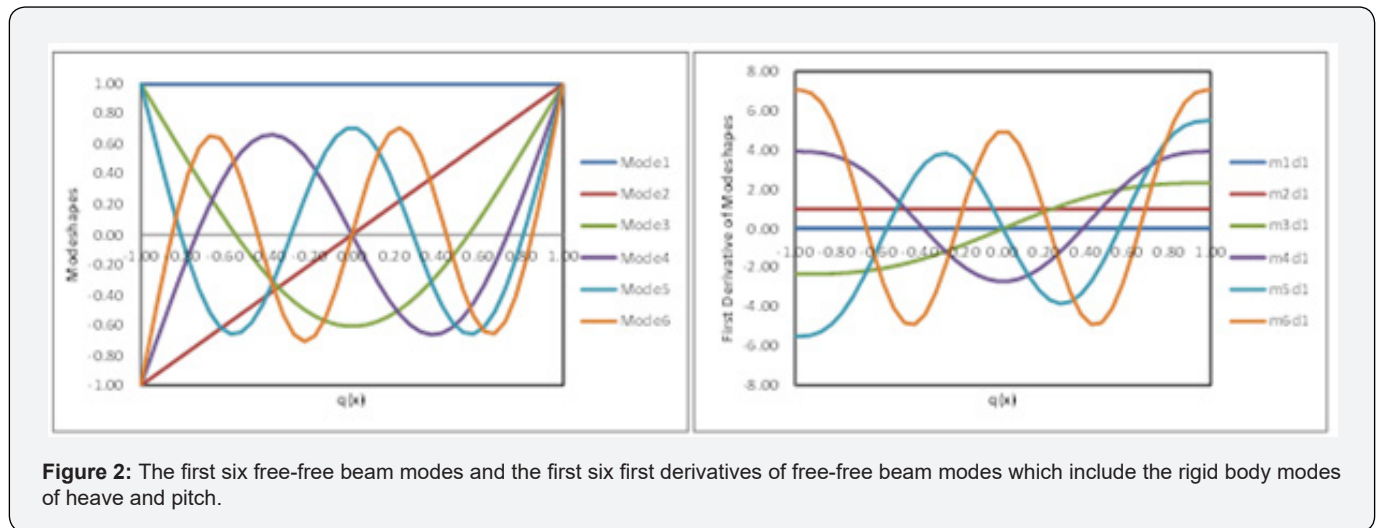


Figure 2: The first six free-free beam modes and the first six first derivatives of free-free beam modes which include the rigid body modes of heave and pitch.

An Elastic Slender Barge for Hydroelastic Analysis

An elastic slender barge in head seas floating freely is used to predict the deformable modes which include heave and pitch rigid body modes. The elastic barge has zero speed with draft to

beam ratio $T/B=0.5$ and length to beam ratio $L/B=10$. Total 516 panels are used to discretise the elastic barge including 3 panel in vertical direction, 6 panels in transverse direction and 40 panels in longitudinal direction as presented in (Figure 3).

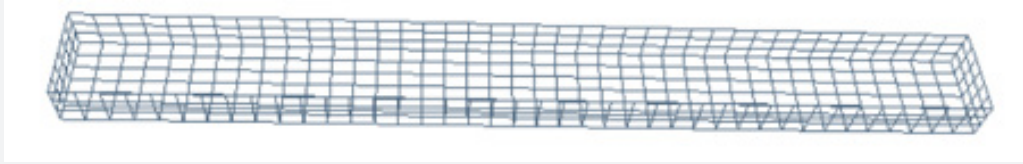


Figure 3: Total 516 panels are used with 3 panel in vertical direction, 6 panels in transverse direction and 40 panels in longitudinal direction.

It is assumed that the structural stiffness and mass are distributed uniformly in longitudinal direction of the elastic floating systems such that mass matrix with constant mass distribution [4] is given as

$$M_{jk} = \int_{-L/2}^{L/2} m \omega_j(2x/L) \omega_k(2x/L) dx = \frac{M}{4} \delta_{jk} \quad (16)$$

where the Kroenecker delta function and elastic beam's total mass are given with δ_{jk} and $M=mL$ respectively. The structural stiffness k_{jk} with constant EI is given as

$$k_{jk} = \int_{-L/2}^{L/2} EI \omega_j''(2x/L) \omega_k''(2x/L) dx = 4 \frac{EI}{L^3} k_j^4 \delta_{jk} \quad (17)$$

where the modulus of elasticity and second moment of inertial are given with E and I respectively. The off-diagonal elements of the stiffness and mass matrices are zero as these matrices are symmetric.

The deformable nondimensional radiation IRFs of elastic barge including 7,8, 9, ... 14 elastic modes are presented in (Figure 4) in which the area under each elastic mode represents the available energy for each mode. It may be noticed in (Figure 4) that available energy decreases with increasing elastic mode numbers which implies that the effects of the higher elastic modes to the total displacements are not significant.

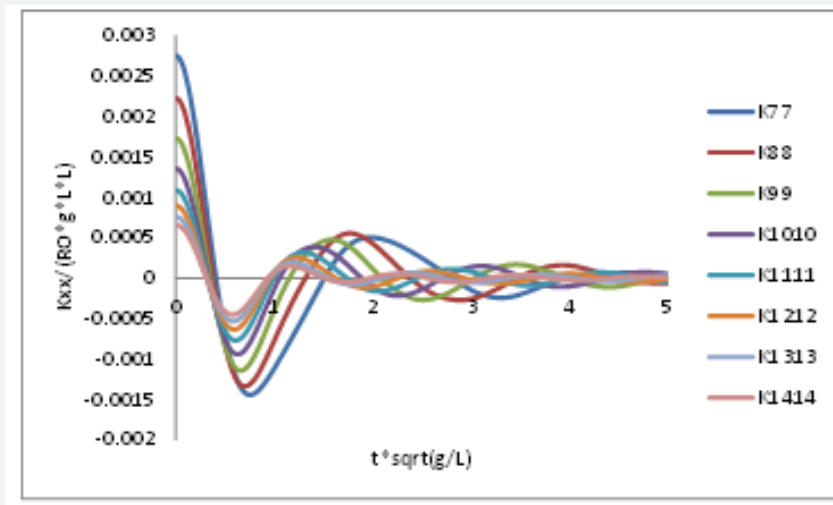


Figure 4: The first 8 deformable modes of nondimensional radiation IRFs of the elastic barge.

The time domain radiation IRFs $k_{jk}(t)$ and frequency domain added mass $A_{jk}(\omega)$ and damping coefficients $B_{jk}(\omega)$ in the context of linear analysis depend on each other through Fourier transform for each elastic mode as presented in Eq. (18) and (19).

$$A_{jk}(\omega) = a_{jk} - \frac{1}{\omega} \int_0^t d\tau K_{jk}(\tau) \sin(\omega\tau) - \frac{c_{jk}}{\omega^2} \quad (18)$$

$$B_{jk}(\omega) = b_{jk} + \int_0^t d\tau K_{jk}(\tau) \cos(\omega\tau) \quad (19)$$

Fourier transform of radiation IRFs $k_{jk}(t)$ in (Figure 4) is

used to obtain the frequency dependent added mass $A_{jk}(\omega)$ and damping coefficients $B_{jk}(\omega)$ in (Figure 5). As in the case of

IRFs in (Figure 4), the same behaviour may be observed in (Figure 5) as the amplitude of the added-mass and damping coefficients are decreasing with the increasing mode numbers.

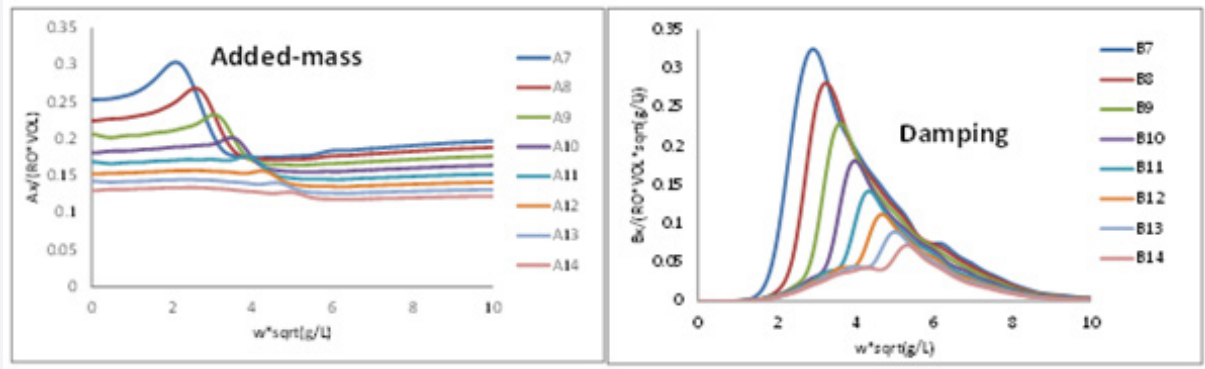


Figure 5: The first 8 deformable modes of nondimensional added-mass and damping coefficients.

The regular or irregular incident wave $\zeta(t)$, which is defined at the centre of body-fixed coordinate system in (Figure 1), is used to excite the elastic floating systems whilst the time

dependent incident wave potential $\phi_I(\vec{x}, t)$ is known and analytically defined in Eq. 20.

$$\phi_I(\vec{x}, t) = \frac{ig}{\omega} e^{k(z-i\omega t)} e^{i\omega t} \quad (20)$$

where the absolute frequency of the incident waves, encounter frequency, wave number in infinite water depth, incident wave heading angle and positions on the free surface with respect

to heading angle are given with $\omega, \omega_e = \omega - U_0 k \cos(\beta)$, $k = \omega^2 / g$, β and $\varpi = x \cos(\beta) + y \sin(\beta)$ respectively.

Froude-Krylov IRFs, diffraction IRFs and exciting IRFs which are obtained by the superposition of Froude-Krylov and diffraction IRFs are presented in (Figure 6) for the first three deformable modes including 7, 8 and 9 modes. The area under these IRFs represent the available energy that would be absorbed by the elastic floating systems during the interactions of incident waves and elastic marine structures.

As in the case of radiation analysis, the time dependent Froude-Krylov, diffraction and exciting IRFs are linked to frequency dependent Froude-Krylov, diffraction and exciting force amplitude and phase angles through Fourier transform as presented in Eq. (21).

$$x_j(\omega_e) = \int_{-\infty}^{\infty} d\tau [K_{jk}(\tau) + K_{js}(\tau)] e^{-i\omega\tau} \quad (21)$$

where the frequency dependent exciting force parameters

in complex form are given with $x_j(\omega_e)$ in which the exciting force amplitudes including Froude-Krylov and diffraction are the

absolute value of complex exciting force $x_j(\omega_e)$ whilst those

of phase angles is the arguments of $x_j(\omega_e)$. The frequency dependent exciting force amplitudes and phase angles in (Figure 7) are obtained via Fourier transform of time dependent IRFs in (Figure 6).

Response Amplitude Operators (RAOs) or deflections of an elastic floating systems in frequency domain may be written as in Eq. (22).

$$x_k(q) = \sum_{k=1}^k x_k(\omega) u_k(q) \quad (22)$$

where normalised coordinate in nondimensional form is

given with $q = 2x/L$. The $x_k(q)$, which is the function of the absolute wave frequency ω and normalised coordinates q , is the complex form of the elastic RAOs in which the absolute value is the amplitude of the response whilst the argument is the phase

angle of the response. The nondimensional stiffness parameter S for fully rigid, hydroelastic effect significant, and fully flexible elastic slender barge are given with $S=1$, $S=10^{-5}$, and $S=0$ for the first eight deformable elastic modes in (Figure 8).

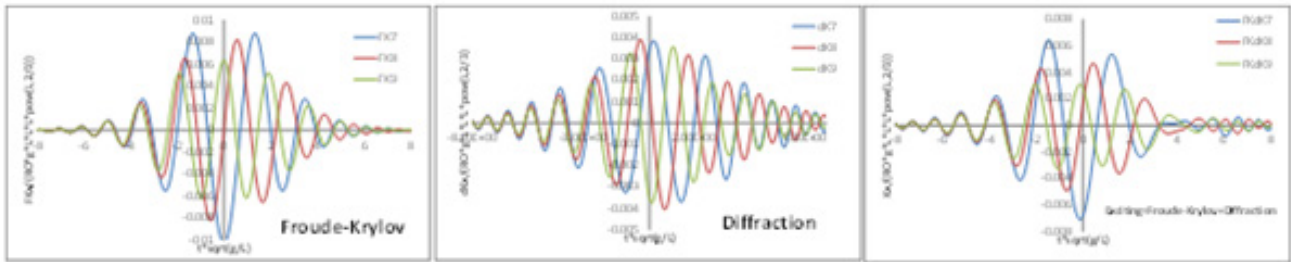


Figure 6: Nondimensional Froude-Krylov, diffraction, and exciting IRFs for the first three deformable modes of 7, 8 and 9.

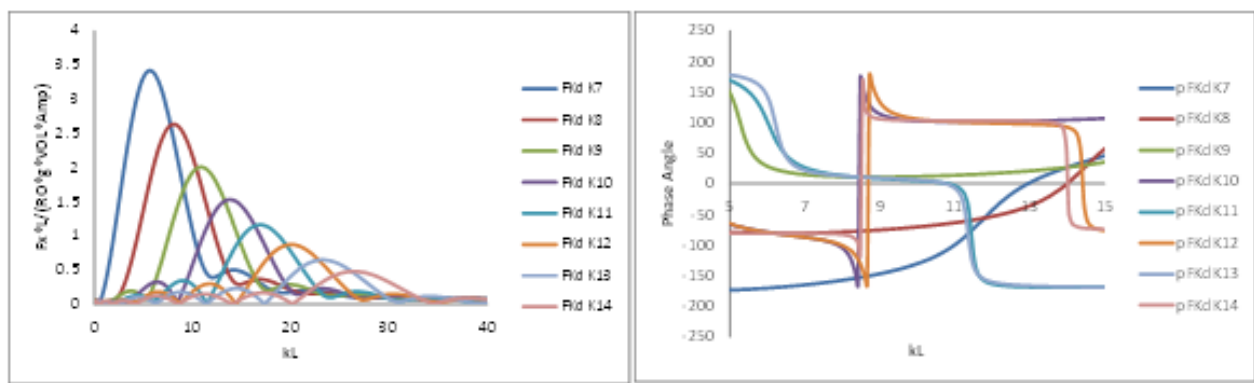


Figure 7: Nondimensional exciting force amplitudes and phase angles of elastic slender barge for the first 8 deformable modes including 7, 8 and 9 modes.

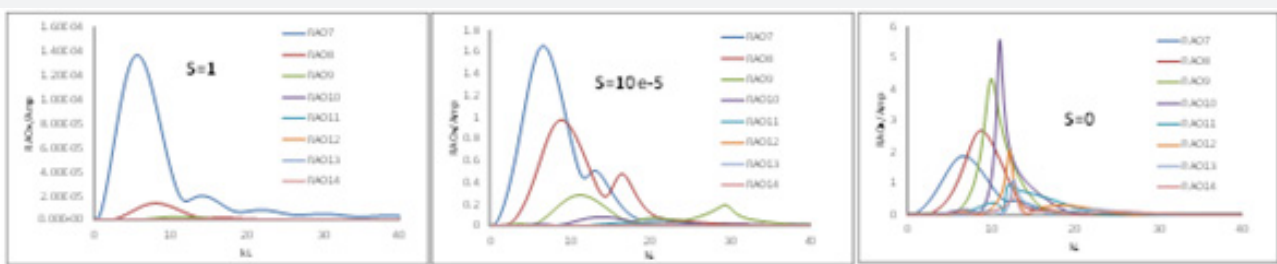


Figure 8: Nondimensional RAOs of elastic slender barge with stiffness factor $S=1$, $S=10e-5$, $S=0$ for the first 8 deformable modes.

The effects of the deformable modes to the response of elastic slender barge in the case of fully rigid condition $S=1$ is not significant and almost zero whilst in the case of fully elastic

condition $S=0$, the effects of elastic deformable modes to RAOs are considerable and significant.

The RAOs, which are predicted using Eq. (22), at stern (-L/2), midship (0xL) and bow (L/2), are presented for different stiffness factor S. It may be noticed from (Figure 9) that there are no differences with the results of $S=10^{-5}$ and rigid body motion whilst there are also no differences with those of stiffness parameter $S=10^{-5}$ and $S=0$. It can be withdrawn from (Figure 9) results that the range of $10^{-8} < S < 10^{-2}$ has the significant hydroelastic effects.

It is known that the maximum response occurs when the elastic floating body length equals the incident wavelength ($\omega = 0.785$ rad/s). The RAOs and the superposition of RAOs are presented in Table 1 using eight deformable elastic modes in the case of nondimensional stiffness factor $S = 10^{-4}$ at the location of L/4 and L/2 (bow). The convergence up to three decimals are achieved with four elastic deformable modes as can be observed from Table 1.

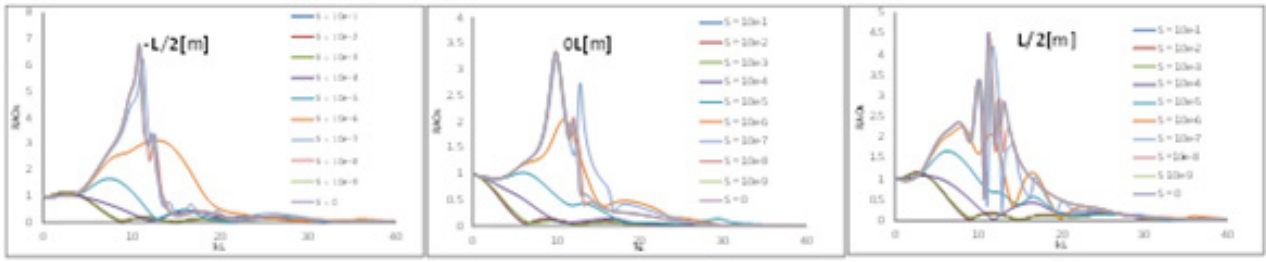


Figure 9: Sum of nondimensional RAOs Eq. (22) for elastic slender barge with a range of nondimensional stiffness factor $S=EI/\rho g L^5$.

The derivative of the shear force is used to obtain the load distribution Eq. (23) [5]

$$L(q) = \frac{dV}{dq} = \sum_{j=1}^k F_j \cdot u_j(q) \quad (23)$$

where F_j is the unknown force coefficients. The first and the second integrations of Eq. (23) are used to determine the shear force and bending moment respectively. The equation of motion in Eq. (1) is used to determine the unknown force coefficient F_j in time domain with Eq. (24).

$$F_j(t) = k_{jk} \ddot{x}_k(t) = \int_{-\infty}^{\infty} d\tau K_{jD}(t-\tau) \zeta(\tau) - \sum_{j=1}^k \left\{ (M_{jk} + a_{jk}) \ddot{x}_k(t) + b_{jk} \dot{x}_k(t) + (C_{jk} + c_{jk}) x_k(t) + \int_0^t d\tau K_{jk}(t-\tau) \dot{x}(\tau) \right\} \quad (24)$$

and in the frequency domain with Eq. (25)

$$F_j(\omega) = k_{jk} \zeta_k(\omega) = X_j(\omega) - \sum_{j=1}^k \left\{ -\omega^2 (M_{jk} + A_{jk}(\omega)) + i\omega B_{jk}(\omega) + C_{jk} \right\} \zeta_k(\omega) \quad (25)$$

(Figure 10) shows the shear forces as a function nondimensional wave number at symmetric locations in longitudinal direction of the elastic slender barge.

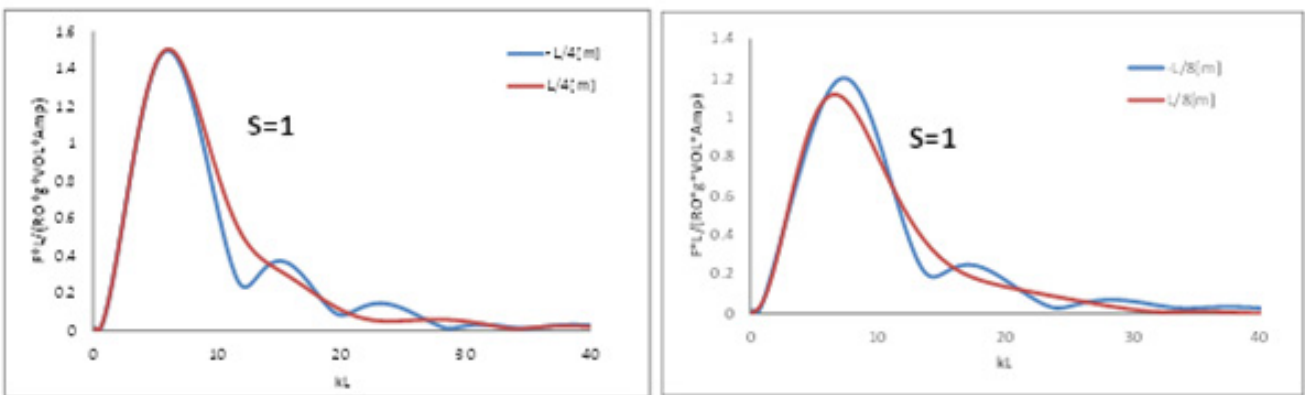


Figure 10: Nondimensional shear force of elastic slender barge Eq. (23) with stiffness factor $S=1$ (completely rigid) and (-) is for aft of mid-ship, (+) for front of mid-ship.

The shear force and bending moment are numerically tested to determine the effects of the hydroelasticity in (Figure 11) and (Figure 12) at which nondimensional shear force and bending moment are presented at the location of $q=-L/4$, $q=0$, and $q=L/4$ in arrange of stiffness factor S .

It can be observed from (Figure 11) that the bending moment and shear force decays to zero when the nondimensional stiffness factor approach the fully flexible condition of $S=0$. The effects of the hydroelasticity for elastic slender barge play significant role at $10^{-8} < S < 10^{-2}$.

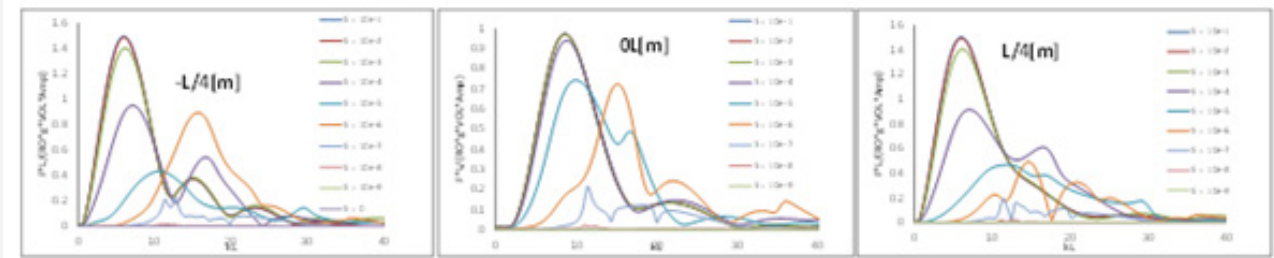


Figure 11: Nondimensional shear forces of elastic slender barge Eq. (23) with a range of non-dimensional stiffness factor $S=EI/\rho g L^4$.

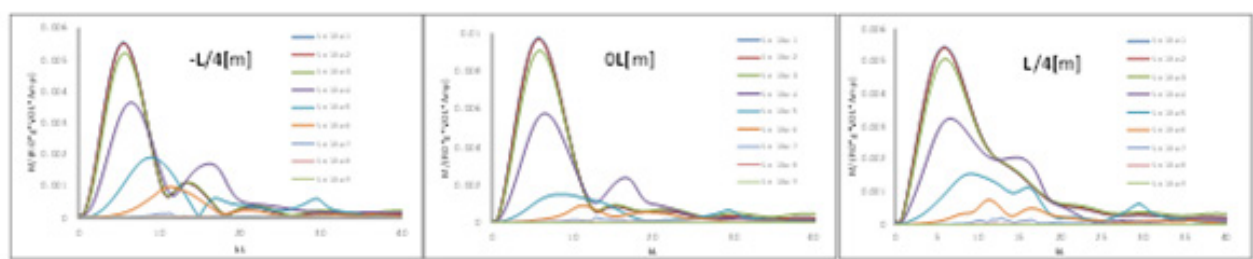


Figure 12: Nondimensional bending moments of elastic slender barge Eq. (23) in a range of nondimensional stiffness factor $S=EI/\rho g L^4$.

Validation of ITU-WAVE numerical results with experimental results of a flexible barge

The experimental results [23] for vertical RAOs (deflection) at head seas and zero forward speed are used to validate the in-house ITU-WAVE computational numerical results of the elastic barge in (Figure 1). The length L , length to draught ratio L/T , and length to beam ratio L/B , vertical bending stiffness EI of the elastic flexible barge are given with 2.445m, 20.375, 4.075, and 175 Nm^2 respectively. The given length dimension and vertical bending stiffness results in the prediction of nondimensional stiffness

factor $S = \frac{EI}{\rho g L^4} = 1.99 \times 10^{-4}$ implying that hydroelastic effect is expected to be significant. Total 1080 elements are used to discretise the flexible barge with 5 elements in vertical direction, 10 elements in transverse direction, 49 elements in longitudinal direction whilst $\tau\sqrt{g/L} = 0.05$ is used for nondimensional time step size for ITU-WAVE numerical prediction. It can be seen from (Figure 13) that ITU-WAVE numerical results show acceptable level of agreement with

the experimental results [23] for vertical deflection (RAOs).

Validation of ITU-WAVE numerical tool with experimental results of a stiff Wigley hull form

ITU-WAVE numerical results of heave and pitch RAOs and bending moment and shear force are validated with experimental results [22] of Wigley hull form in (Figure 14) with $F_n=0.2$, heading angle $\beta = 180^\circ$, length $L=2.5m$, length to draught ratio $L/T=18$, length to beam ratio $L/B=7$.

The convergence test results are presented in (Figure 15) for heave and pitch IRFs. The convergence test is done both with respect to nondimensional time step ($\tau\sqrt{g/L} = 0.01, 0.03, 0.05$) and panel numbers (64, 144, 225, 324, 441). The nondimensional time step $\tau\sqrt{g/L} = 0.05$ and panel number 324 on half part of Wigley hull form due to symmetry are used for the numerical predictions of ITU-WAVE numerical results as the numerical results are converged at these nondimensional time step and panel number.

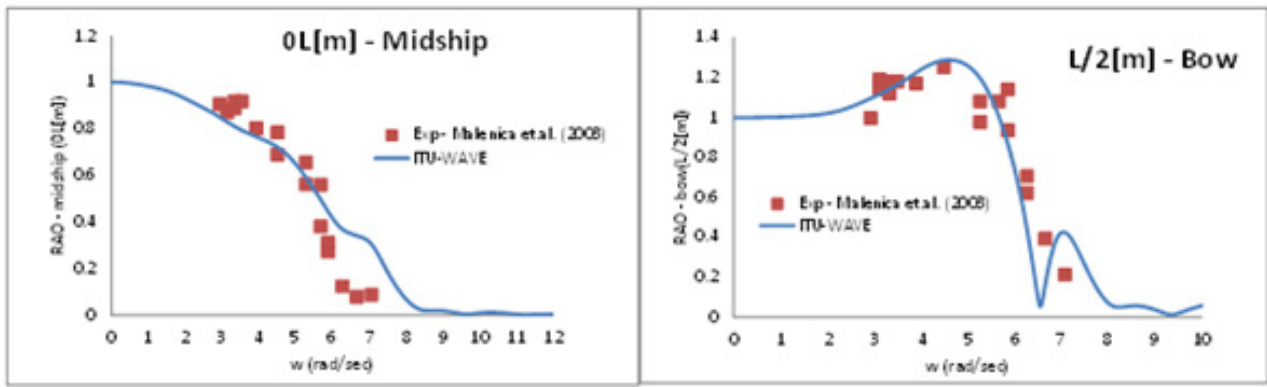


Figure 13: Vertical RAOs of flexible barge at mid-ship (0) and bow (L/2) with heading angle $\beta=180^\circ$, $F_n=0.0$ and stiffness factor $S=EI/pgL^5=1.99 \times 10^{-4}$.

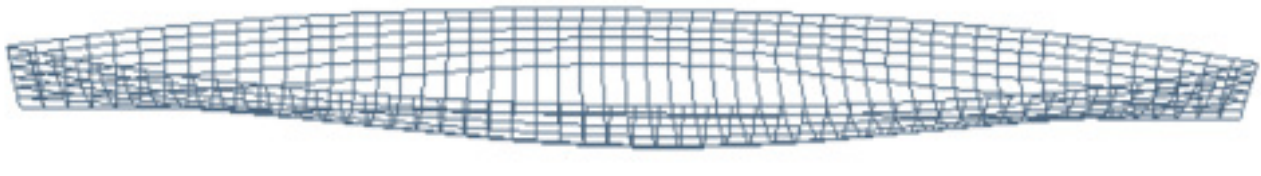


Figure 14: Total 648 panels is used to discretise Wigley form with 12 panels along the girth direction and 54 panels in longitudinal direction.

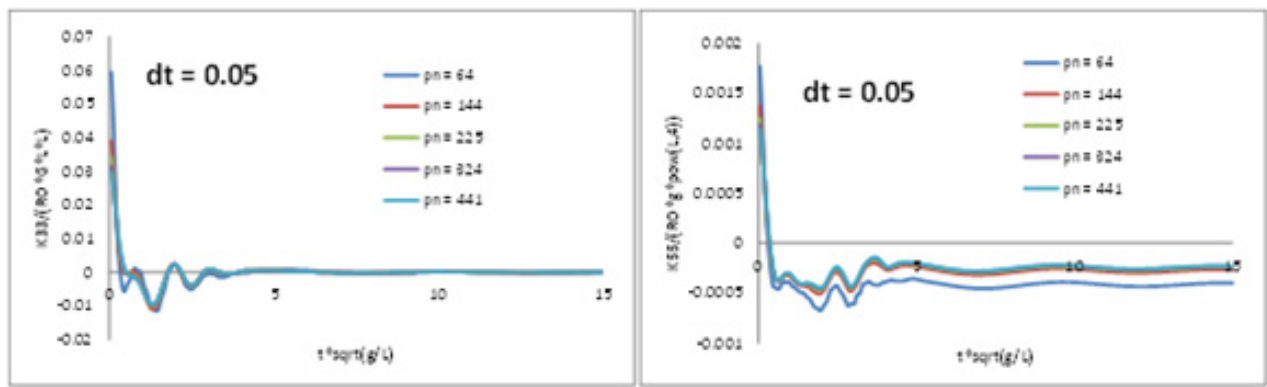


Figure 15: Nondimensional radiation heave and pitch IRFs of Wigley hull form at $F_n = 0.2$.

The convergence test is presented in (Figure 16) for exciting heave and pitch IRFs and the numerical results of ITU-WAVE are converged with nondimensional time step $t\sqrt{g/L}=0.05$ and panel number 324 on half part of Wigley hull form due to symmetry as in radiation convergence test.

The heave and pitch RAOs of ITU-WAVE numerical results at heading angle $\beta=180^\circ$ are presented in (Figure 17) together with experimental results [22] for comparison purpose which show satisfactory agreement. The numerical solution of the RAOs in (Figure 17) are obtained using the frequency domain coupled

heave-pitch equation of motion [36]. The frequency domain radiation and exciting parameters for frequency domain equation

motion are obtained with Fourier transform of IRFs of (Figure 15) and (Figure 16) for radiation and exciting IRFs respectively.

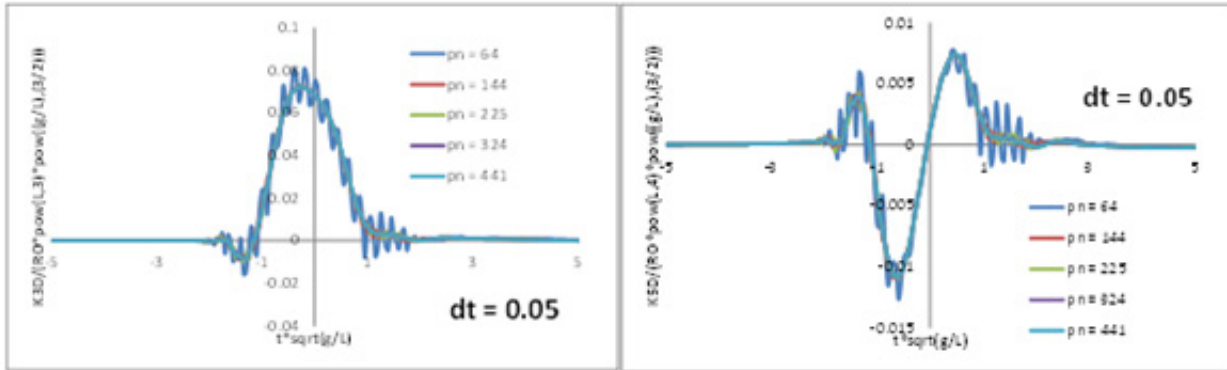


Figure 16: Nondimensional exciting heave and pitch IRFs of Wigley hull form at $F_n = 0.2$ and $\beta=180^\circ$.

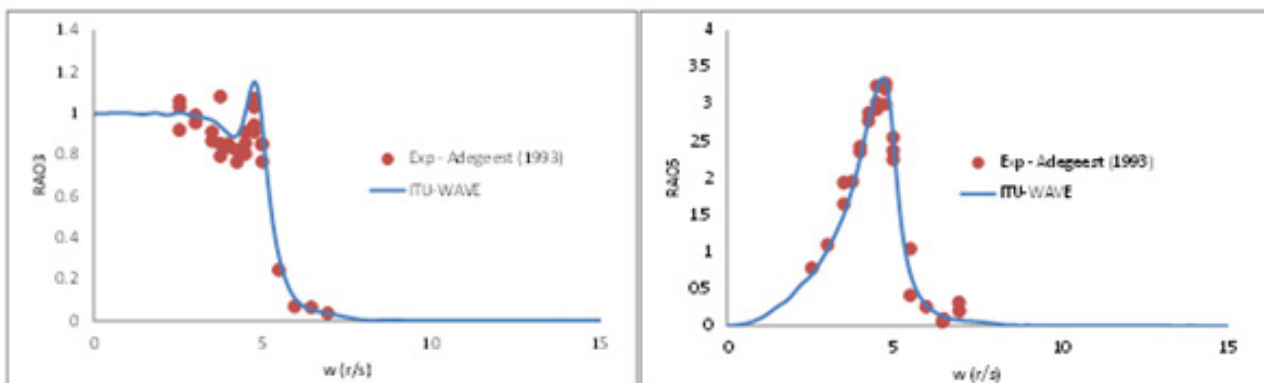


Figure 17: Heave and pitch RAOs of Wigley hull form at $F_n = 0.2$ and $\beta=180^\circ$.

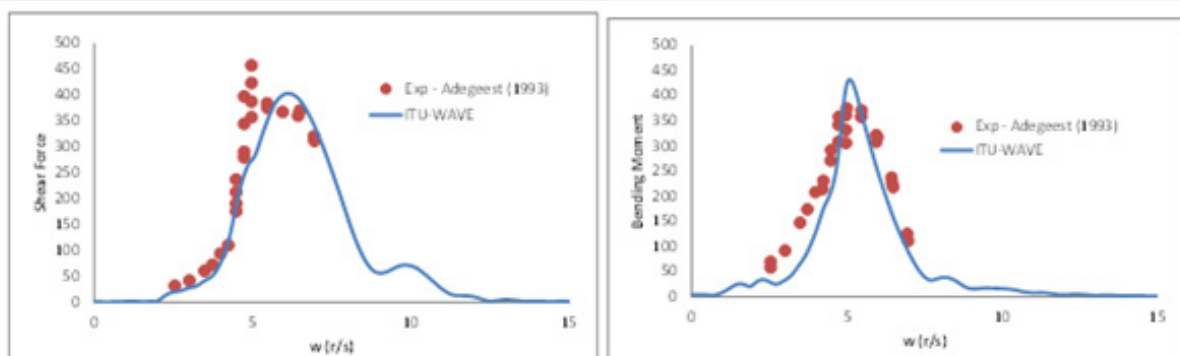


Figure 18: Shear force and bending moment of Wigley hull form at Froude number $F_n = 0.2$ and heading angle $\beta=180^\circ$ using 8 free-free Euler-Bernoulli elastic beam modes.

If the floating body does not deform much compared to rigid body motion, it can be considered as stiff structure implying that contribution of rigid body modes to the disturbance of the pressure field is much greater compared to elastic deformable modes. In this case Eq. (24) and Eq. (25) can be modified to take only contribution of rigid body modes for unknown force coefficients as in presented in Eq. (24a) and Eq. (25a) in which the summation boundary 2 is used for heave and pitch rigid body modes.

$$F_j(t) = k_{jk} x_k(t) = \int_{-\infty}^t d\tau K_{j0}(t-\tau) \zeta(\tau) - \sum_{k=1}^2 \{ (M_{jk} + a_{jk}) \ddot{x}_k(t) + b_{jk} \dot{x}_k(t) + (C_{jk} + c_{jk}) x_k(t) + \int_0^t d\tau K_{jk}(t-\tau) \dot{x}_k(\tau) \} \quad (24a)$$

$$F_j(\omega) = k_{jk} \xi_k(\omega) = x_j(\omega) - \sum_{k=1}^2 \{ -\omega^2 (M_{jk} + A_{jk}(\omega)) + i\omega B_{jk}(\omega) + C_{jk} \} \xi_k(\omega) \quad (25a)$$

The shear force and bending moment of Wigley hull form at heading angle $\beta = 180^\circ$ and Froude number $F_n = 0.2$ are presented in (Figure 18) in which the present ITU-WAVE computational results are compared with the experimental results [22]. Eq. (25a) is used to obtain the force coefficients $F_j(\omega)$ which is then used for the prediction of the shear force and bending moment in Eq. (23).

Conclusion

The application of ITU-WAVE computational tool is extended to include the hydroelastic behaviour of the floating marine structures in the present paper. The hydrodynamic part is solved with a three-dimensional potential panel method whilst Euler Bernoulli beam analysis in which modeshap is defined analtically is used for the prediction of the structural behaviour.

A non-dimensional structural stiffness parameter $S = EI / \rho g L^5$ is used and depending on this stiffness parameter the hydroelastic effects of floating slender barge are studied for RAOs, bending moments, and shear forces. It is found out that the hydroelastic effects are dominant in the range of $10^{-8} < S < 10^{-2}$ for a slender barge. A Wigley hull form is then studied as a stiff structure in order to determine the effects of elastic modes due to rigid body modes only which are coupled with elastic modes. As opposite to the traditional approaches, the effects of the different incident wave lengths and geometry of floating bodies are taken into account for the prediction of bending moments and shear forces in the present study.

Numerical results (including the added-mass and damping coefficients as well as the amplitudes of exciting forces and phase angles which can be obtained by Fourier transform of radiation and exciting IRFs respectively) were presented to demonstrate the convergence of the developed computer code for the radiation and exciting IRFs. The numerical predictions for heave and pitch

RAOs, bending moment, and shear force at mid-ship of Wigley hull form are shown to be in satisfactory agreement with the experimental results.

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