

The division of amyloid fibrils – Systematic comparison of fibril fragmentation stability by linking theory with experiments

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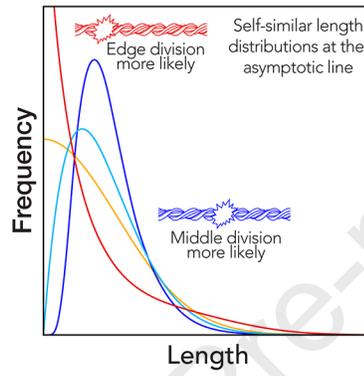
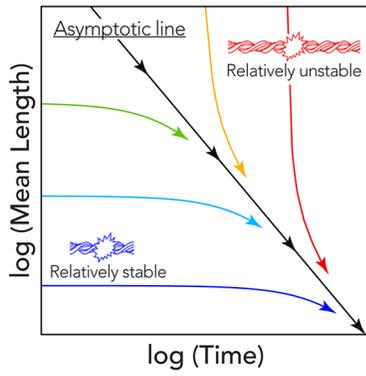
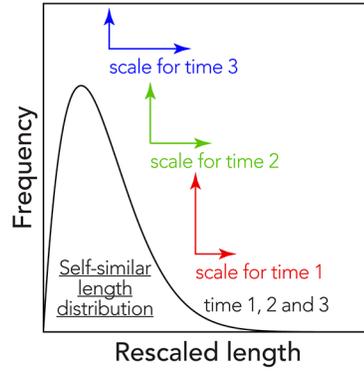
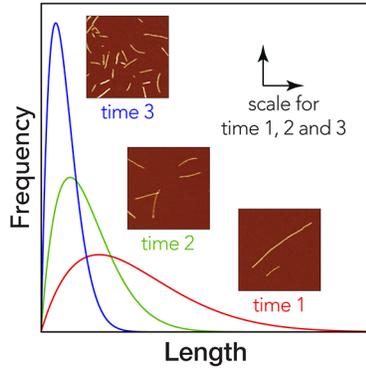
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The division of amyloid fibrils

– Systematic comparison of fibril fragmentation stability by linking theory with experiments

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1

2 **SUMMARY**

3 The division of amyloid protein fibrils is required for the propagation of the amyloid state, and is an
4 important contributor to their stability, pathogenicity and normal function. Here, we combine kinetic
5 nanoscale imaging experiments with analysis of a mathematical model to resolve and compare the
6 division stability of amyloid fibrils. Our theoretical results show that the division of any type of
7 filament results in self-similar length distributions distinct to each fibril type and the conditions
8 applied. By applying these theoretical results to profile the dynamical stability towards breakage for
9 four different amyloid types, we reveal particular differences in the division properties of disease-
10 related amyloid formed from alpha-synuclein when compared with non-disease associated model
11 amyloid, the former showing lowered intrinsic stability towards breakage and increased likelihood of
12 shedding smaller particles. Our results enable the comparison of protein filaments' intrinsic dynamic
13 stabilities, which are key to unravelling their toxic and infectious potentials.

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INTRODUCTION

Amyloid fibrils, proteinaceous polymers with a cross-beta core structure, represent an important class of bio-nanomaterials (Bleem and Daggett, 2017; Knowles and Buehler, 2011). They are also important biological structures associated with devastating human diseases such as Alzheimer's disease, Parkinson's disease, Creutzfeldt-Jakob disease (CJD), systemic amyloidosis and type 2 diabetes (Knowles et al., 2014), as well as having vital biological functions such as adhesion and biofilm formation, epigenetic switches, and hormone storage (e.g. Berson et al., 2003; Bleem and Daggett, 2017; Chapman et al., 2002; Knowles and Buehler, 2011; Larsen et al., 2007; Li et al., 2014; Romero et al., 2010; Tuite and Serio, 2010). Division of amyloid fibrils, which can manifest *in vitro* in amyloid nanomaterials or *in vivo* in disease-associated or functional amyloid aggregates, is mediated by mechanical agitation, thermal stress, chemical perturbation or chaperone catalysis. Fibril division is a crucial step in the life-cycle of amyloid (**Fig. 1a**) (Xue, 2015) and enables the propagation of the amyloid protein conformation and biological information encoded therein. Despite knowledge of its importance, it is not understood why amyloid division processes give rise to varied biological impacts ranging from normal propagation of functional amyloid assemblies to large inert structures or the creation of molecular species involved in disease, e.g. small cytotoxic amyloid species and infective prions, which are transmissible amyloid particles. In this respect, the resistance of amyloid to division is also a critical aspect to protein misfolding associated with disease progression and biological roles of functional amyloid assemblies (e.g. Tanaka et al., 2006). In terms of disease association, there is much debate as to how amyloid aggregates are associated with cellular toxicity, with evidence of both prefibrillar oligomers and fibrillar species (Breydo and Uversky, 2015; Tipping et al., 2015) giving rise to disease-related phenotypes. While it is hypothesised that all proteins can undergo conversion into an amyloid state (Dobson, 1999), why most proteins do not form amyloid under physiological conditions or produce amyloid particles that are non-toxic, non-

1 transmissible or non-disease associated is not clear. In this debate, it has been suggested that fibrils
2 are not merely the end product of amyloid aggregation, but rather elicit profound biological responses
3 through fibril fragmentation and oligomer shedding (Tipping et al., 2015), due to lack of fibril
4 stability.

5
6 Amyloid fibrils have remarkable physical properties, such as their tensile strength comparable to that
7 of steel and elasticity similar to spider silk (Knowles et al., 2007). As proteinaceous polymers, they
8 also offer the potential for modification by rational design, which makes them an ideal target for the
9 development of biologically compatible nanomaterials (Bleem and Daggett, 2017; Hu et al., 2018; Li
10 et al., 2014; Mankar et al., 2011). This interest in amyloid as a bio-nanomaterial has led to a search for
11 proteins and peptides which can undergo conversion into a stable amyloid conformation while lacking
12 the properties that associate them with toxicity, infectivity and disease. Though the precise properties
13 that associate some amyloid to disease or biological function are not resolved, the potential for
14 different morphologies (sometimes referred to as 'strains') to elicit different results (Meinhardt et al.,
15 2009; Sachse et al., 2010; Tanaka et al., 2006) could be attributed to the stability of amyloid fibrils
16 towards division or their mechanical properties (Marchante et al., 2017; Xue et al., 2009a). Thus, the
17 stability of amyloid fibrils is an important physical factor which modulates their biological function of
18 amyloid and potential as a nanomaterial.

19
20 The kinetics of the nucleated growth of amyloid fibrils are profoundly influenced by secondary
21 processes such as fibril fragmentation/breakage (Knowles et al., 2009; Xue et al., 2008) and
22 secondary surface nucleation (Buell et al., 2014; Tornquist et al., 2018) (**Fig. 1a**). These processes
23 determine the rate of the exponential growth phase of amyloid assembly alongside with growth by
24 elongation at fibril ends (Lorenzen et al., 2012; Xue et al., 2008). As one of the key secondary
25 processes, fibril fragmentation stands out compared to the other three main processes (**Fig. 1a**) in that
26 it reduces aggregate size at the same time as it increases the number of aggregates (Xue et al., 2009a).

1 In this aspect, fibril fragmentation results in the division of amyloid fibrils analogous to a microbial or
2 cellular division process. Resistance to fibril fragmentation is linked to the mechanical stability of
3 amyloid fibrils, which has implications for both the development of nanomaterials and on the
4 understanding of amyloid disease-associated biological processes. The mechanism and the rate of
5 fibril fragmentation have been subjected to theoretical considerations (Hill, 1983; Knowles et al.,
6 2009; Paparcone and Buehler, 2011; Xue et al., 2008) and experimental investigations involving
7 fragmentation promoted by mechanical perturbations (Nicoud et al., 2015; Xue et al., 2008; Xue and
8 Radford, 2013). The fragmentation of protein filaments is a length dependent process whereby longer
9 particles break more easily than short ones. This length-dependent breakage of amyloid fibrils can
10 follow a strong, non-linear dependence where longer fibrils are progressively less stable towards
11 breakage per monomeric unit relative to their shorter counterparts (Xue and Radford, 2013). Thus, the
12 fibrils' resistance to division, and in turn the inherent stability of the fibrils, is an important and
13 measurable property (Xue and Radford, 2013) that will help rationalise phenomena such as prion
14 strains, polymorphism, transmission, amyloid toxicity, biofilm formation and epigenetic regulation
15 (e.g. Aguzzi et al., 2007; Cox et al., 2003; Derdowski et al., 2010; Lee et al., 2011; Lin et al., 2017;
16 Marchante et al., 2017; Shorter and Lindquist, 2004; Sondheimer and Lindquist, 2000; Tanaka et al.,
17 2006; Xue et al., 2009a; Zeng et al., 2015) and lead to a better understanding of amyloid-associated
18 diseases.

19

20 The division of amyloid polymers into small more infective particles, either through environmental
21 perturbations or through catalysis by molecular chaperones, is key to the spreading of prion
22 phenotypes (Cox et al., 2003; Marchante et al., 2017). For example, the propagation of the yeast prion
23 phenotype [*PSI*⁺] associated with yeast Sup35 protein assemblies relies on the fragmentation activity
24 of the chaperon Hsp104 and its co-chaperones (Chernoff et al., 1995; Shorter and Lindquist, 2004).
25 The resistance of Sup35 assemblies to fragmentation correlates with the formation of different [*PSI*⁺]
26 phenotypes (Tanaka et al., 2006). In addition, the smaller particles generated by fibril fragmentation
27 show enhanced cytotoxicity when compared with the larger parent fibrils (Xue et al., 2009a), likely

1 due to a higher propensity to interact with cell membranes, entering cells by endocytosis, interacting
2 with the lysosome and inducing cytotoxicity by disrupting proteostasis (Ankarcrona et al., 2016; Hu et
3 al., 2009; Jakhria et al., 2014; Marchante et al., 2017; Milanesi et al., 2012). The stability of amyloid
4 fibrils towards division is, therefore, an important characteristic of amyloid fibrils that must be
5 considered if we are to understand the biological activity and nanomaterial properties of amyloid.
6 Because protein filaments formed from different precursors show a variety of suprastructures and size
7 distributions (e.g. Barritt et al., 2017; Knowles et al., 2007; Meinhardt et al., 2009; Xue et al., 2009a),
8 no unifying theory has been developed for the division of amyloid fibrils. As consequence, the
9 stability towards division for different types of amyloid fibrils with varied suprastructures that ranges
10 from inert network of long filaments to infectious particles is yet to be systematically measured,
11 determined and compared.

12

13 We have previously shown that the time evolution of amyloid fibril length distributions obtained by
14 nanoscale atomic force microscopy (AFM) imaging contain valuable information on the rate, length-
15 dependence and position-dependence of fibril fragmentation that can be extracted (Xue and Radford,
16 2013). However, since fibril division is itself a strongly length-dependent process, systematic
17 comparison of the stability of fibrils towards division and their division rates has been hampered by
18 the varied length distributions of different types of amyloid fibrils. Currently, the links between data
19 and theory that would allow direct comparison of the fibrils' division propensities are also missing.
20 Here, we have developed an analytical approach that enables direct determination of the dynamic
21 stability of amyloid fibrils towards division from fibril length distributions. We have developed a new
22 theory on amyloid fibril division that shows how the division mechanism of amyloid fibrils and their
23 stability towards division dictates the exact shape of the resulting length distributions. We then
24 established an analytical method to extract a set of unique and intrinsic properties of the fibril stability
25 to division from image data of pre-formed fibrils undergoing physical fragmentation experimentally
26 promoted by mechanical perturbation. Demonstrating the utility of our combined experimental and
27 theoretical approach, we determined and compared the division of fibril samples formed from human

1 α -synuclein (α -Syn) associated with Parkinson's disease with fibrils formed from β -lactoglobulin (β -
2 Lac) and lysozyme (Lyz). We have also reanalysed and compared previously published fibril
3 fragmentation data of β_2 -microglobulin (β_2m) under the same mechanical perturbation regime (Xue
4 and Radford, 2013). Comparison of the dynamic stability of these fibrils types of different origin
5 revealed different division properties, with fibrils formed from the human Parkinson's disease-
6 associated α -Syn being the least overall stable and prone to generate small sub 100 nm particles that
7 may possess enhanced cytotoxic and prion-like infectious potential (Brundin and Melki, 2017). The
8 ability to assess and compare the division properties of amyloid fibrils, enumerated as parameters
9 extractable from experimental data, enables the prediction of an amyloid's propensity to generate
10 toxic and infectious particles, and therefore has a significant impact on the understanding of their
11 roles in biology, in diseases, and their application as a functional bio-nanomaterial.

12

13

14 **RESULTS**

15

16 **Amyloid fibrils of diverse suprastructures and length distributions fragment to different extents** 17 **upon mechanical perturbation**

18

19 To demonstrate that the fibril division rates, indicative of their dynamic stability to division, can be
20 assessed and compared for amyloid fibrils with diverse suprastructures and length distributions, we
21 first collected experimental AFM image data sets of amyloid fibrils, pre-formed from different
22 precursors, undergoing division through fragmentation promoted by mechanical stirring. These
23 experiments were designed to isolate the fibril division processes from other growth processes and to
24 generate data that contain sufficient quality and quantity of information on the division of fibril
25 particles under identical mechanical perturbation regimes to enable comparison. Here, we chose to

1 investigate the human disease-associated amyloid system α -Syn alongside bovine β -Lac and chicken
2 egg white Lyz as biophysical model systems not directly related to human disease. Samples were
3 formed containing long, straight fibrils from these three proteins *in vitro*, and validated by negative-
4 stain Electron Microscopy imaging (**Supplementary Fig. S1**). Lyz and β -Lac were both converted to
5 their fibrillar amyloid form by heating under acidic conditions (pH 2.0), commonly used conditions
6 for the assembly of these proteins *in vitro*. α -Syn fibrils were prepared from freshly purified
7 recombinant α -Syn monomers (Cappai et al., 2005) at 37°C under physiological pH. For each fibril
8 sample, 500 μ l of 120 μ M monomer equivalent fibril solutions in their respective fibril forming buffer
9 were then stirred at 1000 rpm by a 3 x 8mm magnetic stirrer bar in a 1.5ml glass chromatography vial
10 using the same mechanical perturbation method as previously reported (Xue and Radford, 2013) using
11 an Ika Squid stirrer plate with a digital display. The *in vitro*-formed fibril samples were initially
12 dispersed by 5-10 min of stirring and were subsequently deposited onto freshly cleaved mica surfaces
13 and imaged by AFM (**Fig. 2** left most column).

14

15 As seen in the leftmost column of images in **Fig 2.**, the initial samples after brief stirring to disperse
16 the fibril particles show long, straight, elongated, unbranched nano-structures expected for amyloid
17 fibrils. However, whereas Lyz and α -Syn form fibrils that exhibit more flexibility and curvature, β -
18 Lac forms comparably shorter, straighter, more rigid assemblies consistent with previous observations
19 (e.g. Knowles et al., 2007; Lara et al., 2011; Nicoud et al., 2015; Sweers et al., 2012). The Lyz and β -
20 Lac images also display higher background noise compared to the images of α -Syn fibrils, which may
21 reflect their overall less efficient fibril assembly reaction conditions compared to α -Syn. Importantly
22 however, all of the samples showed well-dispersed fibril particles that can be individually measured
23 after the brief stirring treatment, as the samples did not show strong propensity for clumping on the
24 surface substrates.

25

1 The samples were then continuously stirred for up to 15 days and 1-5 μl samples (see Materials and
2 Methods) were taken out periodically and imaged using AFM to visualise their fragmentation under
3 mechanical perturbation (**Fig. 2**). For each sampling time-point, an identical AFM specimen
4 preparation procedure was used for each amyloid type, and $20\ \mu\text{m} \times 20\ \mu\text{m}$ surface areas were imaged
5 at 2048×2048 pixels resolution in order to enable quantitative analysis of individual fibril particles as
6 previously described (Xue, 2013; Xue et al., 2009b). In total, fragmentation of two independent fibril
7 samples was followed for each fibril type, and 171 images with at least 300 particles for each sample
8 and time point were analysed, giving a total dataset containing physical measurements of more than
9 220,000 individual fibril particles for the three amyloid types (**Supplementary Table S1**).

10

11 Quantitative single-particle measurements of fibril length and height distributions (**Fig. 3**, leftmost
12 column corresponding to images in **Fig. 2**, leftmost column) reveal that the fibrils have substantially
13 different initial dimensions. Analysis of their height distributions shows that the initial fibril heights,
14 indicative of the width of the fibrils, are around 7 nm for α -Syn fibrils, and around 3 nm for both β -
15 Lac and Lyz fibrils. The initial length distributions for the different fibril types were also dissimilar,
16 with both Lyz and α -Syn forming fibrils of up to $\sim 10\ \mu\text{m}$ in length whereas β -Lac formed shorter
17 particles with lengths of up to $\sim 2\ \mu\text{m}$ under the conditions employed.

18

19 Qualitative inspection of the AFM images throughout the experiment (**Fig. 3**) showed that the
20 amyloid fibrils were fragmented into much smaller particles under the applied mechanical
21 perturbation (**Fig. 2** and **Fig. 3**) as expected. However, the rate of division and shortening of the
22 particles' lengths was seen to differ between the three different fibril types analysed (**Fig. 3** and
23 **Supplementary Fig. S2**). Analysis of the time evolution of the fibril height and length distributions
24 obtained by quantification of individual particles in the AFM images over the course of the
25 experiment confirmed that fibril fragmentation did not cause detectable changes in fibril morphology
26 and fibril width through lateral association and dissociation. Average fibril heights in the AFM

1 images, indicative of fibril widths, remained consistent throughout the experiment for Lyz and α -Syn.
2 The same was also largely observed for β -Lac, with the exception that a small second population of
3 taller polymers at the very end of the fragmentation time-course after 432000 s were exhibited (height
4 graphs in **Fig. 3** and **Supplementary Fig. S2**). Hence the division of the fibrils under mechanical
5 perturbation applied has resulted in a shortening of average fibril length.

6
7 To confirm that the changes in fibril length by fibril division did not cause disaggregation or release
8 of monomer/small oligomers (e.g. dimers), we next determined the residual monomer concentration
9 of the samples. For each fibril type, aggregates were pelleted by centrifugation (75k rpm, 15 min)
10 after fragmentation time-course and the presence of monomer in the supernatants was quantified by
11 SDS-PAGE. The comparison between the initial samples and those fragmented over two weeks
12 showed no substantial changes in the protein composition of the supernatants, with differences of less
13 than 2% for all amyloid systems analysed (Lyz: 1.4%, β -Lac: <1%, and α -Syn: 1.3%, **Supplementary**
14 **Fig. S3**). These data confirmed that the time-dependent imaging experiments we carried out pertain
15 almost exclusively to the fibril division processes along the length of the pre-formed fibrils, and
16 therefore, contain valuable information on their division rates and their stability to division.

17

18 **Time evolution of fibril length distributions converges to time-independent, characteristic, self-** 19 **similar length distribution shapes**

20

21 The fibril samples formed from different protein precursors have different initial length distributions
22 (as seen in **Fig. 2** and **Fig. 3**). However, fibril division is itself a strongly length-dependent process
23 (Xue and Radford, 2013) as short fibril particles will be more resistant towards division compared to
24 longer particles, irrespectively of any differences in the intrinsic stability of the different fibril types to
25 division. Therefore, to compare the stability of amyloid fibrils with different suprastructures and

1 length distributions towards division, a new approach to extract information intrinsic to each fibril
 2 type independent of their experimentally different initial length distributions must be developed.
 3 Consequently, in parallel with the experiments described above, we mathematically analysed the
 4 division equation of amyloid fibrils so that key information on the stability of amyloid fibrils to
 5 division could be resolved. We first describe the division of amyloid fibrils mathematically using a
 6 continuous framework based on the partial differential equation (PDE) Eq. (1). Since the number of
 7 monomers inside a fibril observed in the image data is large, typically in the order of 10^2 or more, we
 8 assumed continuous variables x and y that correspond to the length of fibrils (for example as defined
 9 in **Fig 1b** where y is the length of the parent fibril and x is the length of one of the daughter fibrils).
 10 This approach has the advantage that the infinite set of ordinary differential equations (ODEs)
 11 normally used to describe the length-dependent division processes (e.g. Knowles et al., 2009; Xue et
 12 al., 2008; Xue and Radford, 2013) can now be collapsed into a single continuous PDE that can be
 13 treated analytically (see Supplemental Information for details). Denoting $u(t,x)$ as the distribution of
 14 fibrils of length x at time t in number concentration units (e.g. Molar units), Eq. (1) is the
 15 mathematical translation of the pure division model described by the schematics in **Fig.1b-d**, where
 16 we assume any parent fibril can divide into two daughters, and the end-end reattachment rate of
 17 daughter fibrils is negligible (Hill, 1983):

$$\frac{\partial}{\partial t} u(t,x) = -\alpha_0(\alpha x)^\nu u(t,x) + 2 \int_{y=x}^{\infty} \frac{1}{y} \kappa_0 \left(\frac{x}{y} \right) \alpha_0(\alpha x)^\nu u(t,y) dy$$

18 Eq. (1)

19 In Eq. (1), $\frac{\partial}{\partial t} u(t,x)$ denotes the time (t) evolution of the concentration of fibrils with length x . Here,
 20 we model the total division rate constant of fibrils of size x using the power law $\alpha_0(\alpha x)^\nu$, which we
 21 denote as $B(x)$ (Hill, 1983) (see Supplementary Information), where α_0 is a constant unit reference
 22 we set to 1 s^{-1} . The first term in Eq (1), therefore, denotes the rate of loss of fibrils with length x by
 23 division into smaller fibrils. The probability that after dividing, a given parent fibril of length y gives
 24 rise to a daughter fibril fragments of length x and $y-x$ depends on the ratio of the lengths (x/y) (Xue

1 and Radford, 2013) and is given by the probability density function $\frac{1}{y} \kappa_0 \left(\frac{x}{y} \right)$. The second integral term
 2 in Eq. (1), therefore, denotes the total gain of fibrils with length x by division of all fibrils with length
 3 y that are larger than x . Interestingly, Eq. (1) describes a fundamental division process that is
 4 mathematically analogous to the division of molecules, macroscopic materials and cells (Escobedo et
 5 al., 2005; Robert et al., 2014), and we have mathematically proven that its behaviour is entirely and
 6 uniquely dictated by three properties: α that describes the magnitude of the division rate constant, γ
 7 that describes the fibril length dependence of the division rate constant, and κ_0 that describes the
 8 probability of division at any given position along a fibril, also called the fragmentation kernel
 9 (Doumic et al., 2018). We then proceeded to solve Eq. (1) analytically with regard to α , γ and κ_0
 10 using theoretical results shown in (Escobedo et al., 2005) and (Doumic et al., 2018) (see
 11 Supplementary information). From our solution, we note four key predictive insights that emerged
 12 from our analysis (**Fig. 4**).

13

14 Firstly, we note that given enough time, the decay of the average fibril length will converge to the
 15 same rate independently of the initial fibril length distributions. This result comes from that after a
 16 sufficiently long time, the reduction of average length of the fibril length distribution can be described
 17 as a power law versus time (Eq. 2, see Supplementary Information):

$$\mu(t) = C \cdot t^{-1/\gamma}$$

18

Eq. (2)

19 where C is a constant. As seen in Eq. (2), the experimentally observable average length of a sample,
 20 $\mu(t)$, is predicted to tend towards a straight line when plotted on a log-log plot with the slope of the
 21 line representing $-1/\gamma$ (Eq. 2, black line in **Fig. 4b**) because the long-time behaviour of Eq. (1) can be
 22 described as a power law.

23

1 Secondly, we note that given enough time, the fibril length distribution will converge to the same
 2 shape independently of the initial state of the fibril length distribution. After a sufficiently long time
 3 ($t \gg t_0$), the distribution of fibril-lengths tends towards a time-independent distribution shape, $g(x_g)$,
 4 that scales only with t and γ , but does not depend on the initial length distribution (Eq. (3) and
 5 Supplementary Information).

6

$$g(x_g) \approx f(t, x) \cdot t^{-\frac{1}{\gamma}}, \quad x_g = xt^{\frac{1}{\gamma}}, \quad \text{For any } t \gg t_0$$

7

Eq. (3)

8 where $f(t, x)$ are experimentally measured length distributions. This point is of key importance for
 9 characterising and predicting fibril division processes because it establishes that for any fibril type
 10 under certain conditions: 1) a distinct fibril length distribution shape (**Fig. 4a**) will be reached
 11 independently of the initial fibril length distribution, and 2) the length distribution and the average
 12 length will shrink as function of time in a predictive manner as fibrils continue to divide (e.g. the
 13 black line in **Fig. 4b** for the mean length) but the shape of the distribution will not change as function
 14 of time, i.e. the length distribution can be rescaled to the same $g(x_g)$ using Eq. (3) at any time t along
 15 the black line in **Fig. 4b** if t is sufficiently large. We refer to the distributions with the scaling property
 16 and shape invariance property as ‘self-similar length distributions’ (**Fig. 4a**).

17

18 The existence of a self-similar length distribution that is initial length distribution-independent and
 19 shape invariant over time, as well as the predictable decay of fibril lengths as fibrils divide (e.g. the
 20 reduction of the average length in **Fig. 4b**) can be seen as a characteristic behaviour specific to
 21 individual fibril types under distinct conditions. This fibril division behaviour can, therefore, be
 22 classed as a type of intrinsic dynamic stability of the fibrils. One way to visualise this property is
 23 shown in **Fig. 4b** represented by the black line, here referred to as the fibril type’s ‘asymptotic line’
 24 under the conditions applied. Any fibril populations above this line are relatively unstable and will

1 rapidly divide, pushing the average length towards the line (red and yellow coloured near-vertical
2 arrows showing rapid decay of unstable fibril lengths). In contrast, any fibril populations below this
3 line are comparatively stable or metastable and will only slowly evolve towards the line through
4 division (green to blue coloured near-horizontal arrows showing slow decay of stable fibril lengths
5 towards the black line). Importantly, this result also indicates that the dynamic stability of fibrils to
6 division represented by the asymptotic line: 1) can be determined from experimental data, 2) is
7 intrinsic to fibril type and conditions applied, and 3) can be compared independently of varied starting
8 fibril length distributions, if the characteristic self-similar length distributions that contain information
9 about the intrinsic dynamic stability of the fibrils is reached (e.g. the asymptotic line is reached in an
10 experiment running for sufficiently long length of time).

11

12 Thirdly, we note that the probability of division in the centre of a fibril as compared to the shedding of
13 small particles from fibril edge can be evaluated from the experiments. The self-similar length
14 distributions contain information about κ_0 . **Fig. 4c** shows how different self-similar fibril length
15 distributions are indicative of different κ_0 probability functions. As seen in **Fig. 4c**, a κ_0 indicative of
16 fibril types that are more likely to divide in the middle will result in fibril length distributions with a
17 distinct peak and low relative population of small fragments. In contrast, a κ_0 indicative of fibril types
18 and conditions that promote equal likelihood of division along the fibril or even favouring the
19 shedding of fragments from fibril edges will result in self-similar fibril length distributions that have
20 large relative population of small fibril fragments that may possess enhanced cytotoxic and/or
21 infective potential compared to κ_0 favouring division in the centre of the fibrils.

22

23 Finally, the dynamic stability of fibrils to division, their propensity to break at different lengths, can
24 be determined. The first order division rate constant $B(x) = \alpha_0(\alpha x)^\gamma$ that describes the division of
25 the fibrils as a function of their length x can be directly evaluated from the self-similar length
26 distribution and γ (see Eq. 2) when $t \gg t_0$ (see Supplementary information and Eq SI.21) where t_0 is

1 the start of the experiment. Thus, the division rate constant $B(x)$ can be determined from
2 experimentally observing how fibril length distributions change with time when the self-similar fibril
3 length distribution is obtained, and they are important parameters for defining and comparing the
4 fibrils intrinsic dynamic stability to division. The effect of different values of α and γ on fibril
5 stability is visualised in **Fig. 4d** and **Fig. 4e** as characteristic the asymptotic line plotted in log-log
6 plots of average length versus time. The enumeration of the asymptotic line described by $B(x)$ will
7 subsequently enable direct quantitative comparison of the fibrils' stabilities towards division.

8

9 **The division properties of amyloid fibrils can be obtained from image data and their complex**
10 **stability to division can be compared**

11

12 Applying the results of the mathematical analysis to the experimental AFM image data sets, the
13 parameters γ , α , and the characteristic self-similar length-distributions $g(x_g)$ indicative of κ_0 can be
14 extracted and meaningfully compared as a measure of the fibrils' intrinsic stability to division. We
15 first determined the γ values for each of the fibril types, by globally fitting a variant of Eq. (2) to the
16 time evolution of average fibril length (see Materials and Methods, **Fig. 5**). We also reanalysed
17 previously published data set on β_2m fibril fragmentation under the same mechanical perturbation
18 conditions (Xue and Radford, 2013) using our new theoretical results above and included the
19 reanalysis in the comparison.

20

21 The constant γ was determined from least-squares fitting of our analytical result to the data (Materials
22 and Methods). The power law relationship (Eq. 2) parameterised with γ determined by global analysis
23 was visualised on a log-log plot of mean fibril length vs. time in **Fig. 5**, together with the measured
24 mean fibril lengths. The resulting γ values are listed in **Table 1**. A γ value of 1 would suggest that the
25 division rate of fibrils is only dependent on the number of division sites per fibril, which is linearly

1 related to the number of monomers in the fibrils and in turn to the length of the fibrils. However, the γ
2 values for α -Syn, β -Lac and β_2 m are all significantly larger than 1, indicating highly length dependent
3 microscopic division rates for division sites in these fibril types. Of the four fibril types analysed, the
4 division of Lyz fibrils yielded a γ value closest to 1. This suggests the division rates for Lyz fibrils
5 may only depend on the number of available division sites along the fibrils. β -Lac fibrils yielded the
6 highest γ value of the fibril types analysed. This demonstrates that β -Lac fibril fragmentation is highly
7 length-dependent, and small β -Lac fibril fragments are more resistant to further fragmentation
8 compared with the other fibril types. This behaviour may corroborate with an increased lateral
9 association of small β -Lac fibril fragmentation fragments observed on the height distributions at the
10 end of the time-course experiments (height graphs in **Fig. 3** and **Supplementary Fig. S2**). As seen in
11 **Fig. 5**, the later time points for all of our fibril types follow a straight line on the log-log plots (solid
12 section of the fitted lines in **Fig. 5**), indicating that the self-similar length distributions, and hence the
13 asymptotic line, were sufficiently reached in all cases. The analysis also revealed that all of the fibril
14 types analysed approached the self-similar length distribution shapes in less than 5 hr, with the
15 exception of the Lyz samples that reached the self-similar distribution in approximately 24 hr.

16

17 The α values were subsequently calculated (listed in **Table 1**) with equations Eq. (S21) using all of
18 the fibril length distributions at time points post reaching the near-characteristic self-similar
19 distribution shapes (represented by the solid lines in **Fig. 5**). Once both α and γ values have been
20 extracted from the length-distribution data, the division rate constant $B(x)$ can be obtained for fibrils
21 of any length x . **Table 1** shows the division rate constant calculated for fibrils of 100 nm. The
22 asymptotic line for the fibrils types characterised by the division rate constant $B(x)$ (**Fig. 6b**) or by
23 fibril mean length (**Fig. 6a**) as function of time was also visualised and compared independently of
24 initial fibril length, showing that α -Syn and Lyz fibrils fragments fastest at long-times under the
25 mechanical perturbation applied, suggesting that these fibrils were less stable than the β -Lac and β_2 m
26 fibrils.

1

2 Next, we determined the shape of the self-similar length distributions for each fibril type by rescaling
3 the experimental length distributions to $g(x_g)$ with Eq. (3) using the γ values obtained above. As with
4 the evaluation of α values, only time points where the length distributions closely approached the self-
5 similar length distribution (time points in the section represented by the solid lines in **Fig. 5**) were
6 averaged to obtain $g(x_g)$ for each fibril type (**Supplementary Fig. S4**). **Fig. 6c** shows how the self-
7 similar length distribution shapes compare with each other at extended times (2 weeks) when
8 calculated using $g(x_g)$ (**Supplementary Fig. S4**) with Eq. (3). As seen in Fig 6c, Lyz fibrils tend to
9 produce high relative populations of small particles less than 100 nm long followed by α -Syn and then
10 β_2m . On the other hand, the division of β -Lac fibrils resulted in a lower relative population of small
11 particles over the same long time scale used for the other fibril types.

12

13 Finally, to validate our model and the predictive power of our approach, we performed direct
14 simulations of the fibril division time-course (**Fig. 7**) using only the individual sets of division
15 parameters obtained for each of our fibril types. For each simulation, we used the initial experimental
16 length distributions (dashed lines in **Fig. 7**) directly as the starting points for the simulations. The
17 large set of ordinary differential equations describing the chemical master equation for the system
18 (Xue and Radford, 2013) was then solved to see whether our analytical model was able to predict the
19 full division behaviour and the time evolution of the fibril length distributions for each fibril type. As
20 seen in **Fig. 7**, the result of the numerical simulations based on our results show remarkable
21 agreement with the experimental data. This unequivocal result validated the fact that the set of three
22 properties γ , α , and κ_0 are indeed capable of fully and uniquely describing the complex amyloid
23 division processes, and the enumeration of these properties yield valuable insights. Such insights
24 allow meaningful comparison of the amyloid fibrils' intrinsic stability to division.

25

1

2 **DISCUSSION**

3

4 The understanding of the properties that underline the biological activities of amyloid nano-structures,
5 such as their cytotoxic and infectious potentials, is crucial for the understanding of why some amyloid
6 is associated with devastating human diseases. The division of amyloid fibrils, for example through
7 fibril fragmentation by mechanical perturbation (Xue et al., 2008; Xue and Radford, 2013), enzymatic
8 action (Chernoff et al., 1995; Glover and Lindquist, 1998) or other cellular or environmental
9 perturbations, is a key step in their life-cycle that results in the exponential growth in the number of
10 amyloid particles. Simultaneously, daughter particles resulting from the division of parent fibrils
11 cause a reduction in the overall size distribution as division proceeds. These two consequences of
12 division are undoubtedly linked to the enhancement of the cytotoxic and infectious potentials of
13 disease-associated amyloid (Marchante et al., 2017; Xue et al., 2009a). The amyloid fibrils' resistance
14 to division, i.e. the stability of the amyloid fibrils to division, rationalises these two fundamental
15 requirements for pathogenicity associated with amyloid. Akin to uncontrolled division of cells or any
16 pathogenic microorganisms, the division step in the amyloid life cycle (**Fig. 1**) could be a key
17 determinant in their overall potential to be associated with properties in the amyloid and prion
18 associated pathology.

19

20 Here, we have developed a theory, as well as an experimental approach utilising our theoretical
21 insights to resolve the amyloid fibrils' dynamic stability to division. These represent a step forward in
22 how we are able to study the amyloid fibril division processes such as in fibril fragmentation and
23 prion propagation, essentially the replication step in the amyloid lifecycle. It also allows the direct
24 comparison between amyloid particles of different molecular types and quantifies the difference in
25 division and stability between those that are and are not disease associated. Specifically, we have
26 applied our theoretical results to the comparison of a diverse set of amyloid assemblies consisting of

1 human α -Syn (a neurodegenerative disease-associated amyloid, sample formed under physiological
2 solution conditions), human β_2m (a systemic amyloidosis disease-associated amyloid, sample formed
3 under acidic pH, data from Xue and Radford, 2013), bovine β -Lac and hen egg white Lyz (later two
4 cases are both biophysical model systems not directly related to human disease but converted to
5 amyloid when subjected to heating in acidic pH). By fully analysing and comparing their division
6 behaviour, which is uniquely described by the triplet of parameters (α , magnitude of the division rate
7 constant, γ , fibril length dependence of the division rate constant, and κ_0 , probability of division at any
8 given position along a fibril) under identical mechanical perturbation for long timescales using our
9 approach, we show a remarkable difference in the stability of these different amyloid assemblies
10 relative to each other and how they divide (summarised in **Fig. 8**). Interestingly, for the four fibril
11 types we included here, considering the division rate constant B with their cross-sectional area, the
12 disease-associated human α -Syn fibrils demonstrate lowest overall stability to division followed by
13 Lyz, human β_2m and finally β -Lac particles that are most stable towards division (**Fig 8**. last row).
14 Based on the comparison of the α and γ parameters that together describe the division rates $B(x)$, the
15 likelihood that small α -Syn particles (<100 nm long) will divide is similar to that of Lyz particles of
16 identical length despite having more than double the mean width (and thus around four times bigger
17 cross-sectional area, **Table 1** and **Fig. 8**). More importantly, the division of α -Syn particles also
18 results in a larger relative concentration of small particles compared to β_2m and β -Lac. These results
19 show that human α -Syn amyloid fibrils are relative unstable assemblies capable of a more rapid
20 shedding of small particles that could well possess enhanced cytotoxic and infectious potentials
21 (Peelaerts et al., 2015) through division compared with the other fibril types investigated here. Thus,
22 our results also directly suggest a testable causality link between the low stability of α -Syn fibrils to
23 division and recent observations that human α -Syn may behave in a prion-like manner in cell to cell
24 propagation and their cytotoxicity (Steiner et al., 2018).

25

26 Since the division of amyloid fibrils is an integral part in the propagation of the amyloid conformation
27 (**Fig. 1**), the nanoscale materials properties of amyloid underpin processes which drive the

1 proliferation of amyloid, as well as their varied roles in biology. Therefore, it is important to
2 appreciate the suprastructural properties of amyloid (e.g. clustering, bundling, twist, stiffness, width
3 distribution, orientation distribution, and length distribution etc) at mesoscopic (nanometre to
4 micrometre) length scales, as these properties will influence how individual amyloid fibrils divide.
5 Our data show that despite all amyloid consisting of a cross-beta core structure, their ability to resist
6 division through fragmentation promoted by mechanical perturbation varies strongly between fibril
7 types. Since the stability of amyloid fibrils to division will depend on their suprastructural properties,
8 which in turn depend on their precise structure at atomic level, mesoscopic level structural properties
9 may well be the missing link between amyloid structure and the varied biological effects and
10 consequences that different amyloid types evoke under different conditions. While the results reported
11 here reveal the breakage behaviour of fibril populations, future advances in AFM imaging may allow
12 either individual polymorphs in a fibril population to be distinguished or individual fibrils to be
13 tracked in real-time, further revealing how fibrils divide as individuals. Thus, it should be possible to
14 generate a structure activity relationship correlating the suprastructural properties of amyloid, their
15 ability to divide, and their cytotoxic and/or infectious potentials. Understanding this structure activity
16 relationship for amyloid assemblies could lead to the design of bio-safe polymers with tuned
17 mechanical and nanomaterials properties as well as rationalise the disease-associated properties of
18 amyloid structures.

19

20 Analogous to the diverse response of soluble folded proteins towards unfolding by chemical
21 denaturants, thermal melting and mechanical force etc., the stability of amyloid fibrils could also vary
22 depending on the nature of the perturbation. Indeed, amyloid fibrils may break down in the presence
23 of chemical, thermal or enzymatic action (Baldwin et al., 2011; Chernoff et al., 1995; Glover and
24 Lindquist, 1998; Knowles et al., 2007; Shammas et al., 2011; Surmacz-Chwedoruk et al., 2014), and
25 their relative resistance or stability to different stresses, including those associated with physiological
26 changes involved in human disorders, is not known. In particular, understanding how enzymatic
27 action by molecular chaperones such as Hsp104 or ClpB promote amyloid division, degradation

1 and/or propagation of amyloid conformation (Chernova et al., 2017; Scior et al., 2016) in relevant
2 cases may be key in resolving the complex behaviour of the amyloid lifecycle in a biological context.
3 In summary, the combined theoretical and experimental work we report here will enable the
4 characterisation and comparison of the amyloid division processes and the relative stabilities of
5 amyloid assemblies. Both properties are fundamental in understanding the lifecycle of disease-
6 associated amyloid as well as the normal roles of functional amyloid in biology.

7

8

9 **LIMITATIONS OF THE STUDY**

10

11 The division model (assumptions illustrated in **Fig. 1**) does not take into account the possibilities that
12 newly created fibril ends by division may be more dynamic, disordered, and/or being ‘sticky ends’ in
13 their interactions with other fibril ends or surfaces compared with established fibril ends for
14 elongation. The results reported here reveal the overall breakage behaviour of the fibril populations,
15 as our experiments may contain a mixture of similar but nevertheless different polymorphs that could
16 not be readily distinguished in our images. Future advances in AFM imaging allowing either
17 individual polymorphs in a fibril population to be distinguished or individual fibrils to be tracked in
18 real-time will resolve breakage behaviour of individual fibril polymorphs. The model assumptions
19 and limitations may also leave scope for improvements in the model to be pursued in future work by
20 the field.

21

22

23 **RESOURCE AVAILABILITY**

24

1 Lead contact

2 Wei-Feng Xue (w.f.xue@kent.ac.uk).

3

4 Materials availability

5 This study did not generate new unique reagents

6

7 Data and code availability

8 The published article includes all datasets generated and analysed during this study. List of all (over
9 220 000) raw fibril lengths and associated analysis code supporting the current study are available
10 from the corresponding author on request.

11

12

13 MATERIAL AND METHODS

14

15 All materials and methods can be found in the accompanying Transparent Methods supplemental file

16

17

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19

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5

6

7 **AUTHOR CONTRIBUTIONS**

8

9 D.M.B. designed the research, conducted the experiments, and analysed the data. M.T. designed the
10 research, developed the theory, wrote the analytical software tools, and analysed the data. R.M. and
11 T.J.P. conducted the experiments. D.P.S. provided reagents and methods, and analysed the data.
12 M.F.T. designed the research and analysed the data. M.D. designed the research, developed the theory
13 and analysed the data. W.F.X. designed the research, wrote the analytical software tools, developed
14 the theory, analysed the data, and managed the research. The manuscript was written through
15 contributions of all authors.

16

17

18 **DECLARATION OF INTERESTS**

19 The authors declare no conflicts of interest.

20

21

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- 13
- 14

1 **FIGURE LEGENDS**

2

3 **Figure 1. Schematic illustration of fibril division in the amyloid lifecycle.** (a) The lifecycle of
4 amyloid assembly where soluble monomeric protein (circles) are converted into the amyloid state
5 with a cross- β conformation (the parallelograms). The coloured arrows represent the four main
6 processes in amyloid assembly. Red arrows represent primary nucleation, which may occur as
7 homogeneous nucleation in solution, heterogeneous nucleation at interfaces. Primary nucleation may
8 also occur subsequent to liquid-liquid phase separation or phase transitions (Khan et al., 2018).
9 Purple arrows represent secondary nucleation, which may occur as heterogeneous nucleation at
10 surfaces presented by preformed aggregates. Blue arrows represent growth by elongation at fibril
11 ends. Yellow arrows and box represent fibril division (e.g. fibril fragmentation or breakage). The
12 arrows may represent consecutive reversible steps and the thickness of the arrows symbolizes the
13 relative rates involved in the processes. (b) A simple model of fibril division, where a given parent
14 fibril particle of length y divides to give rise to two daughter fibril particles of size x and $y-x$. The
15 model does not otherwise identify the lineage of the individual fibrils. (c) The division model assumes
16 that each parent fibril particle divides into exactly two daughter particles at each microscopic
17 reaction step. (d) The division model assumes that the division rate for each microscopic step is
18 identical as long as the resulting two particles have the same size.

19

20 **Figure 2. AFM imaging of amyloid fibrils undergoing fragmentation promoted by mechanical**
21 **stirring.** Hen egg white Lyz, bovine milk β -Lac, and human α -Syn amyloid fibril samples (all 120 μ M
22 monomer equivalent concentration) were stirred for up to 15 days. Samples were taken out
23 periodically, deposited on mica and imaged using AFM. Typical AFM images representing 10x10 μ m
24 surface areas are show together with 4x magnified insets. The scale bar represents 2 μ m in all
25 images.

1

2 **Figure 3. Fibril length and height distributions extracted from AFM images of the fibril**
 3 **undergoing fragmentation by mechanical perturbation.** Normalised length (upper row of each
 4 sample) and height (lower row of each sample) distributions of fibril particles corresponding to the
 5 same AFM images in Fig. 2 are shown as histograms. The histograms are shown using the same
 6 length and height scales, respectively, for comparison.

7

8 **Figure 4. Illustration of the key insights emerging from the mathematical analysis of the division**
 9 **model.** The behaviour of the division equation Eq. (1) is entirely and uniquely dictated by a set of
 10 three properties: α , γ and κ_0 . Several key predictive insights emerged from the analytical solution of
 11 Eq. (1) with regard to these three properties. (a) The three example length distributions in the left
 12 panel can be rescaled to show the same distribution shape in the right panel, illustrating the concept
 13 of self-similar length distributions. (b) After a period of time, where the self-similar length
 14 distribution shape is reached. From this point, the reduction in the average length of the fibril length
 15 distribution can be described as a power law versus time. The decay of mean length of a sample is
 16 predicted to tend towards a straight line, the asymptotic line, when plotted on a log-log plot with the
 17 slope of the line representing $-1/\gamma$ (black line in b, d and e). The stability line with mean fibril lengths
 18 also does not depend on the initial length distribution (coloured lines in b). (c) The self-similar length
 19 distribution shape contains information about κ_0 , which describes how likely a fibril will divide in the
 20 middle versus shedding a small fragment from the edge. A κ_0 indicative of fibril types that are more
 21 likely to divide in the middle will result in fibril length distributions with a distinct peak and low
 22 relative population of small fragments (dark green and light green curves). In contrast, κ_0 indicative
 23 of fibril types and conditions that promote equal likelihood of division along the fibril or even favour
 24 shedding of small fragments from fibril edges will result in self-similar fibril length distributions that
 25 have a larger relative population of small fibril fragments (yellow and orange curves) compared to κ_0
 26 values favouring division in the centre of the fibrils. (d) and (e) illustrate how the black asymptotic

1 line describing the decay of fibril lengths in (a) is dictated by the parameters α and γ , respectively.
2 For each panel, the colour bar to the right illustrates the different properties associated with the
3 colours in the panel (e.g. division in the centre vs. at the edge of a fibril for panel c, and division of a
4 long vs. a short fibril in panel e)

5
6 **Figure 5. Fitting the fibril division model to fibril length decay data extracted from AFM images.**

7 The analytical solution of our division model shows the decay of average length as function of the
8 gamma parameter in equation Eq. (2) and Eq. (4). Equation Eq. (4) was fitted to the decay of average
9 fibril length during division for each of the fibril types analysed (including previously published data
10 for β_2m fragmentation under the same mechanical perturbation conditions in Xue and Radford,
11 2013). The solid fitted lines represent the time regime where the length distributions closely
12 approached the stability line and the self-similar distribution shape where Eq. (2) is valid (Materials
13 and Methods).

14
15 **Figure 6. Comparing the stability towards division of different amyloid fibril types.** The decay of
16 mean lengths (a), the division rate constants as function of fibril length (b), and the self-similar length
17 distribution shapes (c) for hen egg Lyz (blue), bovine milk β -Lac (yellow), human α -Syn (red) and
18 human β_2m (black, data from Xue and Radford, 2013) amyloid fibril samples undergoing division by
19 fibril fragmentation under mechanical perturbation. All curves were calculated using α , γ , and $g(x_g)$
20 obtained from our analysis of the experimental AFM images. In (a), the thicker portion of the lines
21 denote the time range where the characteristic self-similar length distribution shape is observed in the
22 imaging experiments (i.e. corresponding to the time regime represented by the solid fitted lines in Fig.
23 5), and crosses are the experimental data points that have closely reached the self-similar distribution
24 shapes shown in the same plot. In (b), the thicker portion of the lines denote the range of fibril lengths
25 observed experimentally on the AFM images. In (c), the distributions were calculated using self-
26 similar distributions $g(x_g)$ in **Supplementary Fig. S3** after two weeks.

1

2 **Figure 7. Validation of the division parameters α , γ and κ_0 and their predictive power.** Full direct
 3 simulation of fibril fragmentation processes using α , γ and κ_0 determined from the image data. For
 4 each fibril type, the initial normalised frequency distribution (dashed lines in top row) were used
 5 directly as the initial state for the simulations. The resulting simulated evolution of length
 6 distributions solely based on the calculated α and γ values and estimated shapes κ_0 (see Materials
 7 and methods) are compared with the experimental data show as histograms.

8

9 **Figure 8. Schematic summary of the fibril division properties and their consequences compared**
 10 **between each of the fibril types.** Comparison of the fibril division profiles reveal differences in the
 11 dynamical stability towards breakage for the four different types of amyloid fibrils, and suggest that
 12 disease-related amyloid has lowered stability towards breakage and increased likelihood of shedding
 13 smaller particles compared to amyloid not related to disease. In the illustrations, the fibril width,
 14 number and number of breakage symbols are not to scale and denote the relative rankings for the
 15 different properties.

16

17

18

19 **TABLES**

20

21 **Table 1.** Parameters from the division analysis of the different fibril types

<i>Sample</i>	$\gamma \pm SE$	$\alpha / nm^{-1} (\log \alpha \pm SE)$	$B (100 nm) / s^{-1} (\log B \pm SE)$	<i>Height (fibril width) / nm</i>

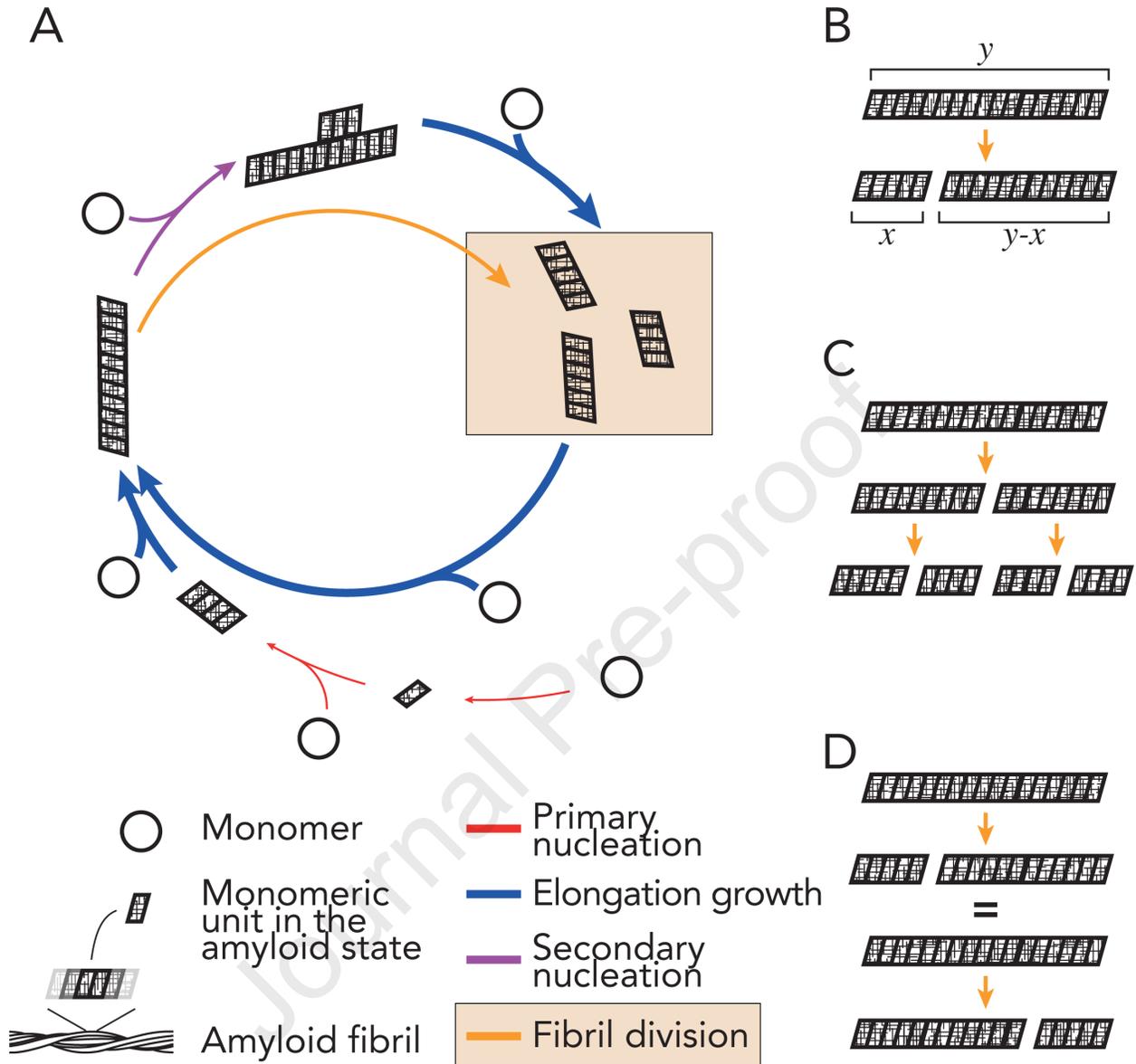
<i>α-Syn</i>	2.0 ± 0.3	$2.6 \cdot 10^{-6} (-5.6 \pm 0.2)$	$9.2 \cdot 10^{-8} (-7.0 \pm 0.3)$	6.8 ± 0.6
<i>β-Lac</i>	5.7 ± 0.8	$1.8 \cdot 10^{-4} (-3.7 \pm 0.2)$	$1.2 \cdot 10^{-10} (-9.9 \pm 0.8)$	3.0 ± 0.5
<i>Lyz</i>	1.7 ± 1.0	$9.4 \cdot 10^{-7} (-6.0 \pm 0.9)$	$2.0 \cdot 10^{-7} (-6.7 \pm 1.0)$	3.1 ± 0.4
<i>β_2m^*</i>	3.4 ± 0.4	$5.6 \cdot 10^{-5} (-4.3 \pm 0.3)$	$2.5 \cdot 10^{-8} (-7.6 \pm 0.4)$	5.4 ± 0.6

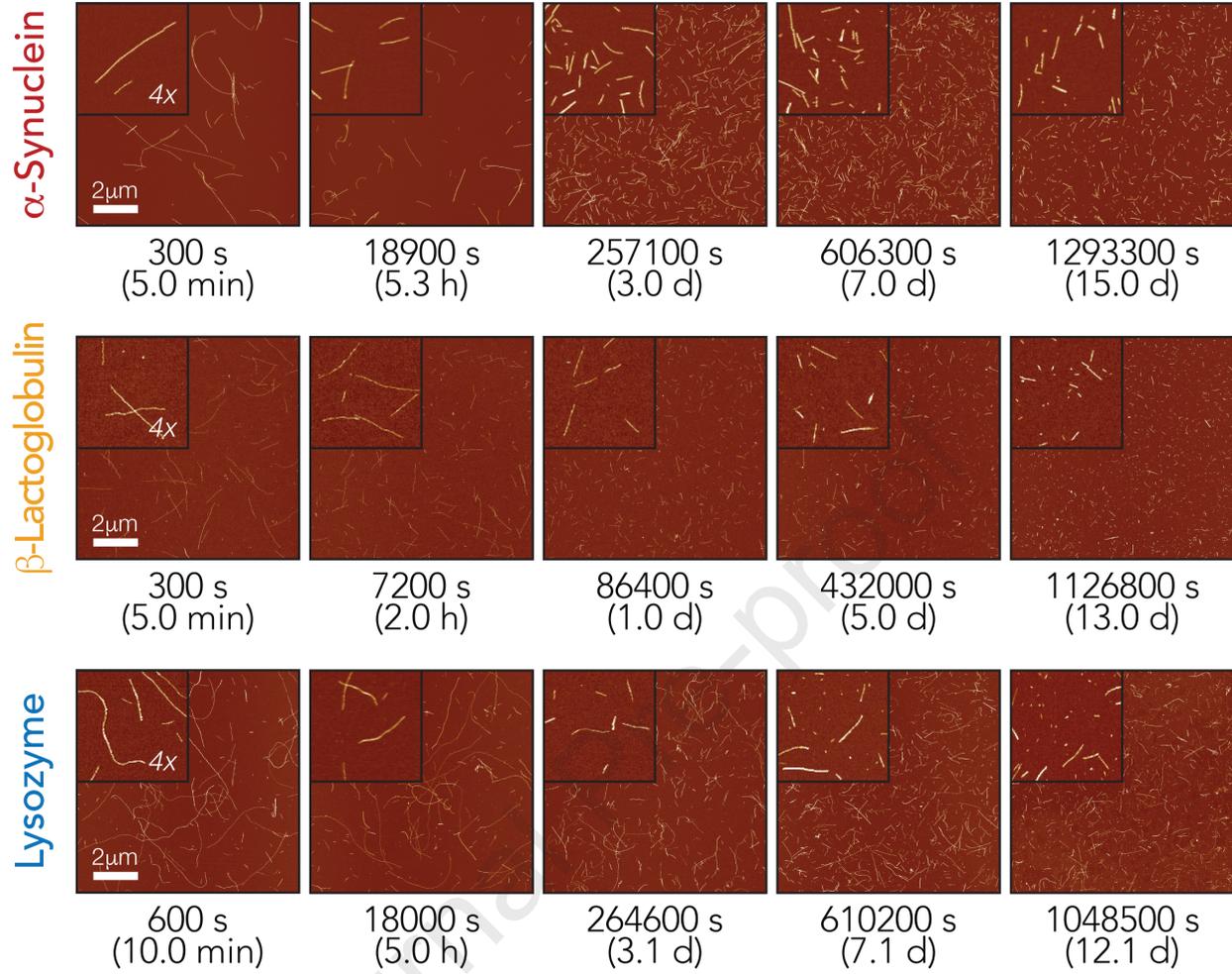
1 * Reanalysis of data from Xue and Radford, 2013.

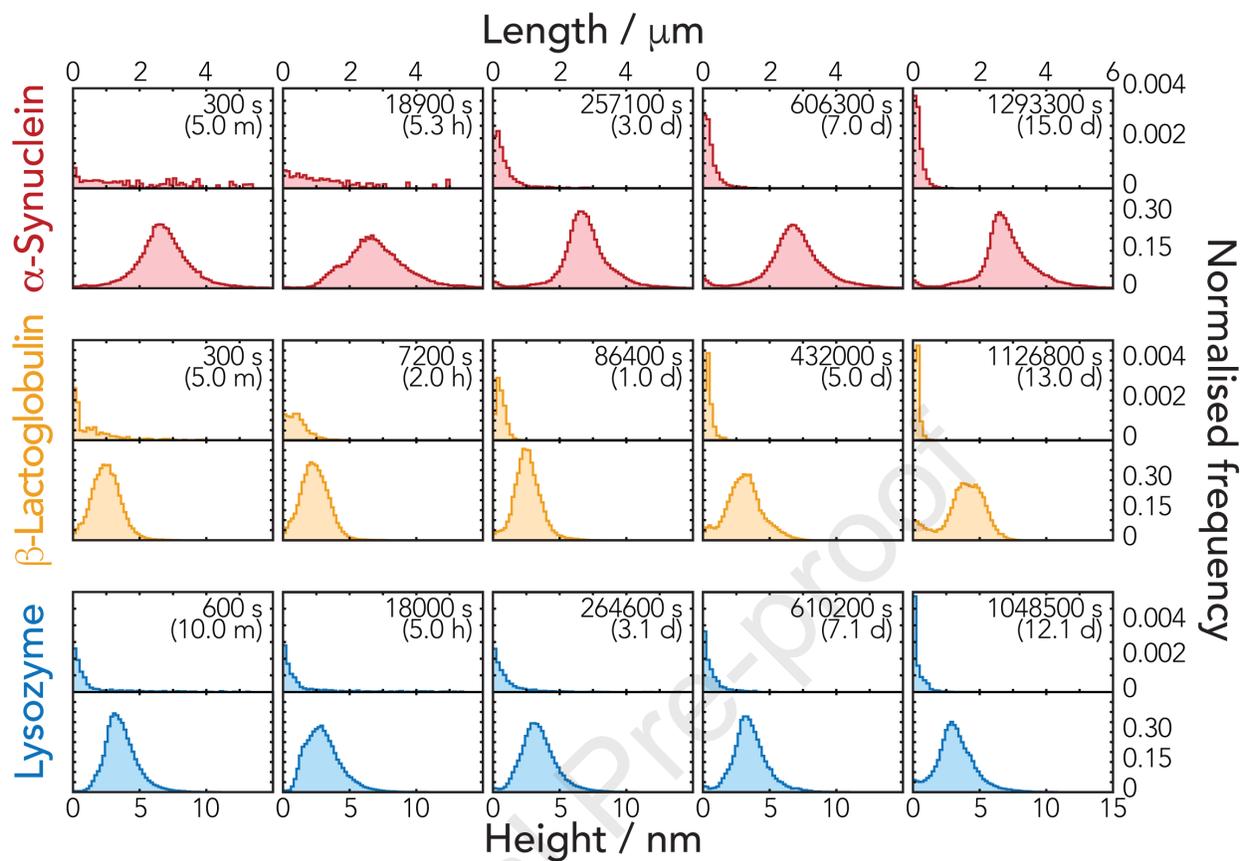
2

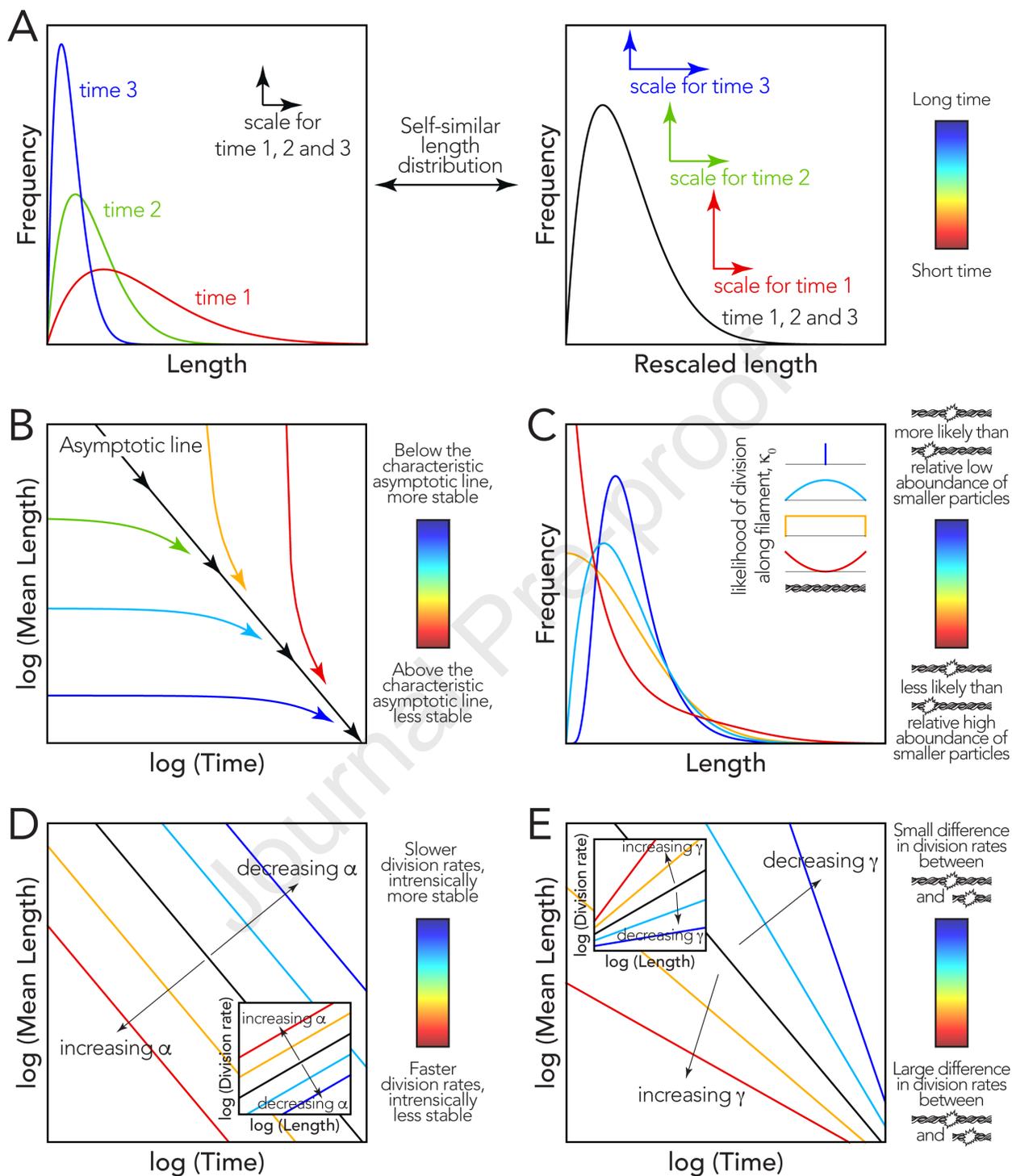
3

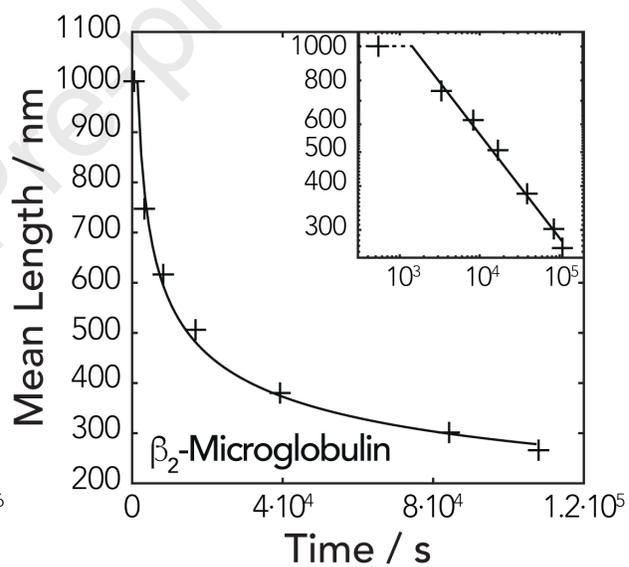
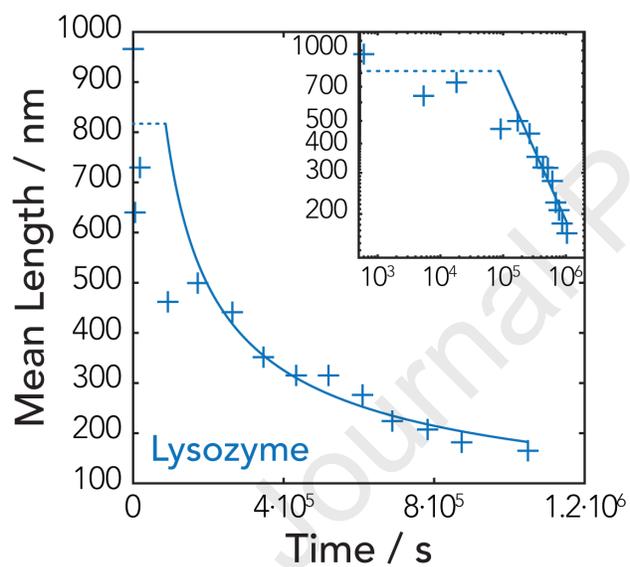
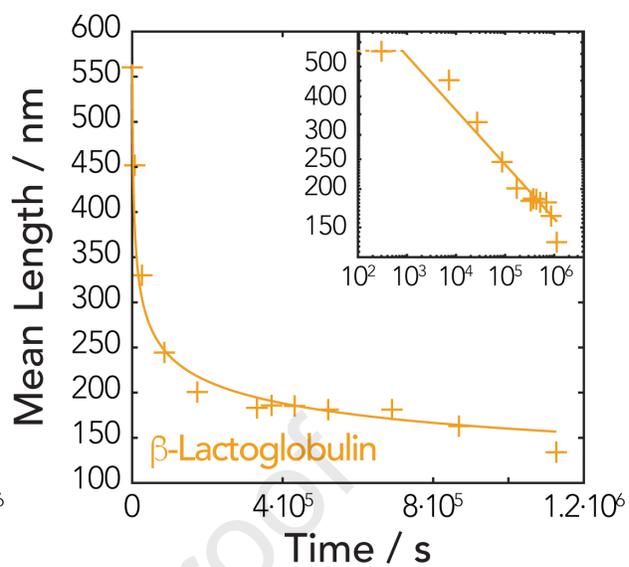
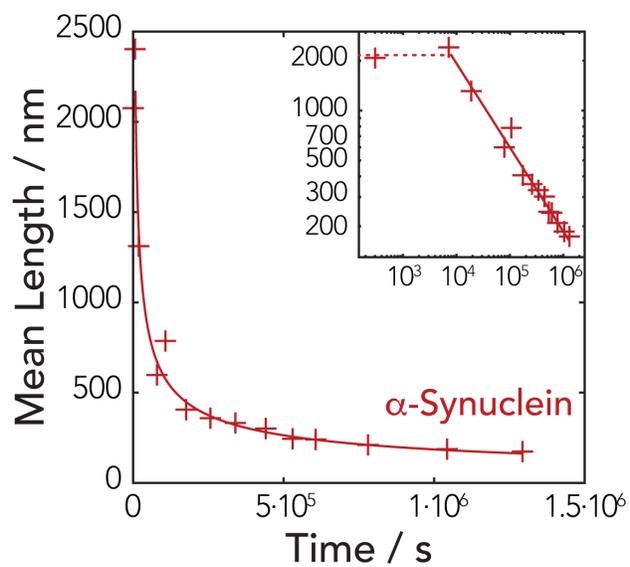
Journal Pre-proof

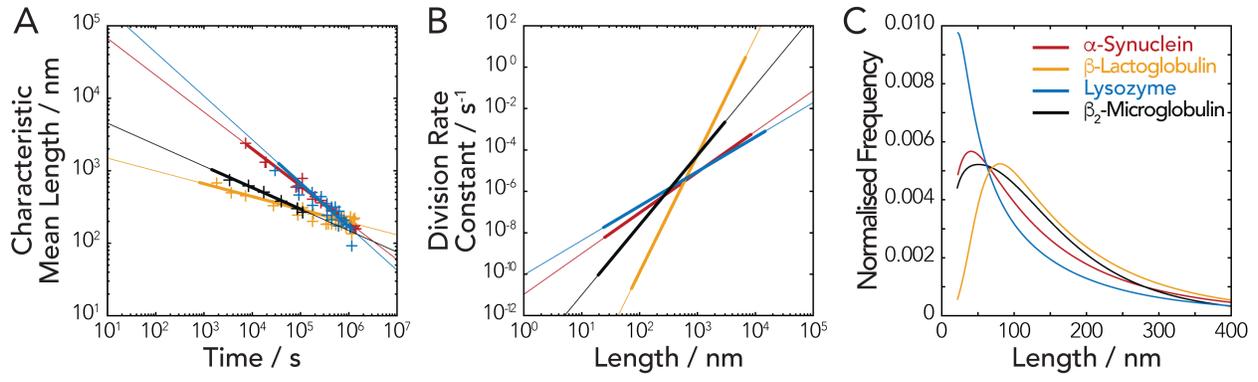




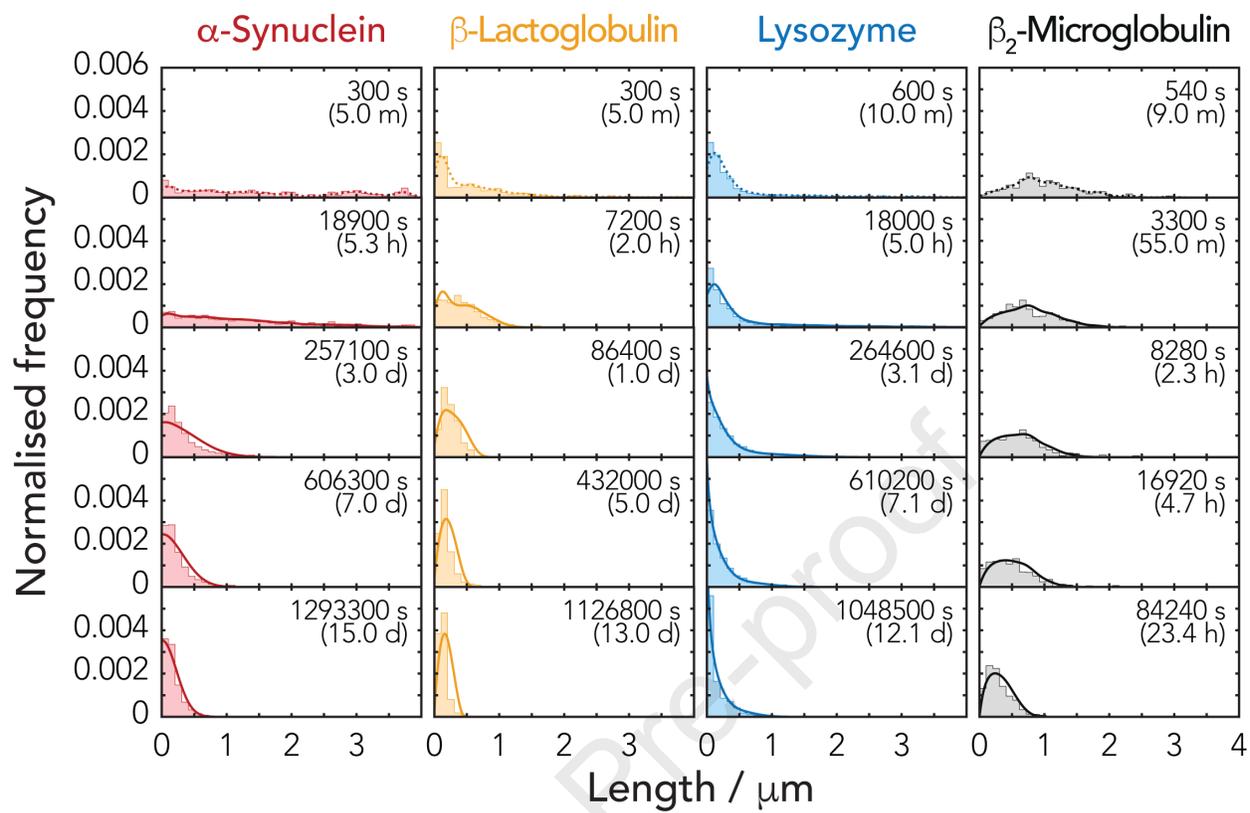








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	α -Synuclein	β -Lactoglobulin	Lysozyme	β_2 -Microglobulin
Filament width and cross-sectional area				
Division rate ($B = \alpha v$) for particles ~ 100 nm or shorter				
Length dependence of the division rate (γ)	$\gamma_{center} < \gamma_{edge}$		$\gamma_{center} < \gamma_{edge}$	$\gamma_{center} < \gamma_{edge}$
Likelihood of division at filament centre vs edge (κ_v)	$\kappa_{center} \approx \kappa_{edge}$	$\kappa_{center} > \kappa_{edge}$	$\kappa_{center} \approx \kappa_{edge}$	$\kappa_{center} \approx \kappa_{edge}$
Characteristic mean fibril length at long timescale ($>$ days)				
Relative abundance of particles ~ 100 nm or shorter				
Overall filament stability				

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HIGHLIGHTS

- Theory on the division of amyloid fibrils developed using a continuous PDE framework
- The theory allowed direct analysis of fibril breakage properties with AFM image data
- The new insights enabled comparison of fibrils' intrinsic stability to breakage
- α -synuclein fibrils showed low stability to division compared to other model amyloid