

Application of Bousinesq's and Westergaard's formulae in analysing foundation stress distribution for a failed telecommunication mast

OJEDOKUN, Olalekan http://orcid.org/0000-0002-9573-4976 and OLUTOGE, Festus Adeyemi

Available from Sheffield Hallam University Research Archive (SHURA) at:

https://shura.shu.ac.uk/24796/

This document is the Published Version [VoR]

Citation:

OJEDOKUN, Olalekan and OLUTOGE, Festus Adeyemi (2012). Application of Bousinesq's and Westergaard's formulae in analysing foundation stress distribution for a failed telecommunication mast. African Journal of Mathematics and Computer Science Research, 5 (4), 71-77. [Article]

Copyright and re-use policy

See http://shura.shu.ac.uk/information.html

Full Length Research Paper

Application of Bousinesq's and Westergaard's formulae in analysing foundation stress distribution for a failed telecommunication mast

OJEDOKUN Olalekan Yinka^{1*} and OLUTOGE Festus Adeyemi²

¹Department of Civil Engineering, Faculty of Engineering, the Polytechnic, Ibadan, Oyo State, Nigeria. ²Department of Civil Engineering, Faculty of Engineering, University of Ibadan, Oyo State, Nigeria.

Accepted 23 January, 2012

The concurrent foundation failure of telecommunication masts in Nigeria and all over the world which endanger the lives and properties of residents situated within the fall distance of the telecommunication mast is a thing of great concern. In this study, a GSM mast that underwent foundation failure at Ibadan, Oyo State, Nigeria was critically examined with a view to providing engineering solution. The soil investigation at the global system for mobile communications (GSM) telecommunication tower comprised of laboratory tests: sieve analysis, Atterberg limits and moisture content tests were carried out on the soil samples obtained while Dutch cone penetrometer test was performed on the site to a depth of refusal to determine the allowable bearing pressure at various depths of the soil. The application of Boussineq's and Westergard's formulae for point loads using Java programme to simulate and compute the stress distribution at various predetermined depths showed the stress distribution pattern beneath the failed foundation of the structure. The stress distribution pattern revealed that the soil strength was lower than the imposed loadings from the structure thereby resulting in differential settlements and cracks at the foundation. A variety of engineering solutions were recommended to improve the soil strength and thus prevent such occurrences in future.

Key words: Telecommunication mast, Bousinesg's and Westergraard's formula, stress distribution.

INTRODUCTION

A telecommunication mast installation comprises of a mast supporting telecommunications antenna and a foundation structure supporting the mast, the foundation structure being in the form of an enclosed chamber situated at least partially underground and defining an internal space which is accessible to personnel and which accommodates electronic equipment associated with operation of the antenna. The telecommunication mast has a foot at its lower end which is supported on a base of the chamber, the base acting as a structural foundation for the mast. The foot of the mast is seated on the base, the seat restraining lateral movements of the foot of the mast at the base without transfer of bending

moments between the mast and the foundation structure (Creighton, 2002).

Numerous investigations have been carried out on the design and erection techniques of telecommunication towers. Comparatively little attention has been directed toward the behaviour and deterioration of tower foundations. It should be pointed out that the design of tower foundations is more involved than that of other steel structures. In the latter case, the foundations are usually subjected to static compressive force with uniform stress distribution on soil (Abdalla, 2002).

Communication masts are used for all types of wireless communication and come in many different shapes and sizes. From a structural point of view, a lattice construction has been shown to provide a strong durable structure upon which to locate antennae of different types and size. However, many people consider lattice

^{*}Corresponding author. E-mail: daniely2kus@yahoo.com.

constructions to be unattractive and in the recent past this has resulted in slim tubular constructions being utilized in order to reduce the visual impact of the mast (Heslop, 2002).

In an engineering sense, failure may occur long before the ultimate load or the load at which the bearing resistance of the soil is fully mobilized since the settlement will have exceeded tolerable limits. Terzaghi (1967) suggested that, for practical purposes, the ultimate load can be defined as that which causes a settlement of one-tenth of the pile diameter or width which is widely accepted by engineers. In most cases where the piles are acting as structural foundations, the allowable load is governed solely from considerations of tolerable settlement at the working load. An ideal method of calculating allowable loads on piles would be one which would enable the engineer to predict the loadsettlement relationship up to the point of failure, for any given type and size of pile in any soil or rock conditions (Tomlinson, 1994).

Estimation of vertical stresses at any point in a soilmass due to external vertical loadings is of great significance in the prediction of settlements of buildings, bridges, embankments and many other structures. Equations have been developed to compute stresses at any point in a soil mass on the basis of the theory of elasticity. According to elastic theory, constant ratios exist between stresses and strains. For the theory to be applicable, the real requirement is not that the material necessarily be elastic, but there must be constant ratios between stresses and the corresponding strains. Therefore, in non-elastic soil masses, the elastic theory may be assumed to hold so long as the stresses induced in the soil mass are relatively small. Since the stresses in the subsoil of a structure having adequate factor of safety against shear failure are relatively small in comparison with the ultimate strength of the material, the soil may be assumed to behave elastically under such stresses. When a load is applied to the soil surface, it increases the vertical stresses within the soil mass. The increased stresses are greatly directly under the loaded area, but extend indefinitely in all directions. Many formulae based on the theory of elasticity have been used to compute stresses in soils. They are all similar and differ only in the assumptions made to represent the elastic conditions of the soil mass. The formulae that are most widely used are the Boussinesq and Westergaard formulas (Murthy, 1992).

METHODOLOGY

Collection of samples

The soil investigation at the GSM telecommunication tower at Ibadan, Oyo State, Nigeria comprised of and was carried out in three parts; field work: (tests two boreholes), laboratory analysis of borehole samples obtained and analysis of the test results. The scope of work executed involved the performance of two boreholes

to depth of refusal. The samples obtained from the borehole test were also subjected to laboratory analysis. The laboratory tests carried out on the samples are: grain size analysis, moisture content, atterberg limits, dutch cone penetrometer tests.

Pile details

Mass of tower ad ladder, W = 12796 Kg
Height of tower, Ht = 55 m

Maximum force/leg, Rv = 524.43 kN

Maximum uplift/leg, Wv = -461.67 kN

Leg spacing heal-heal = 6502 mm

R.C. Stud section = 700 × 700 mm

Load factor = 1.3

Safe working loads

Pile depth, Lp = -6.00 m

Pile requirement

Piles required/leg = Max forces per leg/(Qs + Qb)

300 mm = 524.43/108 = 4.8558333 ~ 5No 400 mm = 524.43/182 = 2.8814835 ~ 3No

Provision per leg 400 mm = 3No

Load per pile

Wp = 174.81 kN Wp (factored) = 174.81 x 1.3 = 227.253 KN

Pile design

Designed as a short braced column min. steel required = 0.4%ACol

 $Acol = (3.142 \times 400^2) / 4 = 125680 \text{ mm}^2$

 $Ast = (0.4 \times 125680) / 100 = 502.72 \text{ mm}^2$

Provide = 6 No. 16 mm diameter bar

 $Asc(pro) = 1206 \text{ mm}^2$

Load capacity N = 0.35 Fcu x Acol + 0.67Ast x Fy N = 0.35 x 25 x 125680 + 0.67 x 1206 x 380 N = 1406.70kN

RESULTS AND DISCUSSION

Physical properties of soil samples

The analysis of total load to be carried by the piles is presented in Table 1. The results of the tests carried out on the soil specimens are given in Table 2. Sample 4 had

the highest value of plastic and liquid limits while samples 1, 3, 5, 7 and 8 had no plastic and liquid limits. Generally, liquid limits vary widely, but values of 40 to 60% and above are typical of clay soils and values of 25 to 50% can be expected for silty soil so clays soils with liquid limits between 30 and 50% exhibit medium plasticity while liquid limits less than 30% infer low plasticity and liquid limits greater than 50% indicate high plasticity. High liquid limit is an indication of soils with high clay content and low bearing capacity.

Sample 8 had the highest moisture content which indicated poor drainage property while sample 1 had the lowest moisture content indicating that the drainage property is good at that depth.

Allowable bearing pressure at predetermined depths

The allowable bearing capacity at predetermined depths were determined for borehole 1 and tabulated in Table 3.

The highest bearing capacity of the soil which was at 7.50 m depth was 220 kN/m². The derived allowable bearing capacity of the soil in relationship to the actual load of the telecommunication mast would be used in the simulation using Java programme to determine the cause of failure.

Application of Bousinesq's formula for stress distribution

$$\sigma_{B} = \frac{3N}{2 \Pi Z^{2}} \frac{1}{[1 + (r/Z)^{2}]^{5/2}} = \frac{N I_{B}}{Z^{2}}$$

$$I_{B} = \frac{3}{2 \Pi \left[1 + (r/Z)^{2}\right]^{5/2}}$$

Where σ_B = Bousinesq stress coefficient

I_B = Bousinesq vertical stress

N = Point load from the end bearing pile

Z = Vertical distance from the end point of pile

r = The radial distance from Z (Murthy, 1992).

Application of Westergaard's formula for stress distribution

$$\sigma_W = \; \frac{N}{\Pi Z^2} \; \frac{1}{[1 + 2(r/Z)^2]^{3/2}} \; = \frac{N \; I_W}{Z^2} \label{eq:sigmaW}$$

$$I_{W} = \frac{(1/11)}{[1 + 2(r/Z)^{2}]^{3/2}}$$

Where σ_W = Westergaard stress coefficient I_W = Westergaard vertical stress N = Point load from the end bearing pile Z = Vertical distance from the end point of pile r = Radial distance from Z (Murthy, 1992).

Stress distribution at predetermined depths

Based on the Bousinesq's and Westergaard's formulae stated, the Java coding for determining the various stresses at predetermined depths was used to analyse the experimental data. The result of the analysis is shown in Table 4.

Figure 1: Graph of values of I_B and I_W showed the values obtained from the Table 4: Stress distribution at predetermined depths when I_B and I_W were plotted against r/z. The graph (Figure 1) showed that both Bousinesq vertical stress and Westergaard vertical stress decreased as the depths moves further away from the point load. In other words, as the values of radial and vertical distances increased, both values of Bousinesq vertical stress and Westergaard vertical stress decreased.

Figure 2: Graph of values of σ_B and σ_W showed the values obtained from the Table 3: Stress distribution at predetermined depths when σ_B and σ_W were plotted against r/z. The graph (Figure 2) showed that both Bousinesq vertical stress coefficient and Westergaard vertical stress coefficient decreased as the depths moved further away from the point load. In other words, as the values of radial and vertical distances increased, both values of Bousinesq Vertical Stress and Westergaard Vertical Stress decreased.

Figure 3: Graph of values of σ_B/σ_W showed the values obtained from the Table 4: Stress distribution at predetermined depths when σ_B/σ_W is plotted against r/z. The graph (Figure 3) showed that σ_B/σ_W decreased as the depths moved further away from the point load. In other words, as the values of radial and vertical distances increased, σ_B/σ_W decreased.

Conclusion

From the analysis of the results obtained from *in-situ* and laboratory tests carried out on the soil samples at the telecommunication mast site, the following conclusions can be drawn.

(1) The telecommunication mast was erected at a distance of two metres to the nearby building thereby violating the Nigerian Communication Commission guidelines of observing a clear fall distance to any nearby building.

The stress distribution at predetermined depths revealed:

Table 1. Load classification on piles.

Pile diameter (mm)	End bearing, Qb (kN)	Skin friction, Qs (kN)	Total load {Qb (kN) +Qs(kN)}
300	84	24	108
400	150	32	182

Table 2. Physical properties of soil samples.

BH number	Sample number	Debin (m)	Soil type	Natural moisture content (%)	Atterberg limits (%)		Grading analysis percentage passing											
					LL	PL	PI	9.5	6.3	4.75	2.36	1.18	600	425	300	212	150	75
	1	0.15	SM	13							100	98	89	80	75	61	48	34
	2	2.25	SC	17	44	18	26				100	97	88	80	71	65	55	48
1	3	3.75	SC	16							100	97	88	80	71	61	54	47
	4	5.25	SC	19	46	19	27				100	98	92	85	77	67	58	49
	5	7.50	GP/SM	20				85	81	80	72	67	56	48	41	34	29	23
	6	0.75	SM/SC	18	31	13	18		100	99	96	90	77	68	59	48	41	34
0	7	3.00	SM/SC	18						100	98	94	81	69	58	47	39	32
2	8	6.00	SC	23					100	99	98	94	83	74	66	57	50	45
	9	8.25	SC	16	45	17	28			100	99	93	81	73	66	58	53	48

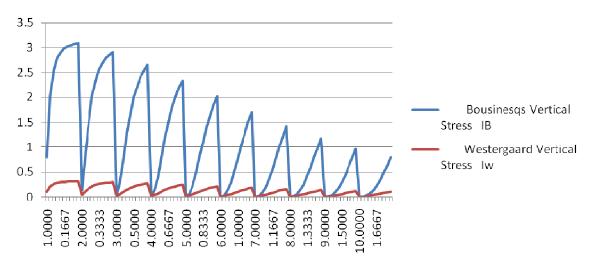


Figure 1. Graph of I_B and I_W.

 Table 3. Allowable bearing pressure at predetermined depths.

Depth (m)	Allowable bearing pressure (kN/m²)
0.00 - 0.15	50
0.15 - 2.25	108
2.25 - 3.75	140
3.75 - 5.25	190
5.25 - 7.50	220

 Table 4. Stress distribution at predetermined depths based on Java coding.

Radial distance, r(m)			Bousnesq's stress coefficient, σ _B (N/m²)	Westergaard vertical stress (I _w)	Westergaard stress coefficient, σ _w (N/m²)	$\sigma_{\text{B}}/\sigma_{\text{w}}$		
1	1	1.0000	0.7854	1104745.006	0.1061	149245.4289	7.4022	
1	2	0.5000	2.0106	2828147.216	0.2122	298490.8577	9.4748	
1	3	0.3333	2.5447	3579373.82 0.2604 366329.689		366329.689	9.7709	
1	4	0.2500	2.7829	3914390.61	0.2829	397987.8103	9.8355	
1	5	0.2000	2.9046	4085595.437	0.2947	414570.6357	9.855	
1	6	0.1667	2.9741	4183344.129	0.3016	424171.2189	9.8624	
1	7	0.1429	3.0172	4243988.416	0.3058	430178.0009	9.8657	
1	8	0.1250	3.0457	4284057.321	0.3087	434168.5203	9.8673	
1	9	0.1111	3.0654	4311857.219	0.3106	436947.4604	9.8681	
1	10	0.1000	3.0797	4331908.661	0.3121	438957.1437	9.8686	
2	1	2.0000	0.1257	176759.201	0.0354	49748.4763	3.5531	
2	2	1.0000	0.7854	1104745.006	0.1061	149245.4289	7.4022	
2	3	0.6667	1.5057	2117972.675	0.1685	237036.8576	8.9352	
2	4	0.5000	2.0106	2828147.216	0.2122	298490.8577	9.4748	
2	5	0.4000	2.3347	3284022.016	0.2411	339194.1565	9.6818	
2	6	0.3333	2.5447	3579373.82	0.2604	366329.689	9.7709	
2	7	0.2857	2.6853	3777134.582	0.2736	384896.106	9.8134	
2	8	0.2500	2.7829	3914390.61	0.2829	397987.8103	9.8355	
2	9	0.2222	2.8529	4012861.999	0.2897	407490.3283	9.8477	
2	10	0.2000	2.9046	4085595.437	0.2947	414570.6357	9.855	
3	1	3.0000	0.0314	44189.8002	0.0168	23565.0677	1.8752	
3	2	1.5000	0.2974	418364.9728	0.0579	81406.5976	5.1392	
3	3	1.0000	0.7854	1104745.006	0.1061	149245.4289	7.4022	
3	4	0.7500	1.2868	1810014.218	0.1498	210699.429	8.5905	

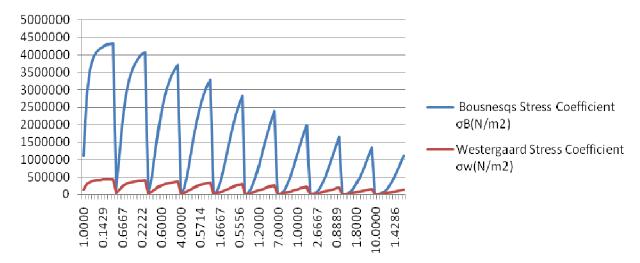


Figure 2. Graph of σ_B and σ_W .

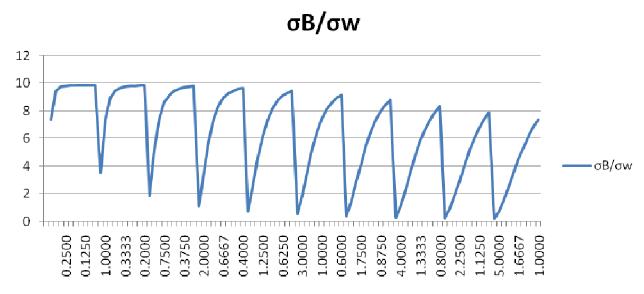


Figure 3. Graph of σ_{B}/σ_{W} .

- 1) Bousinesq vertical stress, Westergaard vertical stress, Bousinesq vertical stress coefficient and Westergaard vertical stress coefficient decreased as the depths moved further away from the point load. In other words, as the values of radial and vertical distances increased, the values of Bousinesq vertical stress, Westergaard vertical stress, Bousinesq vertical stress coefficient and Westergaard vertical stress coefficient decreased.
- 2) The total weight of the structure transmitted by the end bearing of the pile foundation unto the soil which is 389.47 kN/m² in relationship to the soil bearing capacity at the depth of the pile foundation which is 220 kN/m² has caused a differential settlement to occur at the foundation. This differential settlement has resulted to cracks occurring at the pile caps and also a clearance at

the base plate which would eventually result to a total collapse if not attended to.

Based on the conclusions arrived at, the following recommendations could be adopted;

- 1) The telecommunication mast should be dismantled because it violated the Nigeria Communication Commission guidelines for safe erection of telecommunication mast of observing a clear fall distance.
- 2) The soil bearing pressure could be improved by adopting any of the following soil improvement methods: Application of vertical or wick drains, vacuum consolidation, cement deep mixing, vibroflotation techniques, application of geotextiles.

REFERENCES

Abdalla HA (2002). Repair of Cracked Concrete Foundations of Telecommunication Structures. 4th Structural Specialty Conference of the Canadian Society for Civil Engineering, June 5-8.

of the Canadian Society for Civil Engineering, June 5-8.

Creighton BR (2002). Telecommunications mast installation. Free Patents Online, pp. 1-2.

Patents Online, pp. 1-2.
Heslop P (2002). Communications mast. Free Patents Online, Great Britain, pp. 1-2.

Murthy VNS (1992). Principles and Practices of Soil Mechanics and Foundation Engineering, Marcel Dekker Inc., New York, pp. 173-175. Terzaghi K, Peck RB (1967). Soil Mechanics in Engineering. 2nd Edition, John Wiley, New York.

Tomlinson MJ (1994). Foundation Design and Construction. Singapore, Longman, pp. 267-268.