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A New Constant Pushing Force Device for Human Walking Analysis

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Abstract—Walking mechanics has been studied for a long time, being essentially simple but nevertheless including quite tricky aspects. During walking, muscular forces are needed to support body weight and accelerate the body, thereby requiring a metabolic demand. In this paper, a new Constant Pushing Force Device (CPFD) is presented. Based on a novel actuation concept, the device is totally passive and is used to apply a constant force to the pelvis of a subject walking on a treadmill. The device is a serial manipulator featuring springs that provide gravity balancing to the device and exert a constant force regardless of the pelvis motion during walking. This is obtained using only two extension springs and no auxiliary links, unlike existing designs. A first experiment was carried out on a healthy subject to experimentally validate the device and assess the effect of the external force on gait kinematics and timing. Results show that the device was capable of exerting an approximately constant pushing force, whose action affected subject’s cadence and the motion of the hip and ankle joints.

I. INTRODUCTION

The metabolic cost of walking is determined by mechanical tasks such as generating force to support body weight, performing work to redirect and accelerate the center of mass from step to step, swinging the limbs, and maintaining stability. Several works have been carried out in order to provide detailed and meaningful analysis on metabolic cost, often making use of external devices which apply some constraints and/or some forces to a walking person. The metabolic cost of plantar flexor muscletendon mechanical work during human walking was examined in [1] using a robotic ankle exoskeleton on both legs. More in detail, the roles of each ankle plantar flexor muscle in providing body support and forward propulsion during human walking were analyzed in [2] carrying out experiments using a harness worn by subjects walking on a treadmill. The metabolic cost and muscular actions required for the initiation and propagation of leg swing were investigated in [3], and the effects of a horizontal propulsive force on the reduction in metabolic cost during normal walking were studied in [4]. Both in [3] and [4] forces were applied using a rubber tubing stretched over low-friction pulleys with a hand winch.

The application of external constraints and/or applied forces during walking can lead to changes in human motion. Moreover, added weight and inertia can influence human motion as well. Hence, it is important to quantitatively estimate their effect. A novel tethered pelvic assist device was used in [5] to study motor adaptation in human walking with externally applied forces on the pelvis, with no added mass and inertia. As the system was passive, the applied force was configuration dependent. Influencing human motion is desirable in some cases, as in the motor rehabilitation of stroke survivors. Effects obtained from treadmill training with force perturbations on overground walking in patients with incomplete spinal cord injury were investigated in [6]. Many examples of robotic gait trainers for motor rehabilitation of neurologically impaired subjects have been developed in the past, such as the Lokomat [7], the ALEX I, II and III [8], [9], [10], the LOPES [11] and the SPARKy [12].

In this paper, the design of a new Constant Pushing Force Device (CPFD) is presented. It consists of a passive serial manipulator exploiting a novel actuating technique based on extended gravity balancing techniques using springs [13], which makes the device extremely simple and lightweight. It was designed to analyze the effect of a constant horizontal force, pushing the pelvis of a subject walking on a treadmill, in terms of gait adaptation. The exerted force is easily adjustable and is theoretically constant regardless of the configuration of the manipulator, which is gravity balanced at the same time.

The paper is organized as follows. In Section II, gravity balancing principles are described, and the idea of actuation derived by such technique is presented. Section III deals with the design of the new device - after stating the design requirements, some possible designs are investigated, thereafter, the chosen system is optimized according to the defined criteria. In Section IV, results from a first experiment aimed to experimentally validate the design are presented, then final conclusions and future perspectives are discussed in Section V.

II. GRAVITY BALANCING AND ACTUATING IDEA

A machine is said to be gravity balanced if no joint actuator inputs are needed to keep the system in equilibrium in any configuration, i.e., the potential energy of the device is invariant. Theoretically, this happens if the centre of mass of the machine is inertially fixed, or if some elastic elements suitably compensate for the variations of the potential energy due to changes of configuration (motion of masses). Several methods of gravity balancing have been proposed over the years, exploiting clever designs that utilize counterweights, springs, cams, auxiliary links [14], [15], [16], [17].
Let us consider a weightless link (Fig. 1(a)) whose length is \( l \), which can rotate about point \( O \), having an attached mass \( m \) at the free extremity. Its configuration is defined by the angle \( \theta \), so it has 1 degree of freedom (dof). This system can be balanced using a zero free length spring whose extremities are connected to the link at point \( Q \) (located at a distance \( b \) from \( O \)) and to the fixed frame at point \( F \), which is vertically aligned with \( O \) and whose distance from \( O \) is \( a \).

![Fig. 1. Single link configuration (a) and 2-dof architecture (b).](image)

The total potential energy \( E \) of the system is \( E = E_m + E_s = mgl \cos \theta + \frac{1}{2} kb^2 \), where \( E_m \) is the contribution of the mass (\( g \) being the gravity acceleration) and \( E_s \) is the contribution of the spring having length \( \delta = \sqrt{a^2 + b^2 - 2ab \cos \theta} \). To ensure the equilibrium for any configuration we set \( \frac{\partial E}{\partial \theta} = 0 \) \( \forall \theta \), thus for fixed \( m, l, a \) and \( b \), the system can be exactly balanced using a zero free length spring having stiffness \( k = \frac{mg}{ab} \). The principle of gravity balancing described above was extended in [13] as a concept of actuation for serial manipulators with any kinematics. In this work, we exploit this idea by defining an additional potential energy term associated to a constant (and therefore conservative) force which a manipulator is requested to exert at the end point. Again, the total potential energy of the system is made to be constant regardless of the system’s configuration. Details on how to apply this method for a specific design problem are presented in the following section.

III. DESIGN OF THE NEW DEVICE

A. Device specifications

The device has to apply a desired pushing force to a subject walking on a treadmill. On one side, the device is connected to a fixed frame. The end point of the device is interfaced with the user, which was chosen to be located at the pelvis. Indeed, the motion of the pelvis has an important role in gait as it assists forward propulsion of the body by transferring forces from the lower extremity to the trunk. It is also crucial in assisting swing initiation and in modulating the vertical displacement of the body center of mass, helping to reduce energy consumption during walking [18], [19].

While walking, the human pelvis has a general 3D motion with nonzero components in all the three spatial directions [20]. The kinematics of the device must therefore be able to follow such general spatial motion. Lastly, it is desirable to design a gravity balanced device, so that no additional weight is added to the walking subject.

B. Design solutions

The device was chosen to be a serial manipulator. In order to be able to follow the 3D translational motion of the attachment point on the pelvis, the device needs \( n \geq 3 \) dof. For the sake of simplicity, we set \( n = 3 \) and the axis of the first joint was chosen to be vertical (directed as gravity), and the remaining part was chosen to be a planar mechanism. Thus, the following analysis will be related to planar 2-dof mechanisms architectures. A spherical joint was mounted at the interface between user and device, to allow the transmission of pure forces to the human pelvis.

![Fig. 2. Architecture 1: gravity balanced (a) and exerting \( F \) (b).](image)

1) Architecture 1: The first architecture analyzed is depicted in Fig. 1(b). The directions of links 1 and 2 are represented by unit vectors \( \vec{x}_1 \) and \( \vec{x}_2 \), while \( \vec{y} \) is a unit vector whose direction is opposite to gravity. Each link has length \( l_i \) and mass \( m_i \), and the position of its center of mass is indicated by \( h_i \).

The design goals of exerting the desired force and balancing gravity can be addressed separately, and the results can be superimposed. In Fig. 2(a) some links and hinges are added to form the parallelogram linkage ABDE. Two zero free-length springs having stiffness \( k_i \) and length \( \delta_i \) are added, each one being the third side of a triangle having sides \( a_i \) directed as \( \vec{y} \) (due to the parallelogram linkage), \( b_i \) directed as link \( i \), and the spring \( k_i \) \( (i = 1, 2) \). The potential energy related to the masses is

\[
E_m = -m_1 \vec{P}_1 \cdot \vec{y} - m_2 \vec{P}_2 \cdot \vec{y},
\]

where \( \vec{P}_1 = h_1 \vec{x}_1 \) and \( \vec{P}_2 = l_1 \vec{x}_1 + h_2 \vec{x}_2 \). Also, \( \vec{y} = -g \vec{y} \), so

\[
E_m = m_1 h_1 \vec{y} \cdot \vec{x}_1 + m_2 l_1 \vec{y} \cdot \vec{x}_1 + m_2 h_2 \vec{y} \cdot \vec{x}_2.
\]

The potential energy related to the springs is

\[
E_s = \frac{1}{2} k_1 \delta_1^2 + \frac{1}{2} k_2 \delta_2^2,
\]

where \( \delta_1^2 = a_1^2 + b_1^2 - 2a_1 b_1 \vec{y} \cdot \vec{x}_1 \). Therefore, the total potential energy is

\[
E_m + E_s = C + (m_1 h_1 + m_2 l_1 - k_1 a_1 b_1) \vec{y} \cdot \vec{x}_1 + (m_2 h_2 - k_2 a_2 b_2) \vec{y} \cdot \vec{x}_2,
\]

where \( C \) is a constant term. Then, in order to have \( \frac{\partial E}{\partial \theta} = 0 \) \( \forall \theta \), it must be \( k_1 = \frac{m_1 h_1 + m_2 l_1}{a_1 b_1} \) and \( k_2 = \frac{m_2 h_2}{a_2 b_2} \). If such conditions are satisfied, the mechanism is gravity balanced.

In Fig. 2(b) some links and hinges are added to the original mechanism (which is now considered massless), as to form
the parallelogram linkage ABFG. As before, two zero free-length springs having stiffness $k_i$ and length $\delta_i$ are added, each one being the third side of a triangle having sides $a_i$, directed as $\vec{y}$ (due to the parallelogram linkage), $b_i$ directed as link $i$, and the spring $k_i$ ($i = 3, 4$). Unlike the previous design, there is no gravitational potential energy. However, in this subcase we would like to exert a horizontal force $\vec{F}$ to push the user attached to the end effector. According to the third principle of dynamics, the mechanism would then be subjected to a force pushing it back, as shown in Fig. 2(b). Assuming such force to be the same regardless of the configuration, it is possible to define a potential energy associated to $\vec{F}$:

$$E_f = -\vec{F} \cdot \vec{P},$$

where $\vec{P} = l_1 \vec{x}_1 + l_2 \vec{x}_2$ and $\vec{F} = -F \vec{x}$, so

$$E_f = F l_1 \vec{x}_1 \cdot \vec{x}_1 + F l_2 \vec{x}_2 \cdot \vec{x}_2.$$  

As for the springs, Eq. 3 still holds, but now $\delta_i^2 = a_i^2 + b_i^2 - 2a_i b_i x_i \cdot x_i$, thereby the total potential energy is

$$E_f + E_s = C' + (F l_1 - k_1 a_1 b_1) \vec{x}_1 \cdot \vec{x}_1 + (F l_2 - k_2 a_2 b_2) \vec{x}_2 \cdot \vec{x}_2,$$

where $C'$ is a constant term. To ensure $\frac{\partial E}{\partial \theta_i} = 0 \ \forall \theta_i$, it must be $k_1 = \frac{F l_1}{a_1 b_1}$ and $k_2 = \frac{F l_2}{a_2 b_2}$.

In line of principle, the two design goals of gravity balancing the mechanism and exerting the desired force can be obtained by superimposing the two configuration described above. However, the design would be complex and bulky since there would be several springs and auxiliary links, as well as interference problems.

As in architecture 1, this kind of design can be slightly changed and adapted to the case of exerting a horizontal force at the end effector, this time by making $a_1$ horizontal rather than vertical. Furthermore, the two configurations can be superimposed to obtain a gravity balanced mechanism that exerts the desired force (Fig. 3(b)). In particular, the two springs connected between link 1 and link 2 can be reduced to one spring. The advantage of this architecture with respect to the architecture 1 is the ease of design, due to the reduced numbers of links and springs. In this case the conditions to be satisfied are $(8), (9)$ and

$$F l_1 = k_3 a_3 l_3 \quad (11)$$  
$$F l_2 = k_1 a_1 b_1 \quad (12)$$  
$$-k_1 b_1 - k_2 l_2 b_2 + k_3 a_3 b_3 = 0. \quad (13)$$

3) Implemented architecture: By looking at $(8), (9), (11), (12)$ and $(13)$ one can notice that the contribution of spring $k_3$ appears only in $(13)$, and apparently $k_3$ seems to be essential since all the quantities involved are positive and if $k_3 = 0$ then $(13)$ could not be satisfied. However, $b_2$ could be set to a negative value: physically, this means that the attachment point of spring $k_2$ on link 2 is $b_2$ far from the hinge, in the direction opposite to the end-effector, as shown in Fig. 4. By imposing $b_2 < 0$, from $(9)$ we get the constraint $h_2 > 0$: physically, this means that the centre of mass of link 2 lays on the other side of the hinge as well.

The implemented architecture is shown in Fig. 4. It is gravity balanced and it exerts the desired force regardless of its configuration. This goal is achieved without auxiliary links and by using only 2 springs, thus it is a completely novel design. The magnitude of the force $F$ is easily adjustable, since from $(11)$ and $(12)$ it is proportional to $a_1$.

![Fig. 4. Architecture gravity balanced and exerting $F$ with 2 springs only.](image)

C. Approximate spring design solution

The CPFD is represented in Fig. 5. For simplicity, it was decided not to mount any spring on the most proximal joint. As a result, the gravitational potential is unchanged, while the force exerted will lay on the plane defined by the first joint. This is acceptable as long as the first joint range of motion is very small (it was verified experimentally).

So far, we dealt with zero free-length springs. A spring of that kind exerts a force proportional to its length, rather than its elongation. In practice, such a spring is not available off the shelf, but there are several techniques that allow to mimic the same behaviour [22]: for instance, it can be realized by
means of a cable-pulleys system and a traditional nonzero free length spring. This solution might be bulky and complex since in addition to cables and pulleys, a large amount of space is required for the storage of the nonzero free-length spring, which cannot be physically located between the theoretical attachment points. On the other hand, nonzero free length springs can be mounted in the same locations of the zero free-length springs, as studied in [23]. In such a case, the equations to be satisfied become

$$m_1gh_1 + m_2gh_2 = k_2(1 - \frac{l_{02}}{\sqrt{a_2^2 + b_2^2 + l_{02}^2}})a_2l_1$$  \hspace{1cm} (14)

$$m_2gh_2 = k_2(1 - \frac{l_{01}}{\sqrt{a_1^2 + b_1^2 + l_{01}^2}})a_2b_2$$  \hspace{1cm} (15)

$$FL_1 = k_1(1 - \frac{l_{01}}{\sqrt{a_1^2 + b_1^2 + l_{01}^2}})a_1l_1$$  \hspace{1cm} (16)

$$FL_2 = k_1(1 - \frac{l_{02}}{\sqrt{a_2^2 + b_2^2 + l_{02}^2}})a_1b_1$$  \hspace{1cm} (17)

$$-k_1b_1(1 - \frac{l_{01}}{\sqrt{a_1^2 + b_1^2 + l_{01}^2}}) - k_2b_2(1 - \frac{l_{02}}{\sqrt{a_2^2 + b_2^2 + l_{02}^2}}) = 0,$$  \hspace{1cm} (18)

where $l_{01}$ and $l_{02}$ are the free length of springs $k_1$ and $k_2$. It might be proven that (14)-(18) yield acceptable approximations if the following conditions hold:

$$\frac{2b_1l_1x_1^2 - 2a_1l_1x_1x_2 - 2a_1b_1x_2^2}{a_1^2 + b_1^2 + l_{01}^2} < 1$$  \hspace{1cm} (19)

$$\frac{-2b_2l_2x_2^2 - 2a_2l_2x_2x_1 - 2a_2b_2x_1^2}{a_2^2 + b_2^2 + l_{02}^2} < 1.$$  \hspace{1cm} (20)

However, since the number of free parameters (lengths of the links, springs attachment points, center of mass of link 2, etc.) is larger than the number of constraints (14)-(18), the best geometry of the mechanism was defined through a numerical optimization. The used cost function, defined over the representative gait cycle, is $|mean(F_x - 50)| + std(F_x)$. A maximum allowed value of 5 N is set for $F_y$ and $F_z$, and the structural resistance of the springs is also imposed.

The optimum design parameters are (Fig. 4): $l_1 = 0.971$ m, $l_2 = 0.177$ m, $a_1 = 0.218$ m, $a_2 = 0.242$ m, $b_2 = -0.244$ m, $h_2 = -0.266$ m, from which spring ratios and lengths are derived. It was observed that the errors due to use of nonzero free length springs could partially compensate the errors due to inertia and to the movements of the first joint.

IV. EXPERIMENTAL VALIDATION

A. Hardware implementation

For the sake of simplicity, non zero free-length springs were chosen for the first prototype of the device. Due to the limited motion of the pelvis during walking, the device was optimized in the neighborhood of a representative configuration as described in the following.

D. Modelling and Optimization

A standard pelvis motion over the gait cycle [20] was considered as the input for the optimization process. Joint angles and their time derivatives were calculated by means of inverse kinematics. Then the forces at the end effector were calculated with an inverse dynamic model of the device.

The target design force was set to $F_x = 50$ N, $F_y = F_z = 0$ N (axes as in Fig. 5). The actual force output from the dynamic model is not expected to exactly match the one predicted by the static model (14)-(18) because:

- the static model does not take into account the proximal dof (rotation about vertical axis);
- the static model does not account for dynamic forces;
- the static model (featuring non zero free-length springs) is approximate.

Based on the design optimization presented above, a first prototype of CPFD was fabricated and assembled at Columbia University (Fig. 6). The device is made out of light-weight aluminum bars. Eyebolts located on the bars allow fast connection of the springs. The length $a_1$ can be adjusted by moving the corresponding eyebolt along a discrete set of positions, thus making it possible to adjust the nominal force $F_x$. Incremental encoders (Kubler T8.582x series, 18400 pulse rate) are mounted at each joint. The interface with the subject consists of a semi-rigid pelvic belt (Osprey IsoForm CM Hipbelt) connected to the end point of the device by means of a spherical joint. A force/torque sensor (ATI Mini - 45) is installed on a bracket located between the spherical joint and the belt to record interaction forces. An inertial measurement unit (IMU) rigidly attached to the mounting bracket of the force sensor allows to estimate the orientation of the latter with respect to a fixed frame.

B. Protocol

As a proof-of-concept validation of our approach, a first experiment was conducted on a single male subject (age 30 years, $h = 1.80$ m, $w = 68$ kg). The experiment consisted of three sessions, each one lasting 5 minutes. In the first and in the last sessions (baseline and post-test, respectively)
the subject performed free treadmill stepping at a constant speed (1 m/s). In the second session (training), the device was adjusted to exert a force of 50 N on the subject’s pelvis. Reflective markers were placed on the human body to measure gait kinematics (VICON BonitaB3), following the arrangement suggested in [24]. During the training session, data from the encoders, the force/torque sensor and the inertial sensor were recorded through a DS1103 board (fs = 200 Hz for the IMU, fs = 1 kHz for other signals). Motion capture data were sampled at 100 Hz during all the sessions. Synchronization between the two systems was achieved through a dedicated TTL signal.

Only the data recorded over the last minute of each session were retained for subsequent analysis. Each signal was split into gait cycles, and single-stride profiles were time-normalized (0-100% of the gait cycle) and subsequently averaged across all the steps.

C. Results

Fig. 7 shows the magnitude of the interaction force over the gait cycle (GC), where 0 and 100% indicate the initial contact of the right leg (heel strike). The average value of the force was 42.01 N (RMS), less than the nominal desired value of 50 N. Force peaks were recorded at 15% and 65% GC, corresponding to the beginning of the right and left single support phases, respectively. The direction cosines with respect to \( \theta_x \), \( \theta_y \) and \( \theta_z \) are also portrayed in Fig. 7. As expected, the largest projection of the force vector lies along \( \theta_z \) and its negative value indicates that the device actually exerted a forward force on the subject. The out-of-plane component of the force (i.e., the projection along \( \theta_y \)) is negligible, whereas the projection along \( \theta_z \) indicates that the exerted force pointed downward.

The offset in the desired average force can be explained with the average configuration of the device not matching the nominal one when the subject was walking. Indeed, design optimization was carried out by assuming that the device operates in the neighborhood of a nominal configuration. Due to the approximate implementation of our design approach (i.e., one with non zero-length springs), the exerted force slightly varies when this average configuration changes. Fig. 8 illustrates how the average force projections are expected to change as a function of the offsets \( \Delta x \) and \( \Delta z \) from the nominal position: a positive \( \Delta x \) reduces \( F_x \) and increases the downward force (positive \( F_z \)). Therefore, experimental data suggest that the subject’s pelvis was too far away from the inertial frame, presumably 5 cm further than the nominal configuration (Fig. 8, left plot). To prevent this problem in future tests, augmented visual/auditory feedback will be provided to the subject to guarantee that the position of his/her pelvis along \( x \) will remain in an appropriate neighborhood of the nominal configuration.

Kinematic data showed a slight reduction in the hip flexion/extension range of motion (ROM) when subject wore the device (baseline: 38.0 ± 1.2 deg, training: 33.3 ± 1.4 deg). This was related to a reduction in the stride length, that also reflected in a slight decrease in the stride time (baseline: 1.36 ± 0.02 s, training: 1.30 ± 0.03 s), the walking speed being constant. No noticeable changes were measured at the knee joint. Conversely, we observed an increase in the ankle peak plantarflexion (Fig. 9) during weight acceptance (baseline: −11.6 ± 4.7 deg, training: −15.7 ± 3.1 deg) and a slight decrease of dorsiflexion prior to push-off (baseline: 10.6 ± 2.3 deg, training: 9.2 ± 0.7 deg). No noticeable changes were observed in the post-test session, indicating that any motor adaptation was washed out by the 5-th minute of the post-test.

Fig. 8. Exerted force variations with configuration changes.

Fig. 9. Ankle angle during baseline, training and post-training.

Decreases in stride time [25], [26], [27], hip range of motion [25], [27], ankle angle at foot contact [25] and peak dorsiflexion prior to push-off [25], [28] are effects typically observed in downhill walking. Similar to our experiment, also in downhill walking there is a constant force (namely, a fraction of the subject’s weight) acting close to the pelvis
(namely, at the body center of mass) which tends to push the subject forward. Downhill walking has been shown to reduce efforts of the ankle plantar flexor at push-off (positive work), and increases the activity of the knee extensors, which stabilize the knee at heel strike [28] (negative work), the overall effect being a decrease in metabolic cost of walking, at least within a certain range of grades [29]. Therefore, even though further experiments needs to be conducted on a larger sample size (by, e.g., measuring subject’s muscle activity and metabolic cost), there is the possibility that utilizing the CPFD could actually reduce metabolic cost of walking.

V. CONCLUSION

The design of a new Constant Pushing Force Device for human walking analysis was presented. The device is based on a novel actuating technique derived from gravity balancing theory, and it allows to exert a desired constant force at the pelvis of a subject walking on a treadmill.

Unlike previous designs, our approach allows us to utilize the same pair of springs to achieve two goals simultaneously: gravity compensation and exertion of a constant pushing force. It is worthwhile saying that the step from balancing to actuating is not immediate: there are some mathematical conditions to satisfy to ensure that the force exerted is the desired one. However, such details are currently being investigated and are not included in this paper.

Experimental results show that the device was capable of exerting a pushing force that approximated the nominal prescribed force in magnitude and direction, the deviations being mainly due to the subject walking too far away from the nominal configuration of the CPFD. Observing the analogies between subject’s motor adaptations, and those typical of downhill walking, we speculated about the potential for this device to reduce metabolic cost of walking. Future work will experimentally validate this hypothesis on a larger sample size, measuring electromyographic activity on critical muscles of the leg and metabolic cost of walking in addition to the kinematic and kinetic variables analyzed in this study.

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