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# **A hybrid framework for non-linear dynamic simulations including full-field optical measurements and image decomposition algorithms**

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## **1. Introduction**

Structural design of innovative components for transport vehicle structures involves extensive Finite Element (FE) simulations in order to analyze the mechanical response of structural elements under service loads or loading conditions generated by critical events (e.g. impact). Structural dynamics methods initially focused on natural frequency analysis and were limited to frequency domain forced response analysis. Until the mid 70's, transient response analysis was typically performed in the modal space retaining only the first few fundamental modes of vibration. Dynamic response of non-linear systems was limited in the frequency-domain and time-domain calculations were rarely attempted due to numerical instability problems entailed by forward-marching solutions. Generally speaking, time-domain calculations for non-linear systems, especially in case of impulsive loads, present a severe problem in the fact that numerical stability is reached as the time-step size is in the range of 1e-8 seconds.

The implicit methods, such as the Newmark's b-method, were developed to achieve stable integration with larger time steps. Hardware improvements along with algorithm advances made it

possible to use explicit time-integration techniques also for high-speed events with rapidly changing contact impact dynamics. This pushed major commercial aircraft manufacturers towards developing their in-house structural dynamics code in order to analyze impact events.

Presently, commercial codes including explicit schemes, such as Abaqus, LS-Dyna, Pam-Crash, and others combined with high performance computing resources, can model impact and crashworthiness events on the whole structure and provide reasonably good estimations on impact strength. Impact analysis models are usually quite large and include at least some millions of nodes and elements.

Rather than limiting the model size a priori, one should find algorithms able to simulate the actual impact event the most accurately as possible. However, these simulations need reliable validation techniques, especially in cases that anisotropic materials, complex geometry, non-linear dynamic loading and complex boundary conditions are involved.

In this frame, the use of full-field optical techniques can be proven a useful tool for the deeper understanding of deformation and failure process of the structural elements, as well as they can be used in the assessment of the accuracy of numerical results by comparing the predicted values to corresponding experimental data [1]. The strength of full-field optical techniques is that the entire displacement field can be visualized and analyzed. By using High Speed cameras, the Digital Image Correlation (DIC) method can be applied to highly non-linear dynamic events and give quantitative information on the three-dimensional displacement and strain fields [2].

The Digital Image Correlation method (DIC) has been selected for the present research because, unlike moire, speckle and holography, it does not require any phase unwrapping and can hence intrinsically deal with non-smooth displacement / strain distributions. Furthermore, it is relatively fast and hence highly suited for application in industrial environment.

The objective of the present paper is to integrate full-field optical measurement methodologies with state-of-the-art computational simulation techniques for non-linear transient dynamic problems, in

order to validate the numerical simulation. The paper focuses on the methodology for comparing experimental and numerical data. More specifically, the conventional approach of identifying hot-spots in the data and checking if experiments agree well with simulation results may lead to miss essential details on the mechanical response of the structure that should be introduced in the simulation models in order to increase their robustness and predictive capability. Significant progress has been performed in the frame of project ADVISE [3] in developing an integrated methodology for comparing FE simulations to experimental data, including the use of reduced or decomposed data (**Figure 1**) [3]. Different shape descriptors (Geometric moments, Zernike moments, Chebyshev features, etc.) can be used to significantly reduce the amount of the data in order to simplify the data comparison [4].

The validity of the proposed methodology is demonstrated for the case of a car bonnet frame structure of dimensions about 1.8 x 0.8 m, made of PolyPropylene (PP) or PolyAmide (PA) glass fiber reinforced thermoplastic materials. In purpose of assessing their energy absorption capability, bonnet frames have been tested in hard-body low velocity, low energy, mass-drop impact loading, in a drop-tower, with impact energies ranging from 50J to 200J. In parallel, simulation models of the car bonnet frame have been developed using layered shell elements. A node-to-surface contact definition is introduced for modeling the physical contact between the impactor and the bonnet.

A High Speed Image Correlation system was used to record full field optical measurement data, which were used to correlate experimentally recorded and numerically calculated displacement / strain histories at various points of the structures and different time intervals of the event. In such a way, numerical simulations of car bonnet frame impact were validated by full field optical measurements. After decomposition of displacement images captured at time intervals of interest, a reconstruction process is executed, in order to assess the quality of the decomposition process. Consequently, the reconstructed images are compared qualitatively and quantitatively, indicating a successful correlation.

## 2. Low velocity impact tests carried out on the car bonnet.

An Instron 9000 series mass-drop tower capable of delivering up to 1000 J impacting energy was used. Moreover, the Dantec Dynamics Q-450 high speed optical system was deployed to capture strain / displacement fields during the dynamic events. The optical system includes two high speed cameras, mounted on a tripod, capable to capture three-dimensional (3D) fields, an integrated analogue data acquisition system, a portable notebook and a high intensity white light source. Furthermore, for testing purposes, a steel base was designed and constructed to provide a robust support for the car bonnet specimens. The experimental set-up is presented in **Figure 2**.

The impacting energy, originating from gravitational energy, ranged from 50 to 200J and delivered through a rigid cylindrical impactor with a hemispherical tip of 25mm diameter. The car bonnet frame specimens (**Figure 3**), provided by Centro Ricerche Fiat (CRF), were produced by two material types, i.e. Polypropylene reinforced with 30% glass fiber (PP) and Polyamide reinforced with 30% glass fiber (PA). The PA material has greater ductility and higher ultimate strength. The mechanical properties of both materials are summarized in **Table 1**.

Specimens were fixed in a horizontal position, in the three hinge areas marked in **Figure 3**, while the entire structure was allowed to move only in the upwards out-of-plane direction. Impact took place at a central point of the bonnet marked with yellow in **Figure 3**. The acquisition data frequency of the optical system was set to 4000Hz, resulting in 4 pictures per one millisecond.

**Figure 4** shows the images of the damaged specimens taken for the case of PP bonnet (left) and PA bonnet (right) after impacting with 200J energy. Bonnet made of PA absorbed almost all of the impacting energy in contrast to the bonnet made of PP which fractured at the area of impact.

### 3. FE simulation of the car bonnet impact tests

A stress-check finite element model of the car bonnet frame with an accurate geometry description has been provided by Centro Ricerche Fiat (CRF) along with bonnet specimens, in the frame of the ADVISE project [3]. This rough numerical model has been modified, to make it suitable for the simulation of drop-tower impact events carried out with the ANSYS LS-Dyna FE solver.

The modified FE model comprises 22328 elements. The element type used is 'Shell 181', which is suitable for analyzing thin to moderately-thick shell structures. It is a 4-node element with six degrees of freedom at each node: translations in the x, y, and z directions, and rotations about the x, y, and z-axes. There are 5 integration points through-the-thickness. The average thickness of the elements is 3mm. A finer mesh has been generated in correspondence of the region of impact (**Figure 5**), because this is the area facing the impact: consequently, displacement and strain gradients caused by damage propagation will be much sharper than in the rest of the model.

The finer mesh has been obtained by progressively splitting the elements around the critical impact zone until convergence of the FE results occurs. The resulting FE mesh includes elements having edge length equal to about 1/3 of the initial elements. It should be noted that a denser mesh not only facilitates the convergence of FE analysis but also minimizes errors caused by the condensation techniques applied later.

Boundary conditions are introduced at nodes of the hinged areas in fashion of displacement constraints in the coordinate directions x, y and z.

An elastoplastic material model with isotropic damage (MAT2) is used. This model has been calibrated for the materials used in the case of the simple flat panels simulation [5]. Element failure is predicted to occur when strain exceeds the corresponding strain to failure limit set to 4% for PA material and 2.3% for PP material, respectively. The impactor is modelled as a rigid sphere. The node-to-surface contact modelling option is chosen to simulate the contact behaviour between the impactor and the

bonnet. An appropriate initial velocity is given to the impactor in order to develop the desired impact energy values (see **Table 2**). For example, **Figure 6** shows the out-of-plane displacement generated in the PP200J specimen 12ms after the impact.

**Figure 6** shows the out-of-plane displacement generated in the PP200J specimen at 12ms after the impact.

#### 4. Approximation of displacement field

Comparison between experimental and numerical data is performed on a selected area of 170mm x 45mm, which is located around the impact region of the bonnet (**Figure 7**). However, numerical results and experimental data could not be compared over the entire specimen because of space constraints which made it not feasible to cover the whole surface of the bonnet (more evidence of this can be gathered from **Figure 2**).

A quantitative comparison between experimental and numerical data is made through the use of Zernike moment parameters, which are used as shape descriptors for the decomposition of displacement – strain maps.

The compared parameter was the out-of-plane displacement field for selected time frames. **Eq. 4.1** describes the mathematical expression of the Zernike moment descriptor:

$$Z_{n,m} = \frac{n+1}{\pi} \int_0^1 \int_0^{2\pi} I(\rho, \theta) V_{n,m}^*(\rho, \theta) \rho d\rho d\theta \quad (4.1)$$

where,

$I(\rho, \theta)$  is the matrix containing displacement/strain data,

$$V_{n,m}^*(\rho, \theta) = R_{n,m}(\rho) e^{-j\theta} \quad (4.2)$$

$$R_{n,m}(\rho) = \sum_{s=0}^{(n-|m|)/2} (-1)^s \frac{(n-s)!}{s! \left(\frac{n+|m|}{2} - s\right)! \left(\frac{n-|m|}{2} - s\right)!} \rho^{n-2s} \quad (4.3)$$

and  $j = \sqrt{-1}$ ,  $n$  is a non-negative integer representing the order of the radial polynomial;  $m$  and

$n$  are integers subject to constraints  $n - |m|$  even and  $|m| \leq n$ .



Since the Zernike polynomials form an orthogonal basis, the original image may easily be reconstructed as:

$$I(\rho, \theta) = \sum_{n=0}^{\infty} \sum_m Z_{n,m} V_{n,m}(\rho, \theta) \quad (4.4)$$

However, as the reconstruction of an image using infinite number of Zernike moments is not possible, approximate reconstruction may be achieved by keeping the moments from order 0 to  $N_{\max}$  and discarding the remaining higher order Zernike polynomials. That is:

$$\hat{I}(\rho, \theta) = \sum_{n=0}^{N_{\max}} \sum_m Z_{n,m} V_{n,m}(\rho, \theta) \quad (4.5)$$

where  $N_{\max}$  is the total number of moments used.

The quality of the reconstruction depends on the number  $N_{\max}$  of Zernike moments used for the image description. Selection of  $N_{\max}$  can be determined by using a predefined threshold when comparing the similarity between the original image/map and its counterpart numerically reconstructed.

Two coefficients are usually utilized in literature to assess the accuracy of the Zernike moment approximation method: the correlation error (Pearson coefficient) and the normalized mean square error, which can be applied for such comparisons (Eq. 4.6, 4.9). [6, 7]

$$\text{corr}(\hat{I}, I) = \frac{\iint_{\Omega} (\hat{I} - \bar{\hat{I}})(I - \bar{I}) dA}{\sqrt{\left[ \iint_{\Omega} (\hat{I} - \bar{\hat{I}})^2 dA \right] \left[ \iint_{\Omega} (I - \bar{I})^2 dA \right]}} \quad (4.6)$$

where,

$$\bar{\hat{I}} = \frac{\iint_{\Omega} \hat{I} dA}{\iint_{\Omega} dA}, \quad (4.7)$$

$$\bar{I} = \frac{\iint_{\Omega} I dA}{\iint_{\Omega} dA} \quad (4.8)$$

The normalized mean square error can be expressed as:

$$\bar{e}^2 = \frac{\iint_D |I(x, y) - \hat{I}(x, y)|^2 dx dy}{\iint_D I(x, y)^2 dx dy} \quad (4.9)$$

where,  $I(x, y)$  and  $\hat{I}(x, y)$  are the original and reconstructed images, respectively.

#### 4.1 Implementation of the shape-descriptors based approximation method

The comparison procedure following the image condensation entails several steps which are briefly discussed below. First, issues arisen in the post-processing of the numerical and experimental data were settled appropriately. Due to the non-uniformity of mesh points, a grid of 301x301 points (total 90601 points) was created in the area of interest and both numerical and experimental results are linearly interpolated on these grid points. The grid density has been defined after a convergence study performed for the numerical computation of Zernike moments in the unit disc space. Furthermore, the data not available from experiments because of the presence of fractured and shadowed regions are replaced by interpolated values suitable for further processing (**Figure 8**). The same approach is followed for the data not included in the numerical model because of element elimination after fracture.

It must be stated that the interpolation technique should be applied only in cases when shadowed areas are relatively small, in order to avoid adding too much arbitrary information into the images. Furthermore, the interpolation outcome strongly depends on the smoothness of the displacement or strain

field around the shadowed area. If this field is relatively smooth, as it occurs in the present case, the size of the surrounding area is not critical. However, if the surrounding field has high gradients, then the result will depend on the surrounding area size and a parametric study will be necessary to assess the effect of this size on the interpolation results. Under such scenario, the interpolation method may even be not applicable and other shape descriptors (e.g. discrete shape descriptors) should be used to condense the strain field data.

The selection of the total number of Zernike moments is defined such that the normalized mean error calculated in all cases examined does not exceed 2%. Increasing this threshold results in a higher image condensation by calculating less shape descriptors with greater loss of image information. Loss of image information cannot be avoided but should be limited as most as possible. For example, image mapping to a unit disc entails two steps:

a) Image is decomposed in  $N_{\max}$  Zernike moments, where  $N_{\max}$  is the maximum number of Zernike moments that can be calculated before numerical instabilities occur. Numerical instabilities can be dealt using various techniques which allow Zernike moments to be calculated [8, 9]. In this study, 420 Zernike moments were used for the first step of the condensation process. **Figure 9b** depicts an example of image reconstruction with 420 moments. The correspondence existing between the original and the reconstructed images is quantified by the value of normalized mean error that is equal to 0.36%.

b) Condensation process can be performed more efficiently by computing only the most important Zernike moments among those computed before. The measure of a moment's contribution to the image description is its magnitude, therefore only the greatest moment magnitudes must be considered. In **Figure 9**, the original image reconstructed with the 26 most important Zernike moments is displayed. The computed normalized mean error is equal to 0.78%. Additionally, in **Figure 9d** the original image reconstructed with the 52 most important Zernike moments is illustrated, resulting in a slight decrease in the mean error to 0.56%. **Figure 10** presents the normalized mean square error versus number of

moments plot for the PP200J case at 12ms after impact, demonstrating the efficiency of image condensation with the most important terms.

Defining an optimum mean error to number of moments ratio is currently a matter of interest. In the present work, the number of moments used for image decomposition was set to 26 moments for all cases such that no mean error value may exceed the value of 2%.

The displacement field was represented by means of a set of shape descriptors either in the case of FE results and for the experimentally measured data. While this can be done independently for numerical simulations and experimental data, the same type and order of shape descriptors should be used, thus resulting in two feature vectors [10]. Therefore, some extra moments need to be added into DIC map and the FE map feature vectors so that the moment number of both maps becomes identical and comparison may correctly be performed. In Table 3 the normalized mean error computed for each case studied and the number of additional Zernike moments that must be considered are presented. Additionally, the mean error values are re-calculated taking into consideration these extra moments used.

#### **4.2 Comparison between experimental data and FE results**

Once DIC and FE displacement maps vectors were reconstructed, feature vectors obtained for experimental data and numerical results could be plotted in a FE-moments versus EXP-moments diagram. By doing this, it was possible to obtain a region where the comparison curve is a straight line inclined by 45° with respect to a horizontal axis [10].

The simpler approach followed in this work adopted histograms. Four cases were compared: three for PP200J and one for PA50J. **Figure 11** presents qualitative comparison between FE and experimental deformation for the PP200J specimen at the time of 12 ms after impact.

Quantitative comparisons are presented in **Figures 12** through **Figure 15**: the magnitude of Zernike moments is plotted against the number of moments used in the decomposition. This was done for both experimental data and FE results. Correlation between experimental data and numerical results is good.

## 5. Conclusions

In this research, the ‘shape descriptor’ approach was successfully utilized in order to compare experimental measurements and finite element simulation carried out on a car bonnet frame under highly non-linear dynamic loading. It can be observed that a low number of terms is required for image reconstruction of the complex displacement fields of the car bonnet.

Displacement maps gathered from optical methods usually include singular points, right near the critical areas of the structure (e.g. due to the presence of load introduction devices, strain gages etc.); a similar scenario occurs in FE simulations when elements are deleted after severe damage propagation, so that the FE solution can continue without convergence problems. Therefore, the process of selecting an area for comparisons, converting it to a flat surface and then converting it to rectangular or circular area without cutouts, which is necessary for the application of shape descriptor approach, requires much effort.

The design of the experimental set up should account for the integration of a full-field optical system, such that ‘undisturbed’ optical images are obtained and a proper comparison is enabled. The approach described in [10] is very powerful although complicated. Hence, some automation is required before routine application.

A very good agreement between experimental measurements and FE results was found in the case of low-velocity impact tests, taking into account the complexity of geometry and the type of loading (severe non-linear dynamic). This demonstrates that integration of FE analysis with full-field optical measurements along with the use of sophisticated comparison techniques can increase design reliability.

In summary, this paper demonstrated that the shape descriptor comparison is a powerful approach yielding a drastic reduction in computational effort in terms of the quantity of data to be processed. This makes it possible to carry out reliable comparisons between experimental measurements and simulation results obtained in the case of large-scale complex structures subject to highly non-linear dynamic loading.

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**Figure 1:** Validation methodology developed in the frame of ADVISE project.

**Figure 2:** Experimental set-up, including drop tower, optical system, support base and car bonnet frame specimen.

**Figure 3:** Selection of the region of interest where DIC measurements and FE results are compared.

**Figure 4:** Damage on bonnet of PP material (left) and PA (right) after impact with 200J energy.

**Figure 5:** View of the convex side of the FE-model of the car bonnet frame with dense mesh on the impacting area. Gray areas represent the hinged locations.

**Figure 6:** Numerical out-of-plane displacement field obtained from pp200J bonnet case after 12ms of impact.

**Figure 7:** Area selection for comparison.

**Figure 8:** Replacement of singular points through interpolation of surrounding points.



**Figure 9:** a) Original map taken from the numerical out-of-plane displacement field of pp200J case at 12 ms after impact. b) Original w-displacement map with 420 terms (12 ms after impact). c) Displacement map with 26 terms, d) Displacement map with 52 terms.

**Figure 10:** Normalized mean square error versus number of moments plot for the numerical PP200J case (12ms after impact).

**Figure 11:** Qualitative comparison between numerical and experimental out-of-plane-displacement fields for the PP200J case (12 ms after impact).

**Figure 12:** Comparison between numerical and experimental Zernike moment descriptors for the PP200J case (4 ms after impact).

**Figure 13:** Comparison between numerical and experimental Zernike moment descriptors for the PP200J case (9 ms after impact).

**Figure 14:** Comparison between numerical and experimental Zernike moment descriptors for the PP200J case (12 ms after impact).

**Figure 15:** Comparison between numerical and experimental Zernike moment descriptors for the PA50J case (3 ms after impact).

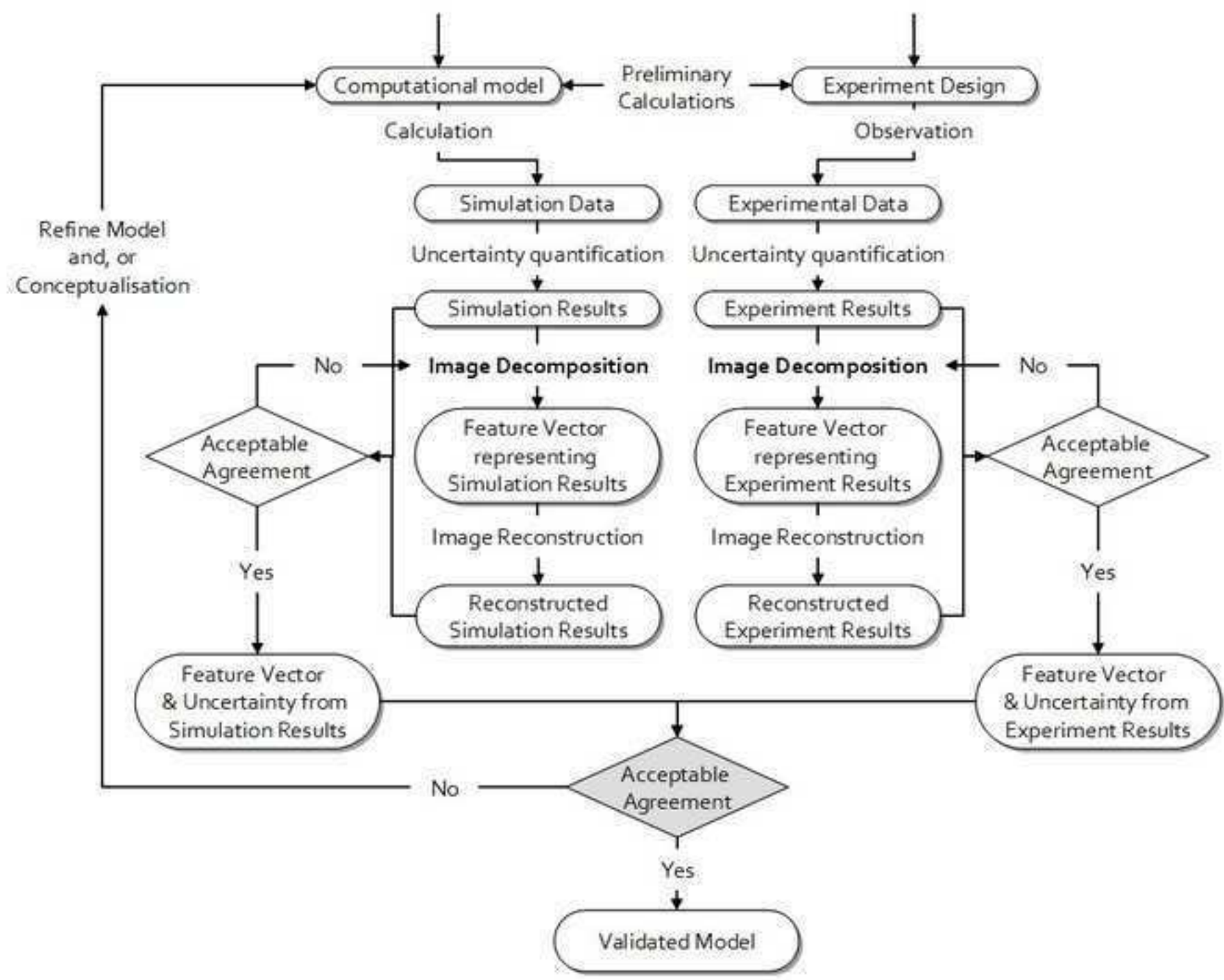
### List of notations

$\overline{e^2}$  Normalized mean square error

$\text{Corr}(\hat{I}, I)$  Correlation coefficient

CRF	Centro Ricerche Fiat
$I(\rho, \theta)$	Data matrix containing displacement/strain information
$\hat{I}(\rho, \theta)$	Data matrix containing reconstructed displacement/strain information
PA	Polyamide material
PP	Polypropylene material
$R_{n,m}$	Radial polynomial
$V_{n,m}$	Zernike polynomial
$Z_{n,m}$	Zernike moment descriptor

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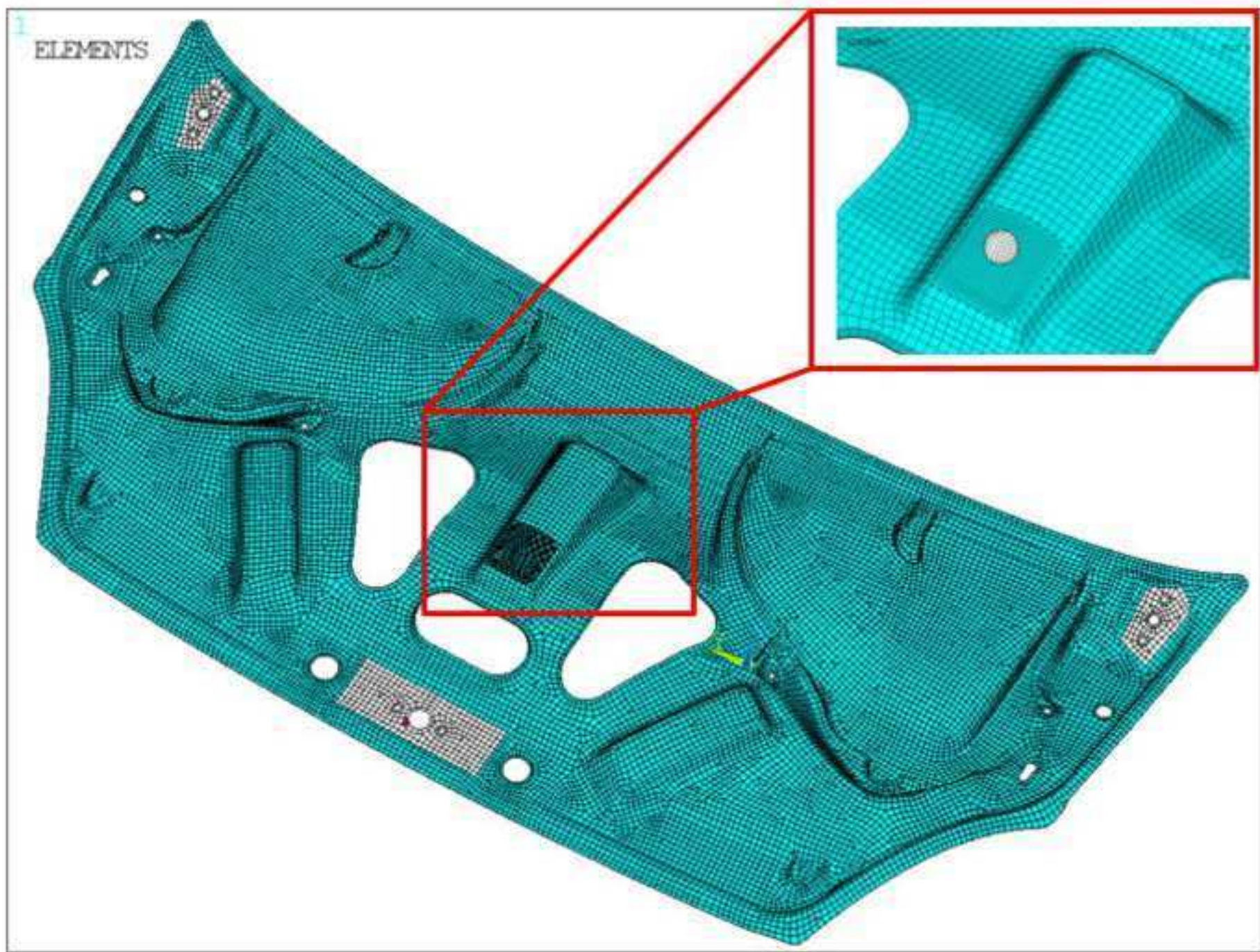
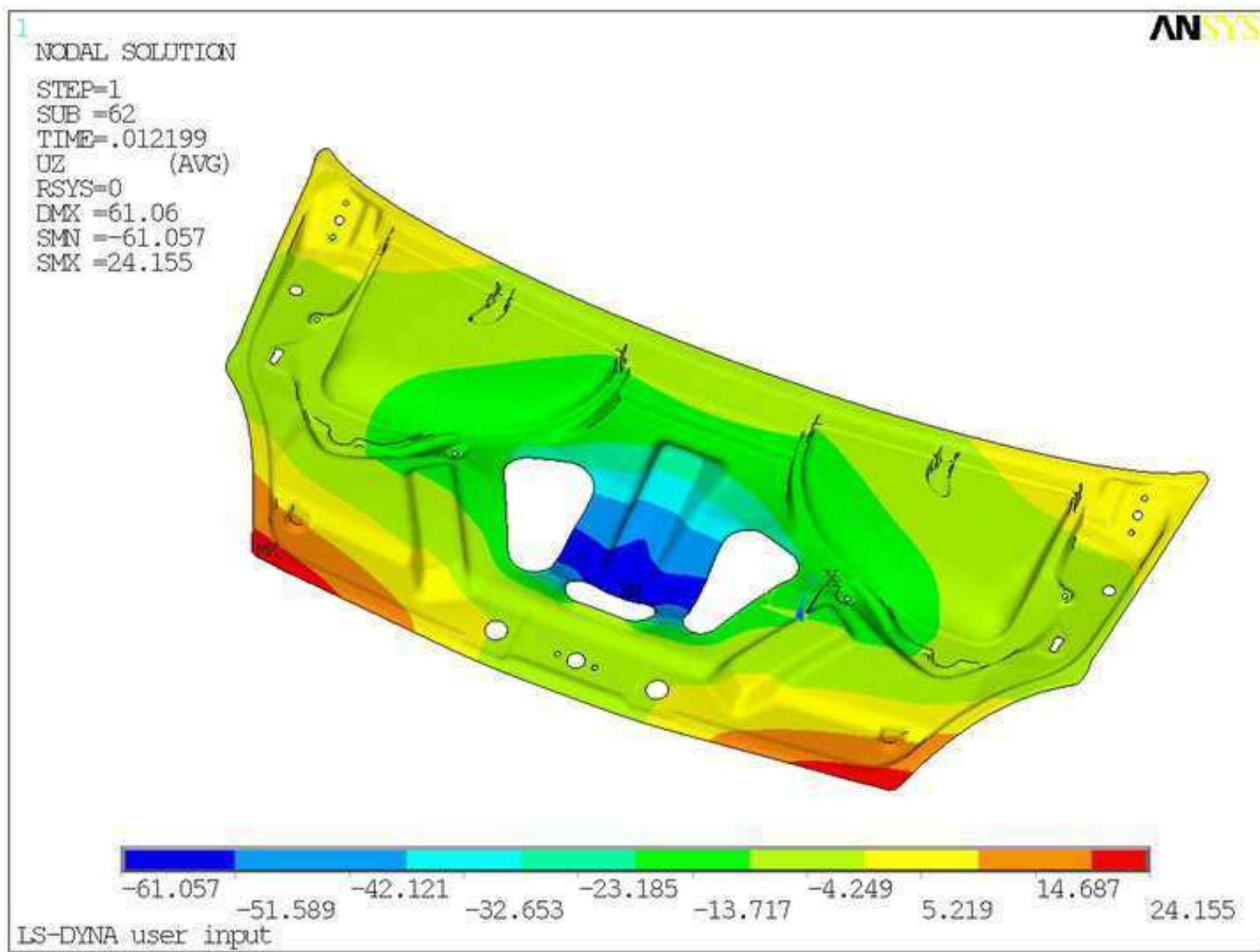




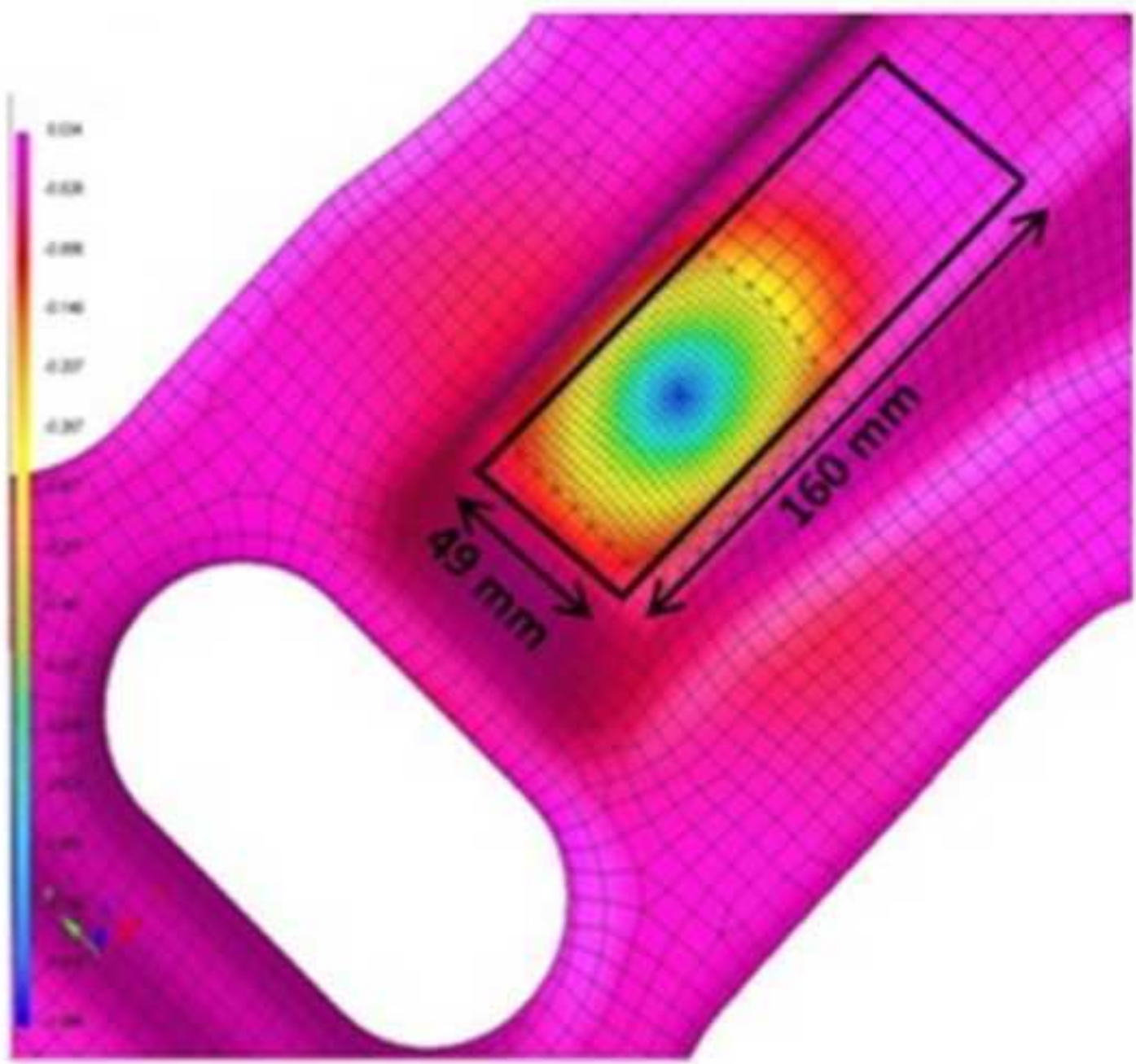
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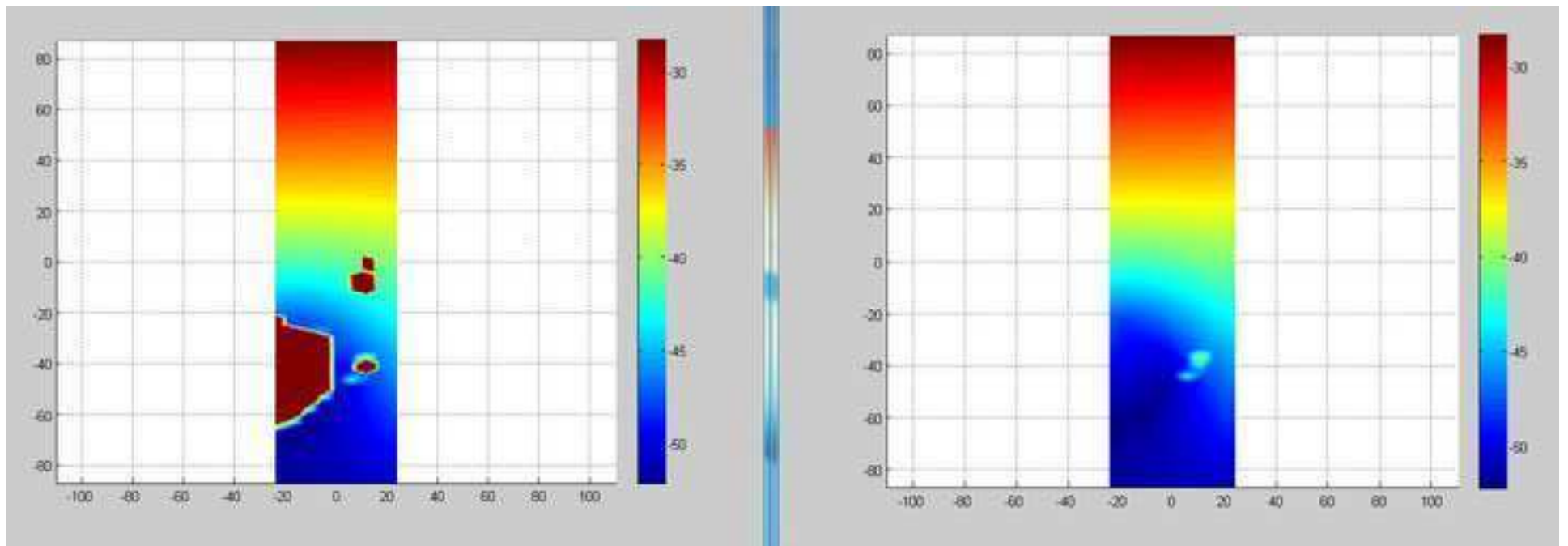
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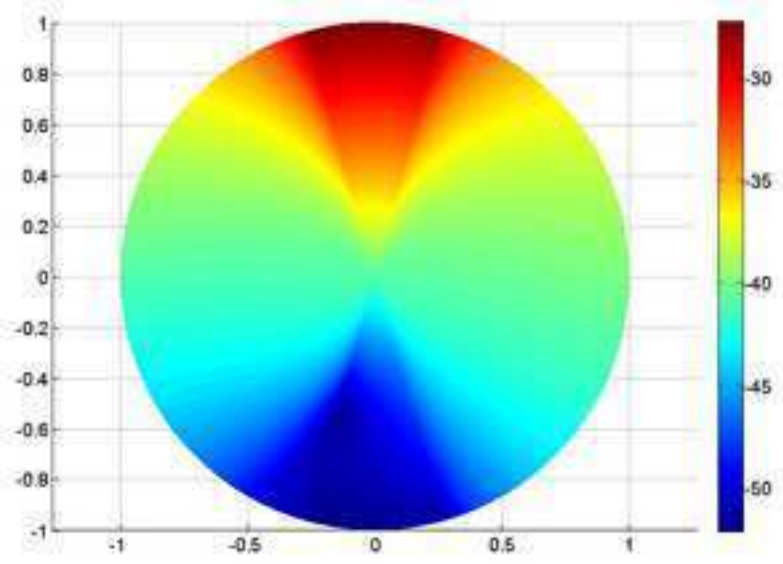
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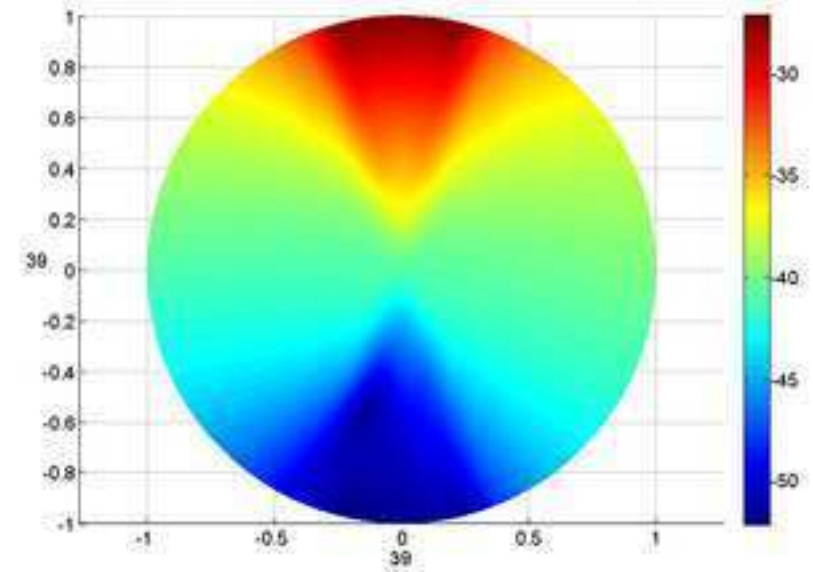


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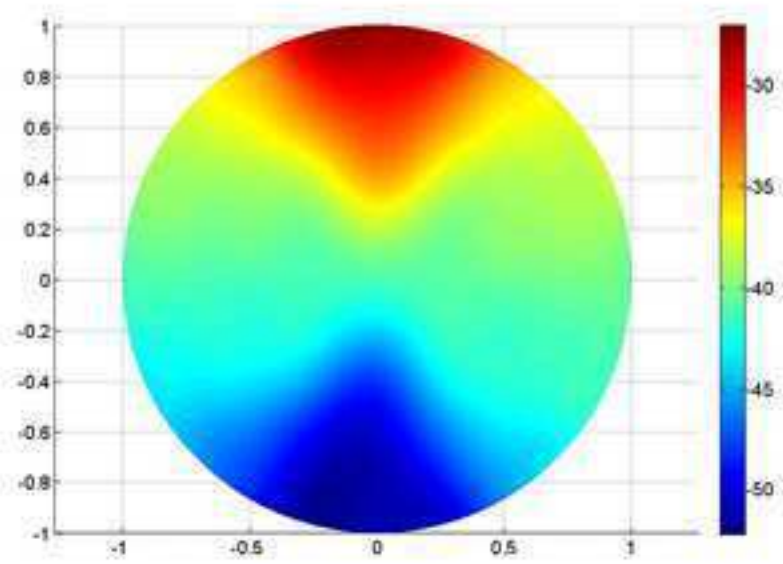
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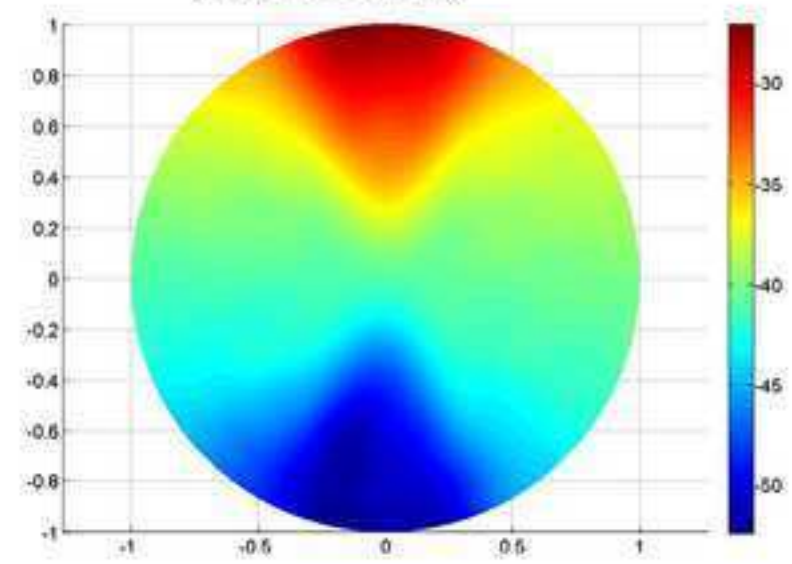
a) Original disc image



b) Reconstructed disc image with full terms



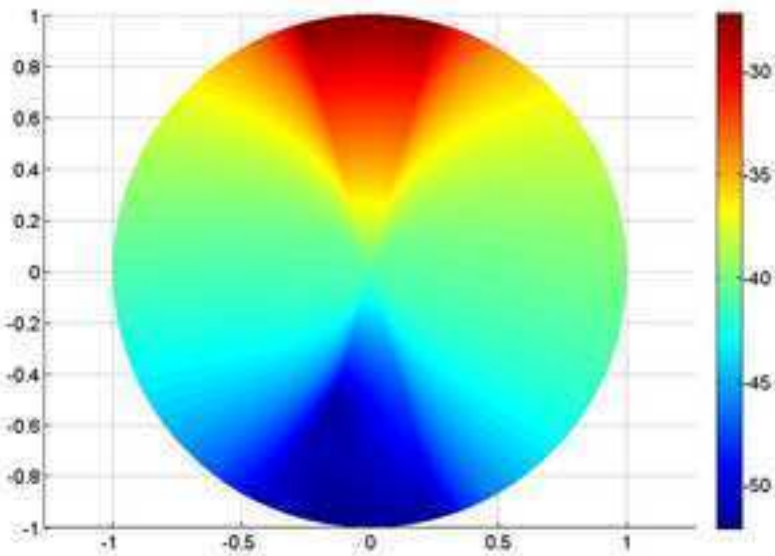
c) Reconstructed disc image with 26 terms



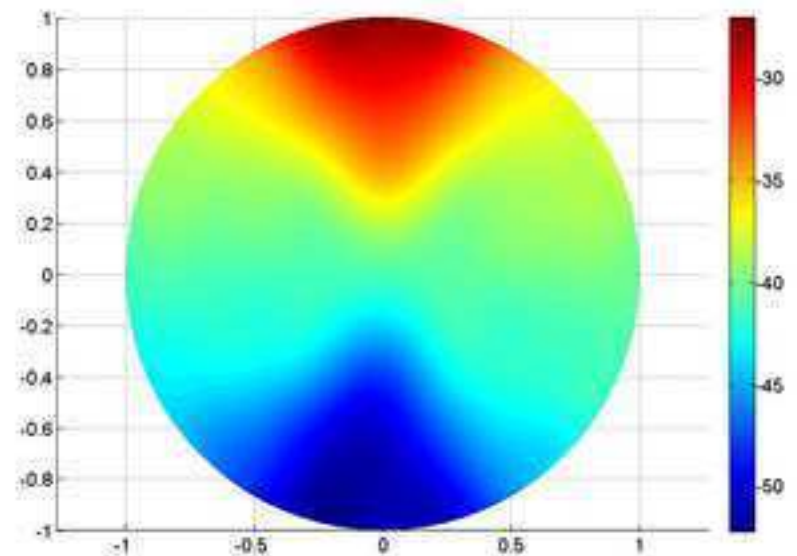
d) Reconstructed disc image with 52 terms

Figure

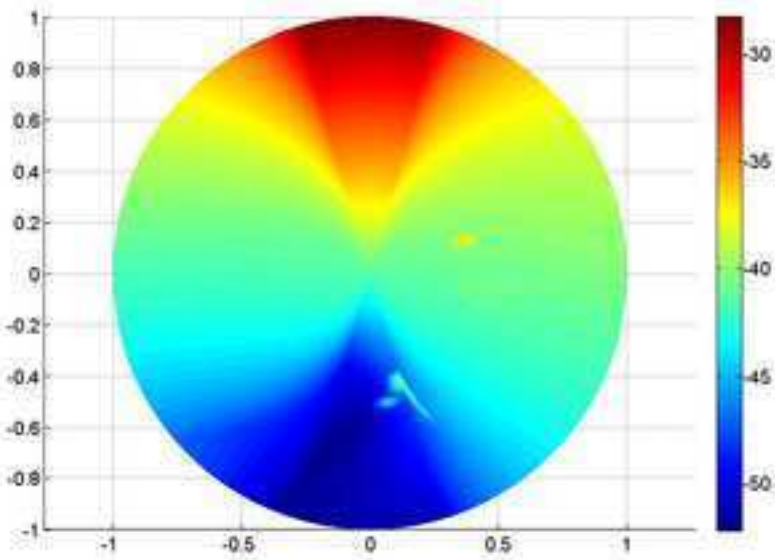
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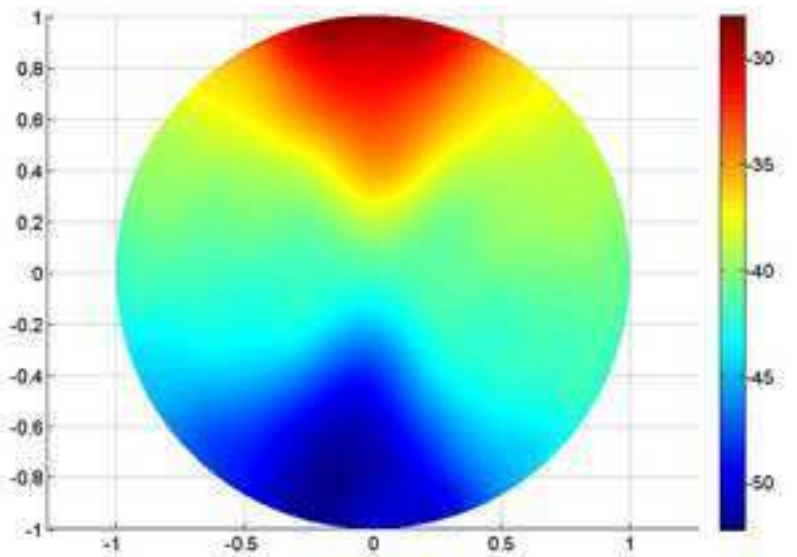
a) FE original disc image



b) FE reconstructed disc image



c) Optical original disc image



d) Optical reconstructed disc image



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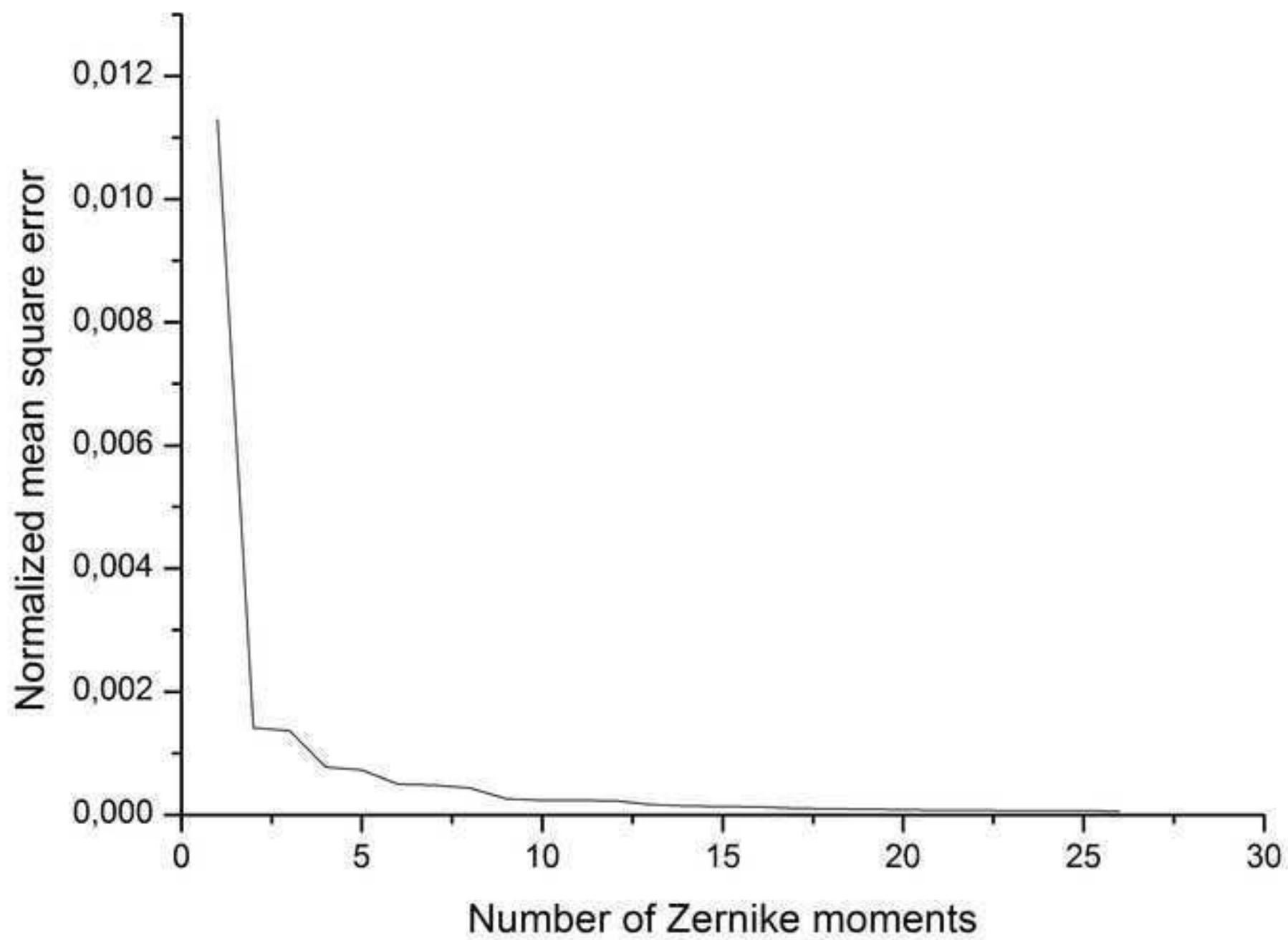


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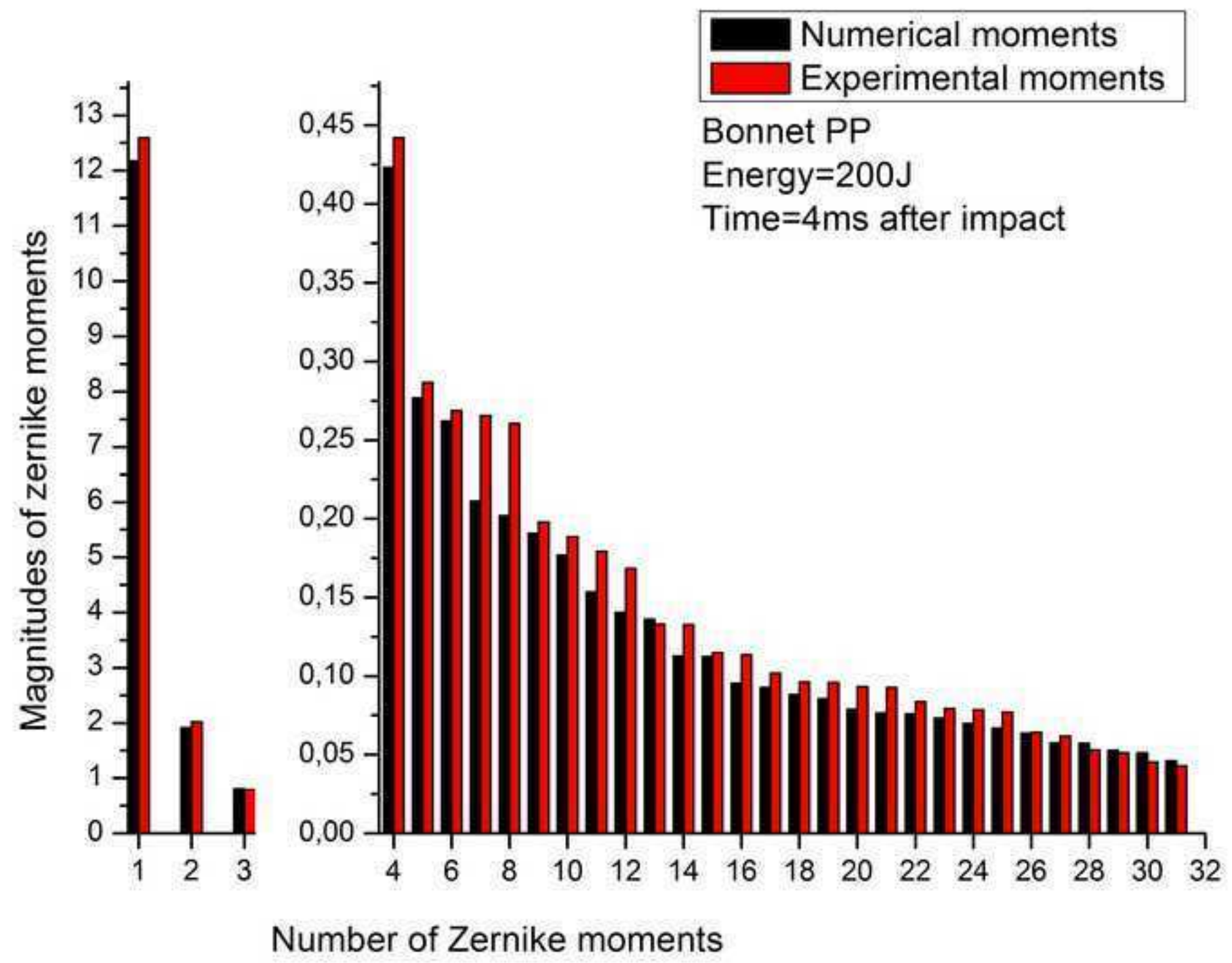


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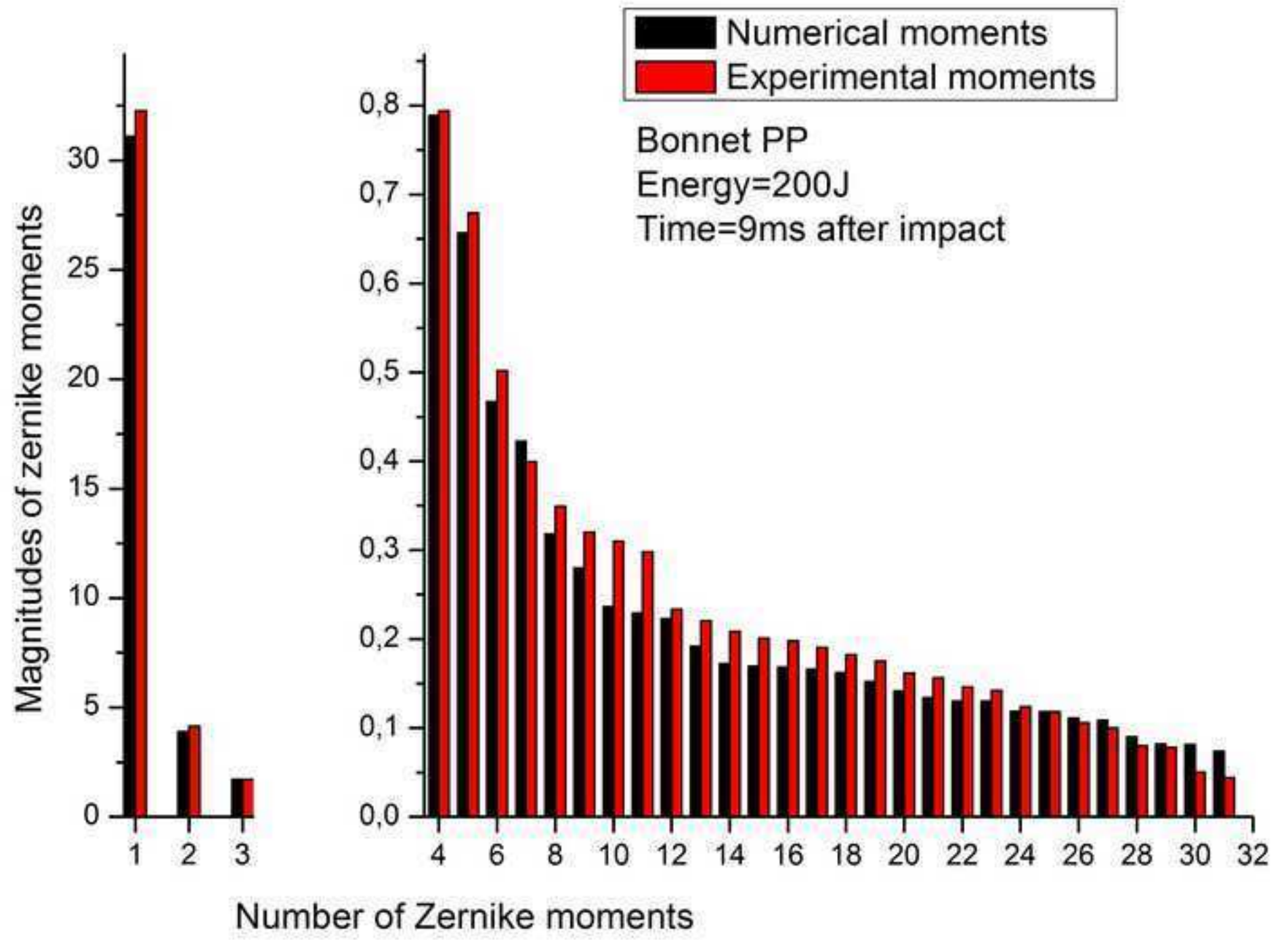
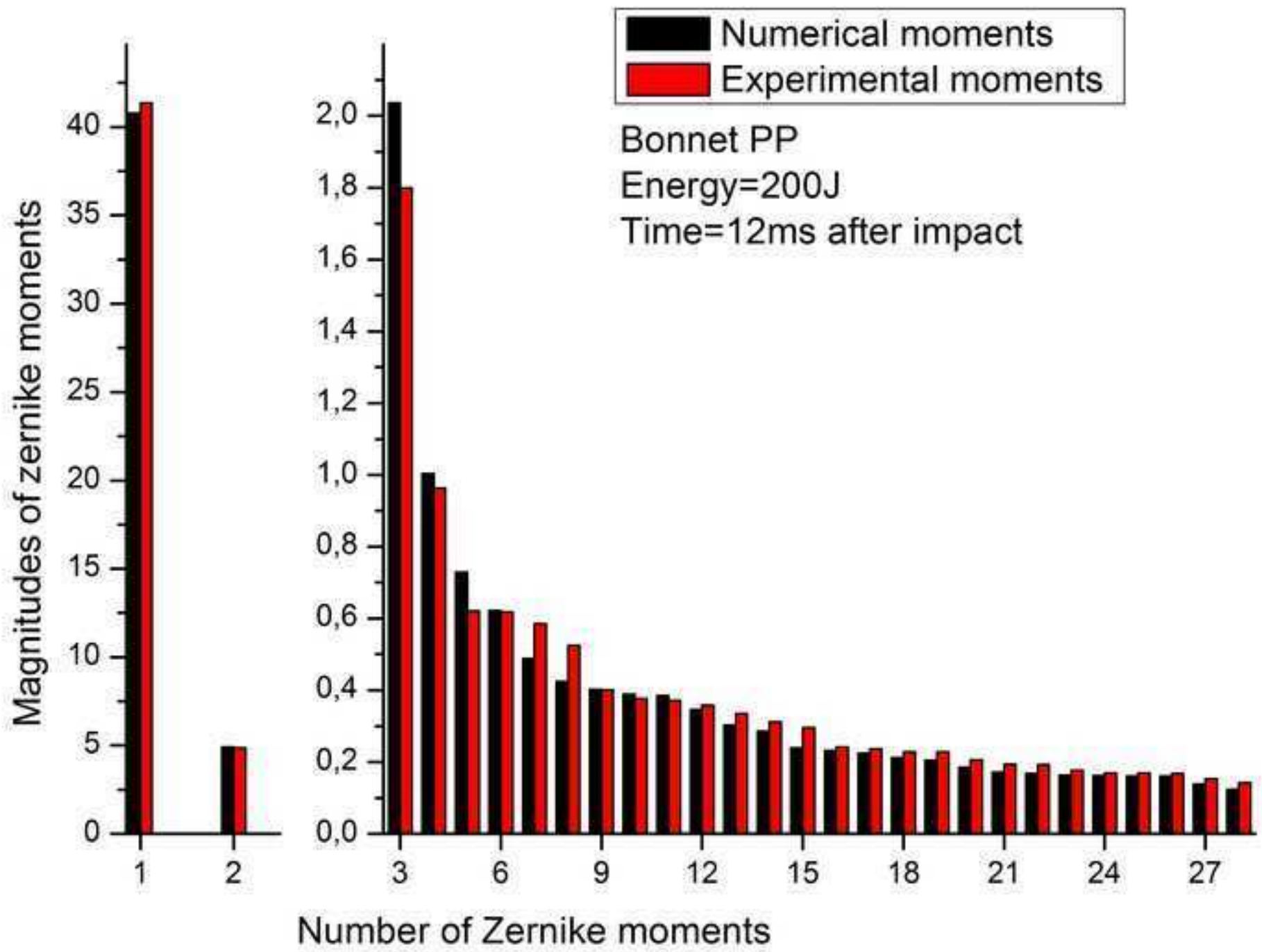


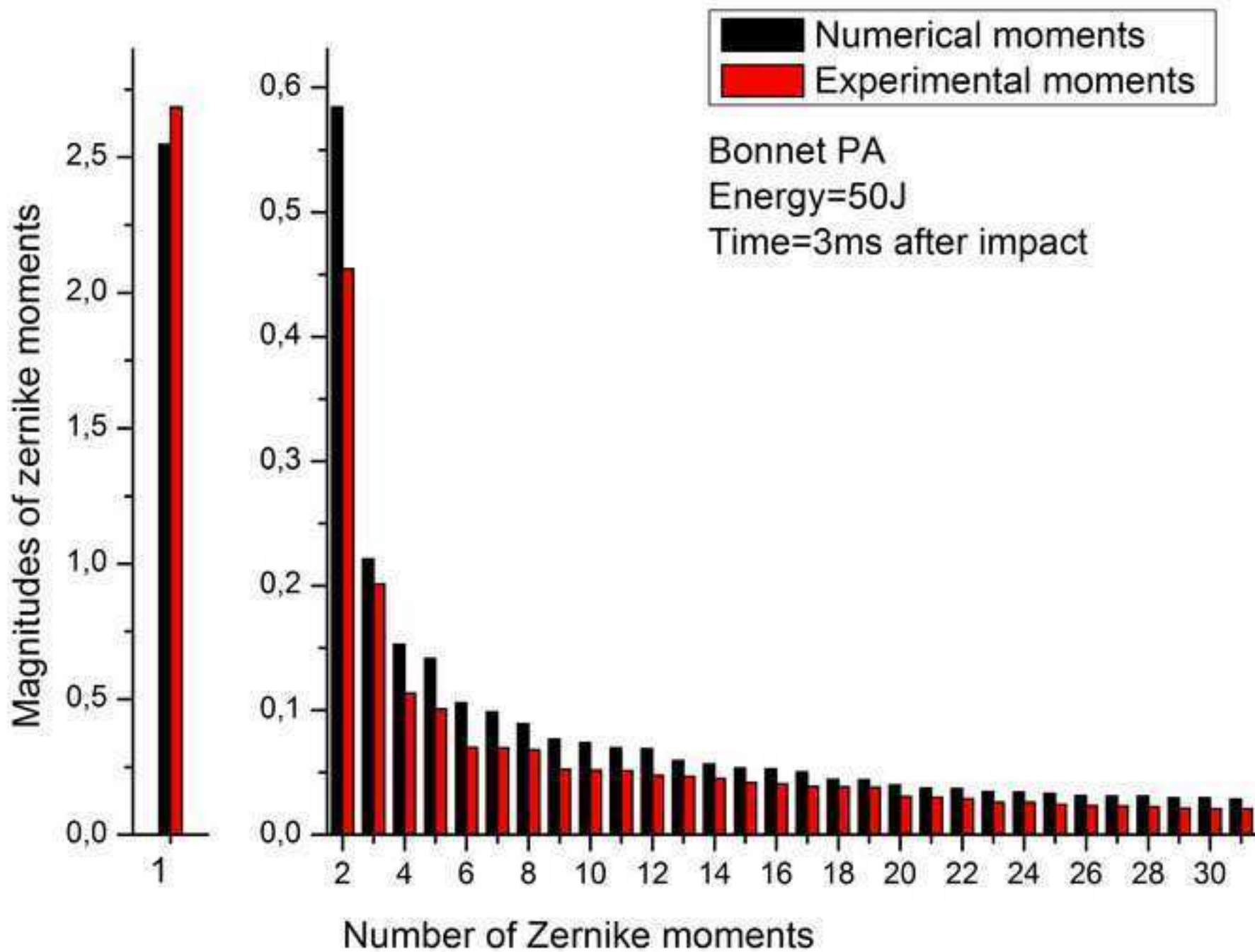
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<b>Material properties at 23<sup>0</sup>C</b>	<b>Tensile modulus (MPa)</b>	<b>Yield Strength (MPa)</b>	<b>Strain to failure %</b>	<b>Density (kgr/m<sup>3</sup>)</b>
<b>PP</b>	<b>7000</b>	<b>109</b>	<b>2.3</b>	<b>1120</b>
<b>PA</b>	<b>9700</b>	<b>180</b>	<b>4</b>	<b>1360</b>

**Table 1:** Mechanical properties of PP and PA materials at 23<sup>0</sup>C

	<b>PP material</b>		<b>PA material</b>	
<b>Energy (Joule)</b>	<b>200</b>	<b>50</b>	<b>200</b>	<b>50</b>
<b>Velocity (m/s)</b>	<b>4.89</b>	<b>2.42</b>	<b>4.89</b>	<b>2.42</b>
<b>Runtime (ms)</b>	<b>30</b>	<b>30</b>	<b>100</b>	<b>100</b>

**Table 2:** Values of parameters used in dynamic FE analyses

Material type	Impact Energy (J)	Time after impact (ms)	Number of additional moments	Normalized mean error %	
				Numerical model	Experiment
PP	200	4	5	1,07	1,06
PP	200	9	5	0,77	0,71
PP	200	12	2	0,76	0,94
PA	50	3	12	1,88	1,59

**Table 3:** Normalized mean errors for the different test cases studied in the paper